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Stabilization and electronic topological transition of hydrogen-rich metal $\text{Li}_5\text{MoH}_{11}$ under high pressures from first-principles predictions

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Regarded as doped binary hydrides, ternary hydrides have recently become the subject of investigation since they are deemed to be metallic under pressure and possibly potentially high-temperature superconductors. Herein, the candidate structure of $\text{Li}_5\text{MoH}_{11}$ is predicted by exploiting the evolutionary searching. Its high-pressure phase adopts a hexagonal structure with $P6_3/mcm$ space group. We used first-principles calculations including the zero-point energy to investigate the structures up to 200 GPa and found that the $P6_3cm$ structure transforms into the $P6_3/mcm$ structure at 48 GPa. Phonon calculations confirm that the $P6_3/mcm$ structure is dynamically stable. Its stability is mainly attributed to the isostructural second-order phase transition. Our calculations reveal the electronic topological transition displaying an isostructural second-order phase transition at 160 GPa as well as the topology of its Fermi surfaces. We used the projected crystal orbital Hamilton population (pCOHP) to examine the nature of the chemical bonding and demonstrated that the results obtained from the pCOHP calculation are associated with the electronic band structure and electronic localized function.

The success of experimental syntheses of metal hydrides has attracted considerable attention especially amongst the high-pressure research community, a corollary to discoveries—both experimental and theoretical—of a variety of interesting physical properties of these materials^{1–8}. Also, metal hydrides have long been considered as one of the best candidates for high-temperature superconductors. The superhydride Ce-H system, for instance, was successfully synthesized using the laser-heated diamond anvil cell (DAC) accompanied with synchrotron X-ray diffraction, which was theoretically confirmed by the evolutionary variable-composition simulation indicating that CeH_9 adopts a hexagonal clathrate structure with the $P6_3/mmc$ symmetry and potentially produces high-temperature superconductivity with estimated T_c of 105–117 K at 200 GPa⁹. Another metal-hydride superconductor of LaH_{10} with $T_c = 260$ K, approaching room temperature, was synthesized and experimentally observed under pressure between 180–200 GPa¹⁰, while it was suggested by a subsequent theoretical study to adopt a sodalite-like clathrate structure with $Fm\bar{3}m$ symmetry and exhibit a decreasing trend in T_c under an increase of pressure¹¹. Additionally, LaH_{11} is expected to produce high T_c as theoretically predicted¹² as well as several other materials^{13–19}.

More recently, ternary superhydrides (compounds each consisting of two substituted metal elements and hydrogen atoms) have been proposed to achieve metallicity and that one can expect a near room-temperature superconductivity out of them^{10,11,17,18}. However, the ternary hydride $\text{Li}_5\text{MoH}_{11}$ does not at all exhibit high-temperature superconductivity under high pressure, only with its maximum T_c of 6.5 K at 160 GPa belonging to the high-pressure phase²⁰. $\text{Li}_5\text{MoH}_{11}$ being one of the family of the hydrogen-rich metals $\text{Li}_5\text{MH}_{11}$, where M

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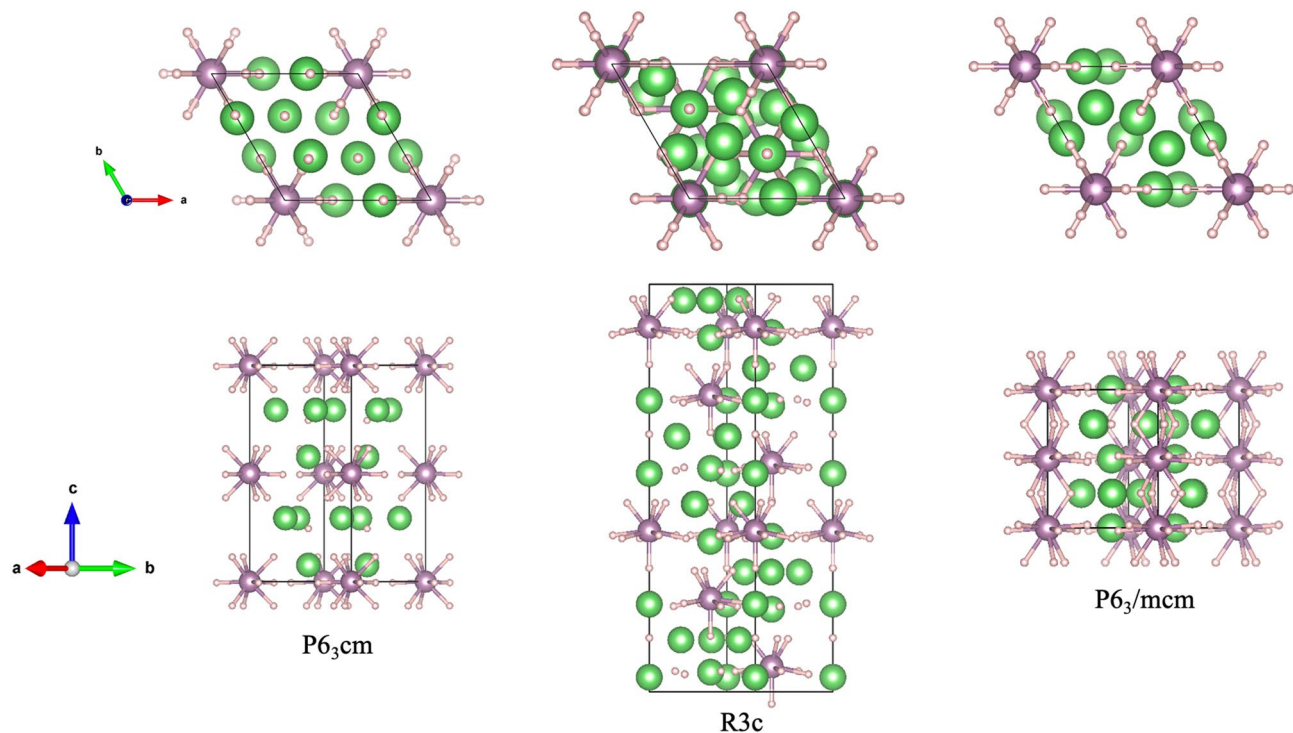


Figure 1. The crystal structures of $\text{Li}_5\text{MoH}_{11}$. The green, purple, and pink spheres represent, respectively, Li, Mo, and H atoms. (drawn by VESTA (ver. 3.4.7)⁶⁵ (URL <https://jp-minerals.org/vesta/en/download.html>)).

= Mo, W, Nb, and Ta²¹, adopts a hexagonal structure with the $P6_3cm$ space group at ambient pressure, which is constructed via the ionic bonds of *i.e.* Li^+ , H^- , and the ninefold-hydrogen-coordinated $[\text{MoH}_9]^{3-}$. The structure was also predicted in theory to exhibit an insulator–metal transition under compression²¹. As for $\text{Li}_5\text{MoH}_{11}$, it was revealed that the $P6_3cm$ structure transforms into the Cc and Pc structures at 5 GPa and 94 GPa, respectively²¹. Not long ago an experimental study utilizing high-pressure synchrotron x-ray diffraction (XRD) cast doubt on the ambiguity in structural determination of this ternary compound. According to the observation, the Cc and Pc structures do not exist at the predicted pressures (5 GPa and 94 GPa, respectively) as well as the fact that at higher pressure the crystal structure of $\text{Li}_5\text{MoH}_{11}$ cannot also be determined experimentally²⁰.

In this work, we aimed to identify the unknown structure of $\text{Li}_5\text{MoH}_{11}$ above 160 GPa, taking the crystal structure obtained from experiment as the starting structure throughout the entire calculation, by using the Universal Structure Predictor: Evolutionary Xtallography (USPEX). It is well-known that the standard spin-polarized DFT calculation, specifically within the generalized gradient approximation (GGA functional), cannot successfully describe the d -orbital of a transition metal²², e.g. Mo atom²³, due highly to the strongly correlated orbitals. In order to fully take into account the valence states of Mo atom, we performed the GGA+U calculations with the objective of correctly determining the reliable values of U_{eff} for $\text{Li}_5\text{MoH}_{11}$. Regarding its potential for superconductivity, the electronic structure and the nature of the chemical bonding observed by the experimental study²⁰ were shown to propound a possibility of T_c . Again, the aforementioned experimental observation found that $\text{Li}_5\text{MoH}_{11}$ has two different superconducting phases, indicating that a phase transition at 160 GPa might be expected to be an isostructural second-order phase transition, while the possibility of which is supported by means of an electronic topological transition (ETT). The concept of ETT has successfully been used to describe the nature of the electronic structures in several materials^{24–28}, particularly the metal hydride class²⁴. It was also shown that ETT plays a crucial role in electronic band structure via the association with the topology of the Fermi surface (FST)^{29,30}. In effect, the relationship between ETT and FST provides new insight into the nature of the electronic structure of $\text{Li}_5\text{MoH}_{11}$, as will be discussed later. We also support results of electronic band structure and electron localized function by demonstrating the projected crystal orbital Hamilton population (pCOHP) method.

Results and discussion

We used USPEX to predict the crystal structure of the hydrogen-rich metal $\text{Li}_5\text{MoH}_{11}$ under high pressure and found that there exist two low-enthalpy structures adopting structurally identical hexagonal structures with $R3c$ and $P6_3/mcm$ space groups. The predicted structures are shown in Fig. 1, while the optimized structural parameters for the $R3c$ and the $P6_3/mcm$ structures are presented in Table 1. Subsequently the calculated structural parameters have been fitted to the Birch–Murnaghan equation of state (EOS), as summarized in Table 2. We initially conjectured that Mo^- might accept electrons from the surrounding Li^+ cations under pressure²³. Also, Mo atom is reported to have an unusual spin-coupling that eventually modifies the oxidation state³¹. We thus applied the GGA and GGA+ U_{eff} methods to investigate the possibility of this effect. In both cases, Mo^- was

Space group	Pressure (GPa)	Lattice parameters Å, °	Atomic coordinates (fractional)
R3c	60	a = 5.104 b = 5.104 c = 18.990	Li1 (0.989, 0.564, 0.960)
		$\alpha = 90^\circ \beta = 90^\circ \gamma = 120^\circ$	Li2 (0, 0, 0.714)
			Li3 (0.667, 0.333, 0.869)
			Mo1 (0, 0, 0.895)
			H1 (0.317, 0.987, 0.709)
			H2 (0.876, 0.540, 0.796)
			H3 (0.345, 0.002, 0.883)
			H4 (0, 0, 0.803)
P6 ₃ /mcm	160	a = 4.644 b = 4.644 c = 5.638	Li1 (0.667, 0.333, 1)
		$\alpha = 90^\circ \beta = 90^\circ \gamma = 120^\circ$	L2 (1, 0.587, 0.750)
			Mo1 (0, 0, 1)
			H1 (1, 0.221, 0.750)
			H2 (0.634, 0, 1.024)
			H3 (0.333, 0.667, 0.75)

Table 1. Structures of Li₅MoH₁₁.

Space group	V ₀ (Å ³)	B ₀ (GPa)	Method
P6 ₃ cm	151.1	21.9	Without ZPE
P6 ₃ cm	133.9	42.4	ZPE
R3c	144.3	21.8	Without ZPE
R3c	166.5	10.5	ZPE
P6 ₃ /mcm	109.7	51.5	Without ZPE
P6 ₃ /mcm	97.3	114.8	ZPE

Table 2. The structural parameters calculated by the Birch–Murnaghan equation of state.

found to not accept any electron from the surrounding Li⁺ cations due to the fact that the predicted structure of Li₅MoH₁₁ structure is verified as being nonmagnetic (NM), since its magnetization is equal to zero. The selected value of U_{eff} plays a decisive role in structural stability as well^{32–35}. In the case of Li₅MoH₁₁, we thus evaluated the corresponding structural phase transition and electronic properties without incorporating U_{eff} .

The structural phase transitions of Li₅MoH₁₁ are presented by the relative enthalpy, which is obtained from the difference between the enthalpy calculated and that of the P6₃cm structure, as a function of pressure. According to our calculations, the P6₃cm structure transforms into the R3c structure at 48 GPa, followed by the existence of the P6₃/mcm structure at 64 GPa, as shown in Fig. 2a. Addition to this, the corresponding structural stability is further confirmed by the incorporation of the zero-point energy (ZPE) of the nuclei estimation, indicating that the R3c structure is not energetically favored at all throughout the whole pressure range, as shown in Fig. 2b. Rather, the P6₃cm crystal only transitions into the P6₃/mcm structure at 48 GPa, which was previously pointed out that the R3c structure becomes unstable when taking into account the effect of ZPE^{36–38}. The P6₃/mcm structure, therefore, is thermodynamically stable over a wide range of pressures. When it comes to dynamical stability, the harmonic approximation incorporating ZPE of nuclei scheme is used to investigate the nature of the lattice dynamics of Li₅MoH₁₁. Reported in Fig. 3a, the phonon dispersions accounting for P6₃cm structure at 40 GPa was computed and the structure is demonstrated to be stable, whereas upon a compression up to 50 GPa this symmetry is dynamically unstable due to the presence of negative frequency branches, as evidenced in Fig. 3b. In effect, the P6₃cm structure has a tendency to transform into the P6₃/mcm structure at this very pressure. The inclusion of ZPE calculation apparently plays a crucial role in determining the stable structure of Li₅MoH₁₁ under pressure, as previously demonstrated in other metal hydride systems^{39,40}. Regarding the R3c phase, the responsible pressure-dependent phonon dispersion displays a tiny soft-mode at the Γ -point which is shown in Fig. 3c, accompanied by a zoomed-in $K - \Gamma - M$ path in Fig. 3d. This suggests a possibility of becoming a meta-stable structure for the R3c phase, while the really stable phase belongs to the P6₃/mcm structure.

Upon a series of compression, the P6₃/mcm structure is clearly confirmed to be dynamically stable by the absence of negative frequency in the phonon spectra, as can be seen in Fig. 4, which implies that the compression promoted the global minimum enthalpy of the structure. At this point, we found that the P6₃/mcm structure is dynamically favored over the P6₃cm and R3c structures under a wide range of pressure, i.e., beginning at 80 GPa. According to the phonon density of states responsible for both Li and H atoms at around 25 THz (Fig. 4b–d), it is obvious that there exists coupling phonon branches, while they each tend to separate and eventually result in the intermediate optical phonon modes. It is worth noting that there remains the plausibility for Li₅MoH₁₁ to have a phase transition due to the fact that it was previously observed to superconduct with two different

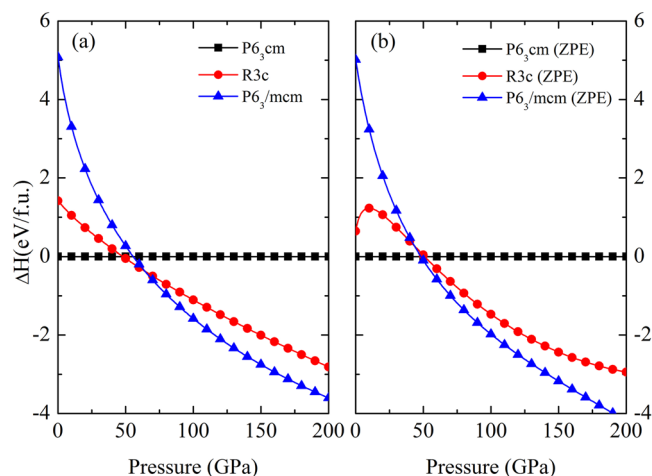


Figure 2. (a) The relative enthalpy as a function of pressure of $\text{Li}_5\text{MoH}_{11}$ without ZPE and (b) the relative enthalpy as a function of pressure of $\text{Li}_5\text{MoH}_{11}$ with ZPE.

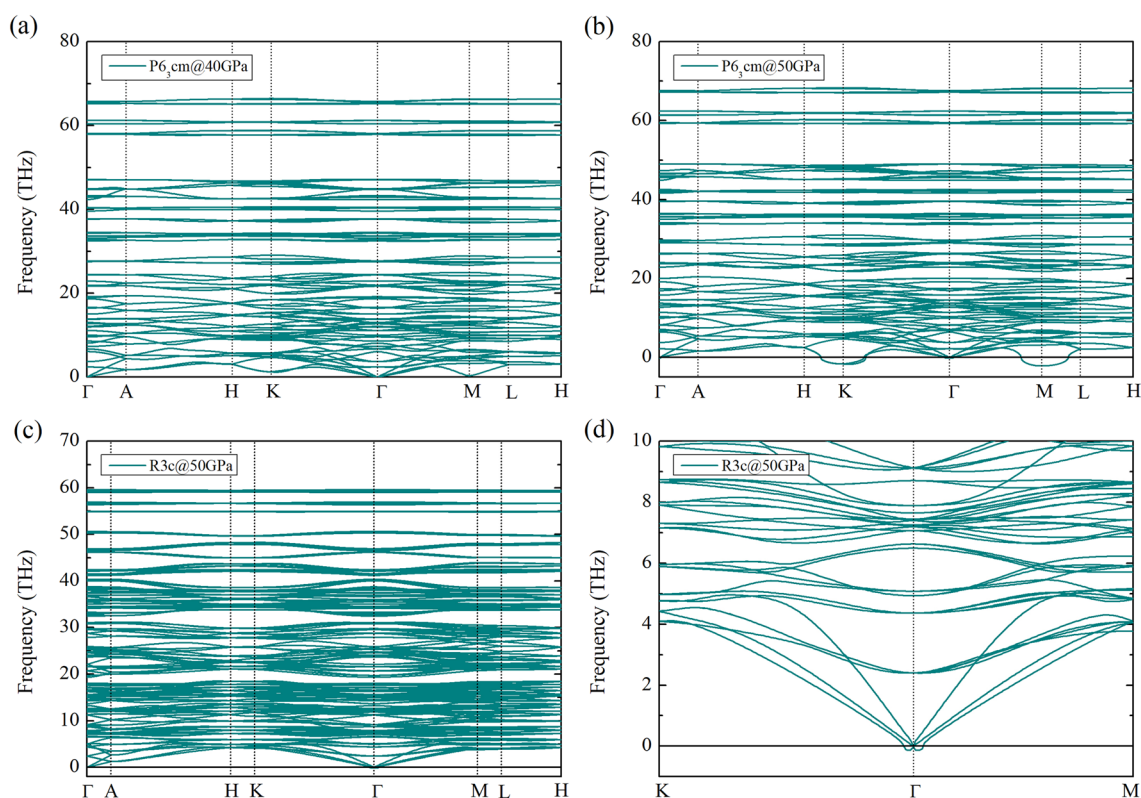


Figure 3. The phonon dispersion of $\text{Li}_5\text{MoH}_{11}$ (a) $\text{P6}_3/\text{cm}$ at 40 GPa. (b) $\text{P6}_3/\text{cm}$ at 50 GPa (c) R3c at 50 GPa (d) soft-mode at the Γ -point of R3c at 50 GPa.

superconducting phases at 160 GPa²⁰. At this point, however, it is difficult to verify whether there exists another phase of $\text{Li}_5\text{MoH}_{11}$ aside from the $\text{P6}_3/\text{mcm}$ structure, which, as a consequence, is expected to undergo the isostructural second-order phase transition above 160 GPa, as previously pointed out by means of the appearance of the intermediate optical phonon modes⁴¹.

The electronic band structures of the $\text{P6}_3/\text{mcm}$ $\text{Li}_5\text{MoH}_{11}$ under varying pressures are plotted in Fig. 5a–d. The Mo atom's 4d orbitals split into two energy levels, i.e. E_{2g} (d_{xy} , $d_{x^2-y^2}$) and E_{1g} (d_{yz} , d_{xz}), whereas the Li atom's 2p orbitals yield the E_{1u} (p_x , p_y) and the A_{2u} (p_z) orbitals as well as into the A_{1g} orbital arising from the H atom's 1s orbital. The band structure evidences a coupling between the E_{2g} of Mo atom and the E_{1u} orbitals of Li atom and reveals a Dirac-like cone, as also found recently^{42,43}, at the Γ -point in Fig. 5a, which is originated from the coupling between the δ - and π -bonds. Upon an increase of pressure, particularly at 100 GPa (see Fig. 5b), the

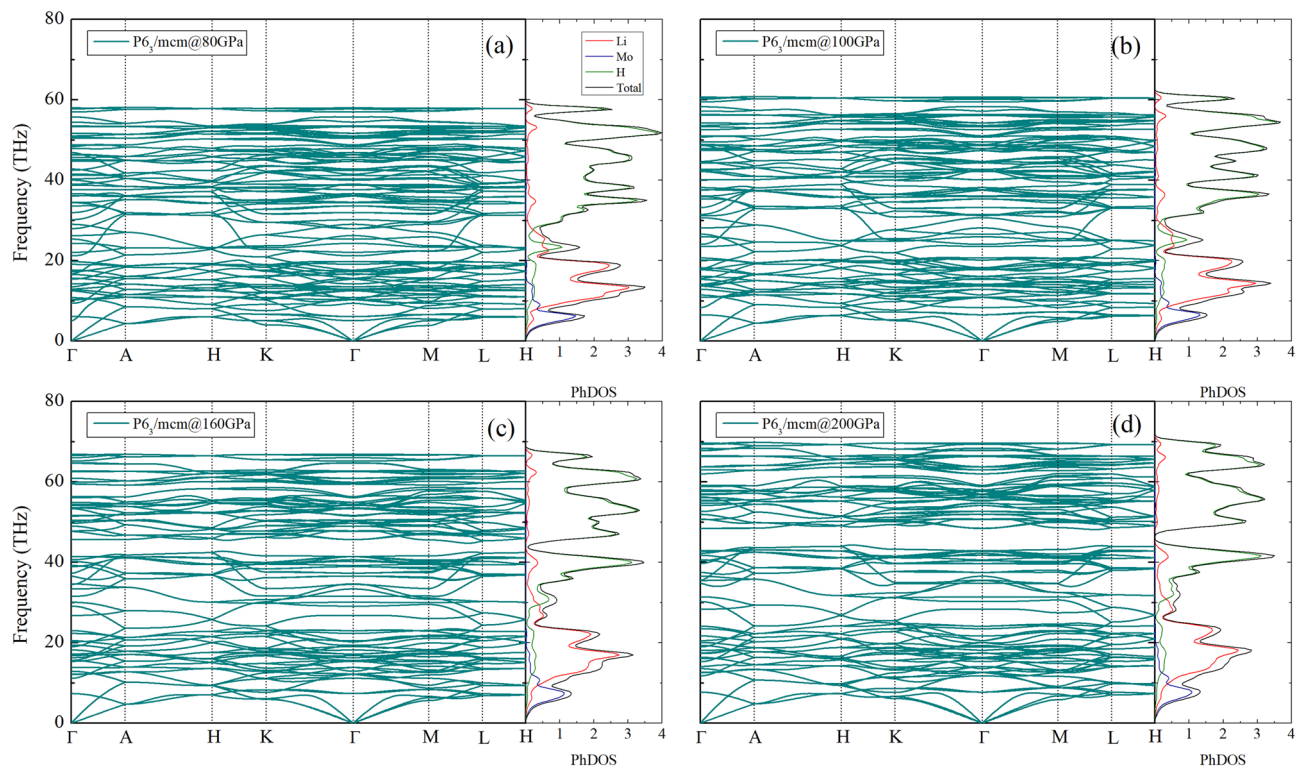


Figure 4. The phonon dispersion of $\text{Li}_5\text{MoH}_{11}$ (a) $\text{P6}_3/\text{mcm}$ at 80 GPa, (b) $\text{P6}_3/\text{mcm}$ at 100 GPa, (c) $\text{P6}_3/\text{mcm}$ at 160 GPa, and (d) $\text{P6}_3/\text{mcm}$ at 200 GPa, respectively.

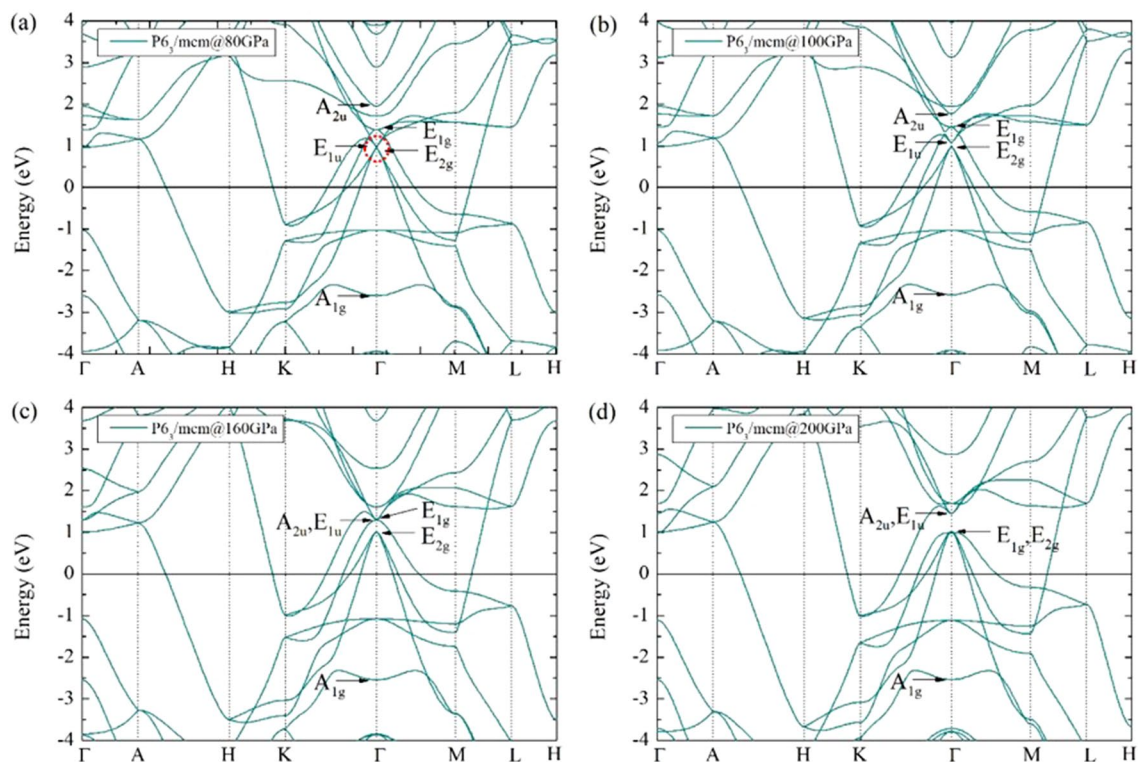


Figure 5. The band structure of $\text{Li}_5\text{MoH}_{11}$ (a) $\text{P6}_3/\text{mcm}$ at 80 GPa, (b) $\text{P6}_3/\text{mcm}$ at 100 GPa, (c) $\text{P6}_3/\text{mcm}$ at 160 GPa, and (d) $\text{P6}_3/\text{mcm}$ at 200 GPa, respectively.

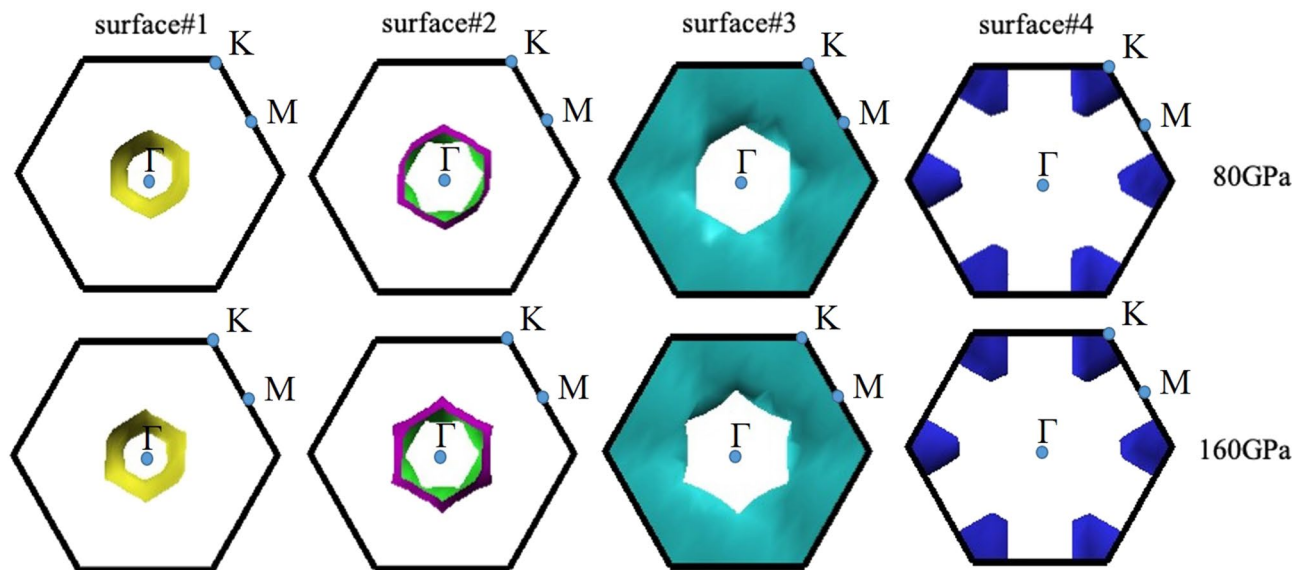


Figure 6. Sketch of FST of $P6_3/mcm$ at 80 and 160 GPa, respectively (drawn by XCrySDen program (ver. 1.5.60)⁶⁶ (URL http://www.xcrysdn.org/Download.html#_toc_11)).

separation of the E_{2g} orbitals of Mo and the E_{1u} orbitals of Li become apparent. This implies the electronic topological transition, which is referred to as the Lifshitz transition⁴⁴. The following dispersion (see Fig. 5c) displays a downward shift of the A_{2u} orbitals of Li, which in turn leads to the coupling between the E_{1u} orbital of Li and the E_{1g} orbital of Mo that exhibit the σ - π bonding, at 160 GPa, when eventually the latter is roughly level with the E_{2g} orbitals of Mo atom at 200 GPa also exhibiting σ - δ bonding. Likewise, the A_{2u} orbitals of Li continue to couple with the E_{1u} orbitals of Li despite the increase of pressure, which results in σ - π bonding. As mentioned earlier, isostructural second-order phase transition induced by the $P6_3/mcm$ structure can be made possible by the Lifshitz transition. Moreover, the electronic band structures show no sign of flat bands near the Fermi level. Even though a set of flat bands can be spotted near the Fermi level as well as the presence of van Hove singularities (vHs) within H_3S ¹³, YH_6 and YH_{10} ¹⁴ systems, leading to the possibility of achieving high values of T_c , this can be alternatively explained by the shape of the electronic band structure or density of states of our system. Our system's electronic structures are similar to those found in YSH_6 ¹⁵, $LaSH_6$ ¹⁵, CeH_9 ¹⁶, and CeH_{10} ¹⁹, in terms of steep branches near the Fermi level. However, we found that Li_5MoH_{11} does not exhibit high-temperature superconductivity. As an explanation, the energy level of the H atom (the A_{1g} orbitals) is lower than the Fermi level by -2.605 to -2.538 eV at 80 to 200 GPa, respectively, which further supports the implication that the high-pressure phase observed by experiment does not give high-temperature superconductivity²⁰.

Another key finding that needs to be mentioned is the Fermi surface topology (FST). It is well-known that the FST is associated with an electronic topological transition (ETT), which originates from a given electronic band structure^{24–28}, that plays a key role in promoting the second-order phase transition⁴⁵. This was previously emphasized in previous studies^{29,30} the change of material's topology is promoted by a compression. As depicted in Fig. 6, the characteristics of the FST clearly increase the likelihood of isostructural second-order phase transition: there are individual variations in surface#2 and surface#3 at 160 GPa, compared to those at 80 GPa. The topological changes in FST corresponds to the electronic band structures calculated. Thus the isostructural second-order phase transition of Li_5MoH_{11} can be described by the presence of ETT. More interestingly, surface#2 and surface#3 both form the Fermi surface nesting at the pockets surrounding the Γ -point at 160 GPa, holding a vital clue to superconductivity²⁹.

The likelihood of finding an electron in the neighborhood space of Li_5MoH_{11} can be measured by the electron localization function (ELF)⁴⁶, as reported in Fig. 7a. The tendency of electron localization in the $P6_3/mcm$ structure is described by uniform electron gas of the same density^{19,47–50}. The calculated ELF reveals a set of chemical bonding at 0 GPa. The distances between the first (Li–Mo), second (Li–H), third (Mo–H), and fourth (H–H) nearest neighbors (NN) read 2.94826 Å, 1.83412 Å, 1.90874 Å, and 2.24193 Å, respectively. There exists electronic probability weakly accumulating between the first NN Li–Mo, the second NN Li–H, and the third NN Mo–H, particularly the bonding between the fourth NN H–H which indicates that it is likely to be a strong bonding at 0 GPa. Upon further compression up to 160 GPa, the ELF displays that the distance between the first NN Li–Mo, second NN Li–H, third NN Mo–H, and fourth NN H–H are 2.38216 Å, 1.55862 Å, 1.70037 Å, and 1.27095 Å, respectively. It is worth noting that there is also a strong bonding between H and H, and the increase of electronic distribution between Mo and H at 0 GPa, implying that H–H bonding is likely to be a strong covalent bonding. We further investigated the nature of the chemical bonding near the Fermi level by with the aid of the projected crystal orbital Hamilton populations (pCOHP) calculation, which enables the determination of anti-bonding and bonding characteristics, e.g., covalent bonds, along energy range^{51–53}. Illustrated in Fig. 7b, it is obvious that the projected wave function of the Li–Mo bonding displays anti-bonding, in a good agreement with ELF and corresponds to anti-bonding in the electronic band structure⁵⁴. Our calculations also reveal that the E_{1u} orbitals

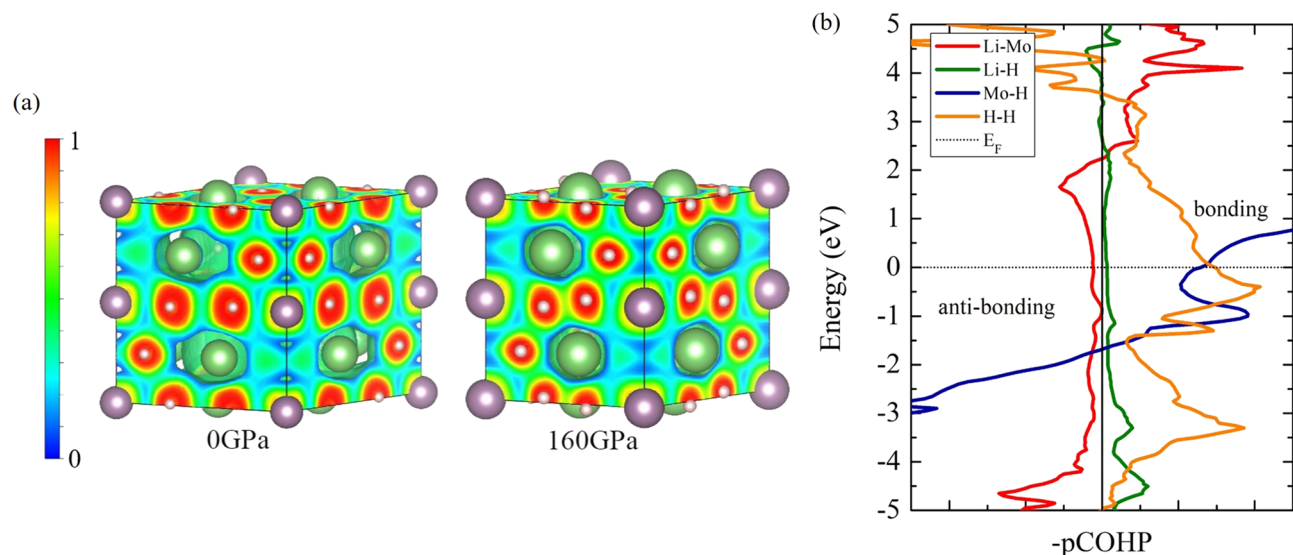


Figure 7. (a) The 3D-electron localization function (ELF) in $\text{Li}_5\text{MoH}_{11}$ structure at 0 and 160 GPa, respectively. (drawn by VESTA (ver. 3.4.7)⁶⁵ (URL <https://jp-minerals.org/vesta/en/download.html>)) (b) Projected crystal orbital Hamilton populations (pCOHPs) in $\text{Li}_5\text{MoH}_{11}$ structure at 160 GPa.

and the E_{1g} orbitals exhibit the σ - π bonding, by a determination of the electronic band structure. The projected wave function of the Li-H bonding is proved to be an ionic bond, which is confirmed by the ELF calculation, while those of the Mo-H and H-H bondings are indicated to be covalent bonds. In particular, the ELF calculation remarkably suggests a strong covalent bond as a result of the H-H bonding. So, the characteristic of the Li-Mo anti-bonding implies that $\text{Li}_5\text{MoH}_{11}$ cannot achieve a high value of T_c .

Conclusion

In this work, we identify the high-pressure phases of $\text{Li}_5\text{MoH}_{11}$ by performing an evolutionary searching. Our calculations show that by incorporating the zero-point energy evaluation the $P6_3/mcm$ structure is thermodynamically and dynamically favored over the $P6_3cm$ and $R3c$ structures above 50 GPa. The perspective of theoretical inspection points out that the $P6_3/mcm$ structure exists under high pressure adopting the hexagonal basis. Phonon dispersion calculations and the electronic topological transition reveal that the $P6_3/mcm$ structure exhibits an isostructural second-order phase transition. Also, we have shown that the topology of the Fermi surface is associated with the electronic band structure, which nonetheless does not exhibit any flat bands near the Fermi level. This reflects that fact that $\text{Li}_5\text{MoH}_{11}$ does not have a high value of T_c . Here, our calculations support the experimental observations of T_c in the previous study²⁰. The nature of the chemical bonding is associated with the electronic band structure, implying that the characteristics of the chemical bonding entail the value of T_c .

Methods

The searching for the structures of the hydrogen-rich metal $\text{Li}_5\text{MoH}_{11}$ was performed by USPEX⁵⁵. In all subsequent generations, the random symmetric algorithm employed 40% heredity, 20% random symmetric, 20% soft mutation, and 20% transmutation operators in the pressure range from 160 to 200 GPa with structures containing up to four formula units. All structures were fully relaxed using the generalized gradient approximation of the Perdew-Burke-Ernzerhof (GGA-PBE) functional⁵⁶ as the exchange-correlation functional. We selected the projector augmented wave (PAW) method⁵⁷ to describe the core and valence electrons as well as the conjugate gradient scheme, as implemented in the Vienna *ab initio* simulation package (VASP)⁵⁸. A plane-wave basis set up to a cutoff energy of 700 eV and a $10 \times 10 \times 4$, $12 \times 12 \times 4$, and $12 \times 12 \times 10$ k -point meshes generated by the Monkhorst-Pack (MP) method⁵⁹ were used for the $P6_3cm$ structure, the $R3c$ structure, and the $P6_3/mcm$ structure, respectively. The pseudocore radii of Li, Mo, and H account for 1.7, 2.50, and 0.80 Bohr, respectively, which are small enough to ensure that no overlap of spheres will occur under applied pressure. The zero-point energy of the nuclei (ZPE) is estimated within the harmonic approximation, which was included in the enthalpies as a function of the pressure. All values of enthalpy of all structures obtained were fitted by a Birch-Murnaghan equation of state (EOS). The dynamic stable structures were calculated by using the *ab initio* lattice dynamics with the supercell approach, as implemented in the VASP code together with the PHONOPY package⁶⁰. The plane-wave energy cutoff of 60 Ry was selected as well as a $12 \times 12 \times 10$ k -point mesh was used for the $P6_3/mcm$ structure. Based on the linear response theory⁶¹, the GGA+ U was selected as a means to perform the Hubbard U calculation which is implemented in Quantum Espresso (QE) package⁶². The effective interaction parameters of which were tested to be $U_{\text{eff}} = U - J = 1.2$ eV. The projected crystal orbital Hamilton population⁶³ (pCOHP) was used to describe the chemical bonding of the $P6_3/mcm$ structure, as implemented in LOBSTER code⁶⁴.

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Author contributions

Author contributions: P.T. and T.B. designed the research; P.T. and T.B. performed the research; P.T. and T.B. analysed the data; and P.T., R.A., W.L., and T.B. wrote the paper; W.S. and T.B. corrected the paper.

Competing interests

The authors declare no competing interests.

Additional information

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