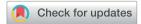
# **RSC Advances**



## **PAPER**



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# Estimation of the tensile modulus of polymer carbon nanotube nanocomposites containing filler networks and interphase regions by development of the Kolarik model

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In this paper, the Kolarik model for the tensile modulus of co-continuous blends based on cross-orthogonal skeleton structures is simplified and developed for polymer/carbon nanotube (CNT) nanocomposites assuming continuous CNT networks in the polymer matrix and the reinforcing and percolating efficiencies of the interphase. For this purpose, the Ouali model for the modulus of nanocomposites above the percolation threshold is linked with the Kolarik model and the interphase percolation is considered with the excluded volume of the nanoparticles. In addition, the simplified Kolarik model is developed with the interphase as a new phase surrounding the nanofiller. A good agreement between the experimental data and the predictions is observed in the samples containing interphases and filler networks, while the developed model cannot estimate the modulus in the absence of interphases and network structures. The developed model demonstrates the effects of all the parameters on the modulus. The interphase parameters more significantly affect the modulus compared to the concentration and modulus of the filler, demonstrating the importance of the interphase properties.

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### 1 Introduction

A large amount of effort has been deployed to develop highperformance polymer nanocomposites for the benefit of nanotechnology, including the combination of nano-reinforcements with polymer matrices.<sup>1-5</sup> Widespread research on polymer nanocomposites has been conducted to suggest novel materials for various applications. Carbon nanotubes (CNTs) have attracted much attention as innovative nanofillers for polymer nanocomposites since their discovery in 1991.6-9 CNTs consist of a single or several graphite layers with diameters of 1-100 nm and lengths of about 5 to a few tens of microns. Also, they show Young's moduli of around 1000 GPa as well as tensile strengths of 10-50 GPa.10 So, CNTs exhibit extraordinary physical properties such as high aspect ratios (length per diameter) and large surface areas as well as excellent mechanical performance which properly justifies their addition to polymer matrices. However, the advantages of CNTs are realised in polymer nanocomposites when they are uniformly dispersed in the polymer matrix, because they seriously tend to aggregate/ agglomerate during processing.<sup>11</sup>

Besides the outstanding mechanical performance of polymer/CNT nanocomposites (PCNTs), the electrical conductivity of these materials is also attractive. Polymers are commonly insulating, limiting their application in various fields such as electronics, sensors, etc. 12,13 Conductivity is obtained in nanocomposites above a determinate filler concentration known as the percolation threshold.<sup>14,15</sup> At percolation, a conducting network forms in the polymer matrix, which transfers electrons and creates the conductivity. As a result, obtaining a smaller percolation threshold is important in PCNTs. In addition, a percolation threshold was also observed in the mechanical properties of polymer nanocomposites, named as mechanical percolation. Some authors have interpreted the high levels of modulus in reinforced composites and nanocomposites by mechanical percolation. 16-18 Since the percolation threshold is inversely related to the aspect ratio of particles, PCNTs generally show very low percolation thresholds which promotes the electrical conductivity and mechanical behavior with a low content of CNTs. 19-21

In conventional composites containing reinforcements, a thin interface layer usually covers the particles. However, its thickness is much smaller than the filler size in most cases. Therefore, the presence of interfaces negligibly affects the overall properties of the composites. But, the dimensions of the interface layers in polymer nanocomposites containing large-

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surface-area nanoparticles are often comparable to the nanoparticle size forming a different phase as the interphase around the nanoparticles.22,23 The interphase has a substantial effect on the overall properties of the nanocomposites and previous researchers have investigated the reinforcing role of the interphase in polymer nanocomposites.24-26 Since the interphase level significantly controls the mechanical performance of the nanocomposites, some authors have characterized the interphase by the modeling of the mechanical properties. In this area, some conventional models such as Halpin-Tsai and Mori-Tanaka were developed to include the interphase or some new models were suggested.27,28 In addition, the interphase areas can produce connected networks, which accelerate the mechanical percolation in polymer nanocomposites at a lower volume fraction of nanoparticles.<sup>29,30</sup> Consequently, the interphase affects the percolating role of the nanoparticles in the nanocomposites besides the reinforcing efficiency.

The electrical conductivities of composites were modeled by power-law equations, due to the rapid improvements in conductivities at the critical level of percolation. Following this approach, a few power-law models were also proposed for the tensile moduli of composites assuming the percolating effect. Ouali *et al.*<sup>31</sup> suggested a power-law model for the moduli of polymer composites above the percolation point. Kolařík<sup>32</sup> also proposed a cross-orthogonal skeleton (COS) configuration for the tensile modulus and yield strength of co-continuous polymer blends assuming the percolation threshold using a power-law equation. Nevertheless, these models cannot be well utilized for polymer nanocomposites, because they fail to address some important aspects such as the interphase.

In this study, the Kolarik model for the tensile moduli of cocontinuous blends is developed for PCNTs above the percolation threshold assuming a continuous network in the polymer matrix. This model is linked with the Ouali model to consider the percolation threshold. Moreover, both the reinforcement and percolation effectivenesses of the interphase area are assumed in the Kolarik model to expand its predictability for polymer nanocomposites. The predictions of this model are examined against the experimental results of several samples from the available literature and by the roles of different materials and interphase parameters in the modulus.

# 2 Model development

The COS structure suggested by Kolarik<sup>32</sup> includes three orthogonal bars of a component as a filler which are embedded in a unit cube as the total volume (Fig. 1). This construction was used for polymer blends with co-continuous arrangements. Moreover, when the network of CNTs in PCNTs is assumed to be a continuous phase in the polymer matrix, this model can be applied for PCNTs above the percolation threshold.

Based on the COS structure, Kolarik<sup>32</sup> calculated the tensile modulus of composites with co-continuous morphology using:

$$E = E_{\rm m} (1 - f^2) + E_{\rm f} f^2 + \frac{2f(1 - f)E_{\rm m}}{1 - f + fE_{\rm m}/E_{\rm f}}$$
(1)

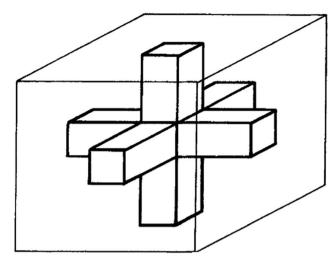


Fig. 1 Cross-orthogonal skeleton (COS) structure which consists of three orthogonal bars as reinforcement in a unit cube as a whole composite.<sup>32</sup>

$$1 - \phi_{\rm f} - (1 - f)^2 (1 + 2f) = 0 \tag{2}$$

where " $E_{\rm f}$ " and " $E_{\rm m}$ " are the tensile moduli of the filler and polymer matrix, respectively. Also, " $\phi_{\rm f}$ " is the filler volume fraction.

In PCNTs containing low concentrations of nanoparticles, the "f" parameter has very low values. So, the term (1-f) is approximated to 1. Also, since the modulus of CNTs is about 1000 GPa, the term  $fE_{\rm m}/E_{\rm f}$  can be disregarded. Therefore, the Kolarik model for PCNTs is simplified to:

$$E = E_{\rm m} + E_{\rm f} f^2 + 2f E_{\rm m} \tag{3}$$

However, the exact level of the "f" parameter cannot be easily determined. To show a definition for "f" assuming the networking of nanoparticles above the percolation threshold, the known Ouali model for the tensile moduli of composites containing filler networks is applied. It was mentioned that this model has been used for the tensile modulus of PCNTs in previous articles.

Ouali *et al.*<sup>31</sup> suggested a model based on the inverse rule of mixtures by the percolation concept as:

$$E = \frac{(1 - 2\psi + \psi\phi_{\rm f})E_{\rm m}E_{\rm f} + (1 - \phi_{\rm f})\psi{E_{\rm f}}^2}{(1 - \phi_{\rm f})E_{\rm f} + (\phi_{\rm f} - \psi)E_{\rm m}}$$
(4)

$$\psi = \phi_{\rm f} \left( \frac{\phi_{\rm f} - \phi_{\rm p}}{1 - \phi_{\rm p}} \right)^b \tag{5}$$

where " $\phi_p$ " is the volume fraction of the percolating phase and "b" is the percolation exponent. The "b" parameter commonly has a value of 0.4 in a 3D structure.<sup>31</sup> In addition,  $\psi=0$  below the percolation threshold reduces the Ouali model to the inverse rule of mixtures as:

$$E = \frac{E_{\rm m}E_{\rm f}}{\left(1 - \phi_{\rm f}\right)E_{\rm f} + \phi_{\rm f}E_{\rm m}} \tag{6}$$

The very low levels of " $\phi_{\rm f}$ " and " $\psi$ " in PCNTs can simplify eqn (4) to:

$$E = \frac{(1 - 2\psi)E_{\rm m}E_{\rm f} + \psi{E_{\rm f}}^2}{E_{\rm f}} = (1 - 2\psi)E_{\rm m} + \psi E_{\rm f}$$
 (7)

In addition, the " $\phi_p$ " parameter for cylindrical fillers such as CNTs<sup>33</sup> is given by:

$$\phi_{\rm p} = \frac{V}{V_{\rm ex}} \tag{8}$$

where "V" and " $V_{\rm ex}$ " are the volume and excluded volume of the nanoparticles, respectively. " $V_{\rm ex}$ " is defined as the volume about an element into which the center of a similar thing cannot arrive. "V" and " $V_{\rm ex}$ " for an unsystematic distribution of spherically capped CNTs<sup>33</sup> are expressed by:

$$V = \pi R^2 l + (4/3)\pi R^3 \tag{9}$$

$$V_{\rm ex} = \frac{32}{3} \pi R^3 \left[ 1 + \frac{3}{4} \left( \frac{l}{R} \right) + \frac{3}{32} \left( \frac{l}{R} \right)^2 \right]$$
 (10)

where "R" and "l" are the radius and length of the CNTs, respectively. So, the percolation threshold can be presented as:

$$\phi_{\rm p} = \frac{\frac{l}{R} + 4/3}{\frac{32}{3} \left[ 1 + \frac{3}{4} \left( \frac{l}{R} \right) + \frac{3}{32} \left( \frac{l}{R} \right)^2 \right]} \tag{11}$$

However, the interphase area around the nanoparticles may produce a network structure in PCNTs before the networking of the nanoparticles. Accordingly, the interphase region increases the excluded volume of each particle by changing "R" to "R + t" (t is the interphase thickness), while the volume of particles is constant. The excluded volume changes with the interphase to:

$$V_{\rm ex} = \frac{32}{3}\pi(R+t)^3 \left[ 1 + \frac{3}{4} \left( \frac{l}{R+t} \right) + \frac{3}{32} \left( \frac{l}{R+t} \right)^2 \right]$$
 (12)

which decreases the percolation threshold in eqn (8) to:

$$\phi_{p} = \frac{\pi R^{2}l + (4/3)\pi R^{3}}{\frac{32}{3}\pi (R+t)^{3} \left[1 + \frac{3}{4} \left(\frac{l}{R+t}\right) + \frac{3}{32} \left(\frac{l}{R+t}\right)^{2}\right]}$$
(13)

As a result, the percolation threshold of CNTs in PCNTs is expressed by the sizes of the nanoparticles and the interphase.

Eqn (3) is now linked to the simplified Ouali model (eqn (7)) to obtain an expression for the "f" parameter by the percolation effect which leads to following equation:

$$E_{\rm f}f^2 + 2fE_{\rm m} = -2\psi E_{\rm m} + \psi E_{\rm f} \tag{14}$$

The two terms " $2fE_{\rm m}$ " and " $-2\psi E_{\rm m}$ " are very much smaller than the other terms, because the modulus of the polymer matrix  $(E_{\rm m})$  is very slight compared to the CNTs' modulus  $(E_{\rm f})$ . So, eqn (14) can be simplified to:

$$E_{\rm f}f^2 = \psi E_{\rm f} \tag{15}$$

which suggests a connection between "f" and " $\psi$ " as:

$$f = \psi^{0.5} \tag{16}$$

The predictions of the Kolarik model are evaluated to validate this expression for the "f" parameter. Fig. 2 illustrates the calculations from the simplified Kolarik model for the expression of the "f" parameter in eqn (16) at average values  $E_{\rm m}=2$  GPa,  $E_{\rm f}=1000$  GPa, R=10 nm, l=10 µm and t=5 nm. Clearly, a higher CNT concentration causes an improved tensile modulus, which is reasonable for PCNTs containing CNT networks. Accordingly, eqn (16) is valid for the "f" parameter in the Kolarik model.

By substitution of " $\psi$ " from eqn (5) into eqn (16), the "f" parameter can be represented as:

$$f = \phi_{\rm f}^{0.5} \left( \frac{\phi_{\rm f} - \phi_{\rm p}}{1 - \phi_{\rm p}} \right)^{0.2} \tag{17}$$

when " $\phi_p$ " from eqn (13) is substituted into the latter equation, "f" is defined by the CNT and interphase dimensions. However, the calculations show that the "f" parameter can be further simplified.

Fig. 3a depicts the effects of the "R" and "l" parameters on "f" at average levels of  $\phi_{\rm f}=0.01$  and t=5 nm using a contour plot. Also, Fig. 3b shows the variation of the "f" parameter at different "t" levels at  $\phi_{\rm f}=0.01$ , R=10 nm and l=10 µm. It is well observed that the common ranges of the "t", "t" and "t" parameters cannot meaningfully change "t". In fact, the dissimilar levels of the "t", "t" and "t" parameters affect the percolation threshold, but the very low values of "t" cannot meaningfully change the "t" parameter.

Accordingly, the influence of " $\phi_p$ " on the "f" parameter is negligible and can be eliminated which simplifies eqn (17) to:

$$f = \phi_{\rm f}^{0.7} \tag{18}$$

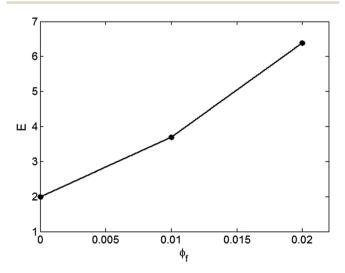


Fig. 2 Moduli predicted by the simplified Kolarik model at  $E_{\rm m}=2$  GPa,  $E_{\rm f}=1000$  GPa, R=10 nm, l=10  $\mu{\rm m}$  and t=5 nm.

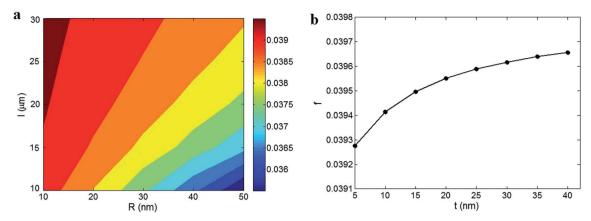


Fig. 3 The effects of (a) "R" and "I" factors shown using a contour plot and (b) the "t" parameter on the "f" parameter based on eqn (13) and (17).

where the "f" parameter only depends on the filler volume fraction and other factors cannot significantly vary it. The substitution of the "f" parameter from eqn (18) into eqn (2) also suggests the correct results which confirms the present equations.

By the substitution of eqn (18) into eqn (3), the Kolarik model for the tensile modulus of PCNTs above the percolation threshold is stated as:

$$E = E_{\rm m} + E_{\rm f}\phi_{\rm f}^{1.4} + 2\phi_{\rm f}^{0.7}E_{\rm m} \tag{19}$$

By dividing the latter equation by the matrix modulus ( $E_{\rm m}$ ), the relative modulus of PCNTs based on the suggested model is given by:

$$E_{\rm R} = 1 + \frac{E_{\rm f}\phi_{\rm f}^{1.4}}{E_{\rm m}} + 2\phi_{\rm f}^{0.7} \tag{20}$$

However, this model does not consider the interphase between the polymer matrix and the nanoparticles in polymer nanocomposites. Accordingly, its predictions for PCNTs cannot be accurate, because the interphase plays a significant role in the mechanical properties of nanocomposites, as mentioned previously. Since the interphase forms around the nanoparticles, it can be assumed to be a separate phase in addition to the nanoparticles in the Kolarik model (eqn (20)) as:

$$E_{\rm R} = 1 + \frac{E_{\rm f}\phi_{\rm f}^{1.4}}{E_{\rm m}} + 2\phi_{\rm f}^{0.7} + \frac{E_{\rm i}\phi_{\rm i}^{1.4}}{E_{\rm m}} + 2\phi_{\rm i}^{0.7}$$
 (21)

where " $\phi_i$ " and " $E_i$ " are the volume fraction and modulus of the interphase, respectively. Similarly, the term " $\phi_i$ " is expressed by the radius of the CNT and the thickness of the interphase in PCNTs<sup>34</sup> as:

$$\phi_{\rm i} = \phi_{\rm f} \left[ \left( 1 + \frac{t}{R} \right)^2 - 1 \right] \tag{22}$$

By the substitution of eqn (22) into eqn (21), the developed model shows that the tensile modulus of PCNTs containing filler networks depends on the properties of the nanoparticles and the interphase. Also, the experimental results of the tensile modulus as well as the radii of the CNTs can be applied to this model to calculate the average levels for the interphase parameters.

### 3 Results and discussion

Experimental results from the literature are applied to evaluate the developed model and predict the interphase properties and percolation threshold. Likewise, the variation of the modulus at different parameter levels is plotted and discussed to confirm the correctness of the developed model.

Fig. 4 illustrates the experimental results for polyamide 6 (PA6)/multiwall CNT (MWCNT),  $^{35}$  epoxy/MWCNT $^{36}$  and chitosan/MWCNT $^{37}$  samples and the calculations of the developed model. The R and  $E_{\rm m}$  levels in nm and GPa units are reported as 6 and 2.45, 25 and 0.52 and 8, and 2 for these samples from their references, respectively. A good agreement between the experimental data and the calculations is observed for these reported samples at all of the filler fractions demonstrating that the developed model can properly estimate the tensile modulus of PCNTs. In fact, the developed model can predict the modulus of PCNTs by assuming the reinforcing and percolating roles of the nanoparticles and the interphase.

The comparable nature of the experimental results with the predictions shows that the samples contain filler networks and interphases. The average t and  $E_{\rm i}$  values in nm and GPa units are obtained as 4 and 40, 6 and 80, and 12 and 150 for PA6/MWCNT, epoxy/MWCNT and chitosan/MWCNT samples, respectively, based on the predictions. So, it is concluded that the developed model can estimate the values of the interphase properties by the experimental measurements of tensile modulus.

Furthermore, this model can compare the average values of the interphase properties. According to t and  $E_i$  values, the chitosan/MWCNT sample shows the highest interphase, while the PA6/MWCNT nanocomposite shows the lowest. The interphase level generally depends on the interfacial interaction/adhesion between the polymer matrix and the nanoparticles. The MWCNTs covalently bonded to the chitosan matrix show the highest interfacial adhesion, while poor interaction between the PA6 matrix and MWCNTs in the PA6/

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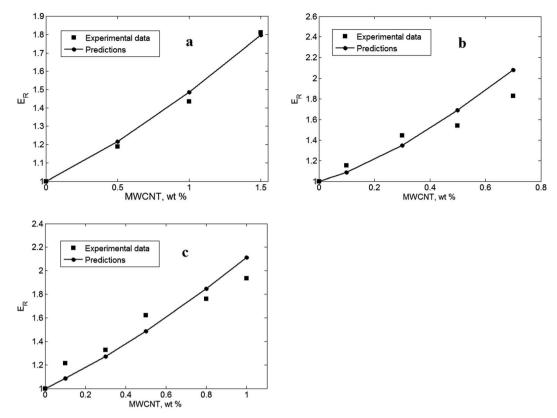


Fig. 4 Comparison between the experimental results and the calculations of the developed model for (a) PA6/MWCNT,<sup>35</sup> (b) epoxy/MWCNT<sup>36</sup> and (c) chitosan/MWCNT<sup>37</sup> samples.

MWCNT sample causes poor interphase characteristics. Additionally, the levels of " $\phi_p$ " in the presence of the interphase can be calculated by eqn (13). The average length of CNTs in all samples is assumed to be 10 µm. " $\phi_p$ " was calculated as 0.0004, 0.002 and 0.0003 for PA6/MWCNT, epoxy/MWCNT and chitosan/MWCNT samples, respectively. All samples show a very low value of " $\phi_p$ " indicating the formation of filler networks by very low amounts of CNTs. The highest " $\phi_p$ " is obtained for chitosan/MWCNT, due to it having the thickest interphase, while the epoxy/MWCNT example shows the worst percolation level, because of the high CNT radius. According to eqn (13), the percolation level of CNTs in PCNTs correlates to the dimensions of both the CNTs and the interphase.

The developed model also overpredicts the modulus in some samples. Since the presented model considers the interphase and filler networks in PCNTs, which play significant roles in the mechanical behavior of nanocomposites, the overprediction of the developed model demonstrates the absence of these terms in the nanocomposites. In fact, the nonappearance of the interphase and CNT network leads to a poor modulus in some samples and thus, the developed model cannot predict these low levels.

Fig. 5 depicts the experimental and theoretical results based on the developed model at  $t=E_{\rm i}=0$  in four samples from previous articles including PA6/MWCNTs,<sup>40</sup> PVA/MWCNTs,<sup>41</sup> polypropylene/MWCNTs<sup>42</sup> and PA6/MWCNTs.<sup>43</sup> The predictions are higher than the experimental results even at  $t=E_{\rm i}=0$  which

shows the absence of the interphase and CNT networks in all of the samples. Therefore, the developed model can predict the formation of the interphase and filler networks in PCNTs by proper calculations, while it can also show the nonexistence of these terms through overprediction.

As mentioned, poor interfacial interaction/adhesion between the polymer matrix and MWCNTs and the high level of the percolation threshold can result in the absence of the interphase and filler networks, respectively. The interfacial adhesion can be improved by some techniques such as functionalization of the filler surface by acids. 44,45 Since the interphase level makes a positive effect on the percolation threshold, the improvement of the interfacial properties decreases the percolation threshold and helps the formation of filler networks. Moreover, the discrepancy between the experimental and theoretical data rises at higher concentrations of CNTs. It seems that the aggregation/agglomeration of nanoparticles at high filler fractions weakens the interfacial properties and causes large differences between the measured and the predicted moduli.

The influences of various parameters on the predictions are discussed to confirm the predictability of developed model. We start from the material parameters attributed to the nanoparticles.

Fig. 6 shows the effects of CNT concentration  $(\phi_f)$  and modulus  $(E_f)$  on the estimated relative modulus at average values of  $E_{\rm m}=2$  GPa, R=10 nm, t=5 nm and  $E_{\rm i}=100$  GPa. The

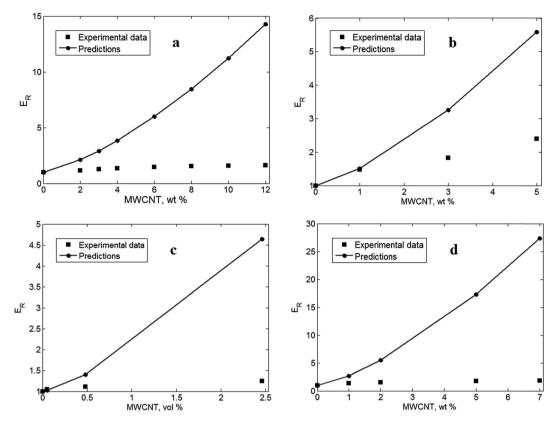


Fig. 5 Overprediction of the developed model for (a) PA6/MWCNT,<sup>40</sup> (b) PVA/MWCNT,<sup>41</sup> (c) polypropylene/MWCNT<sup>42</sup> and (d) PA6/MWCNT<sup>43</sup> samples.

modulus does not increase at very low levels of filler concentration. As observed,  $E_{\rm R}=1$  ( $E=E_{\rm m}$ ) is obtained with  $\phi_{\rm f}<0.004$  which demonstrates the non-reinforcement of the polymer matrix by low numbers of nanoparticles. As a result, very low concentrations of nanoparticles cannot cause reinforcement in PCNTs. However, the modulus improves with the increment of filler concentration, but the highest modulus is obtained with the highest levels of filler concentration and modulus. The highest relative modulus of about 6.5 (a 550% improvement in comparison to the polymer matrix) is gained at the uppermost

values of  $\phi_f = 0.03$  and  $E_f = 1300$  GPa. Therefore, both high ranges of nanofiller concentration and stiffness are essential to improve the modulus of the nanocomposites.

These observations reflect the reinforcing role of the nanoparticles in the nanocomposites. A high filler content, which causes a large number of nanoparticles undoubtedly stiffens the nanocomposite. However, it should be noted that high filler concentrations may result in nanoparticle agglomeration which has a detrimental effect on the modulus. Moreover, a higher filler stiffness further increases the modulus of polymer

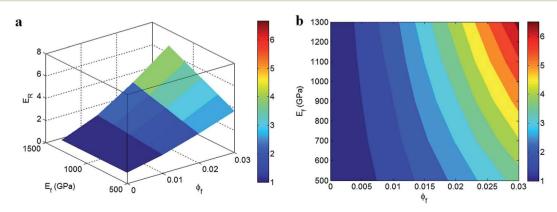


Fig. 6 Variation of the relative modulus at different " $\phi_{\rm f}$ " and " $E_{\rm f}$ " parameters and at  $E_{\rm m}=2$  GPa, R=10 nm, t=5 nm and  $E_{\rm i}=100$  GPa: (a) 3D and (b) contour plots.

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nanocomposites, because the nanocomposite modulus is a function of the moduli of both the polymer matrix and the nanoparticles according to the rule of mixtures. Conclusively, the developed model indicates that the nanocomposites benefit from a high volume fraction of strong nanoparticles, due to the improved properties of the nanoparticles compared to the polymer matrix.

Fig. 7 also shows the dependence of the relative modulus on the "R" and "t" parameters at average values of  $E_{\rm m}=2$  GPa,  $\phi_{\rm f}=$ 0.01,  $E_{\rm f}=1000$  GPa and  $E_{\rm i}=100$  GPa. The worst modulus is observed at high and small values of the "R" and "t" parameters, respectively. In other words, the poorest relative modulus of about 2 is predicted by R > 30 nm and t < 10 nm showing that thick CNTs and a thin interphase decrease the modulus of nanocomposites. In contrast, the highest modulus is obtained by the thinnest CNTs and the thickest interphase, *i.e.*  $E_R = 7$  is achieved by R=10 nm and t=35 nm. Accordingly, thin nanotubes and a thick interphase produce a good modulus in PCNTs, whereas thick nanoparticles and a thin interphase cannot considerably improve the modulus. These results are well described by the reinforcing and percolating roles of the nanoparticles and the interphase in PCNTs. Thin CNTs increase the interfacial contact/interaction with polymer chains, which positively improves the mechanical involvement between the polymer chains and the nanoparticles. At the same filler concentration, it is clear that small nanoparticles can produce a greater interfacial area with the polymer matrix compared to larger particles.46 Since the specific surface area of the nanoparticles (surface area per weight) plays a major role in the reinforcing effects and the interphase level, small nanoparticles mainly control the mechanical performances of nanocomposites, as revealed by the developed model.

On the other hand, thin nanotubes create a high aspect ratio  $(\alpha = l/2R)$  which reduces the percolation threshold and assists the formation of network structures. As a result, thin nanotubes promote the percolating role of nanoparticles.

A thick interphase enhances its role in the mechanical properties of polymer nanocomposites. A thick interphase is representative of the high extent of interfacial interaction/adhesion between the polymer matrix and the nanoparticles.

So, a thicker interphase should further improve the modulus of nanocomposites, due to a better level of stress transferring at the interface.<sup>47</sup> From a modeling view, the Ji<sup>34</sup> and Pukanszky<sup>48</sup> models have shown that a thick interphase produces an improved modulus and strength in nanocomposites. A thick interphase also positively shifts the percolation threshold of nanoparticles to smaller filler concentrations as established by the excluded volume of nanoparticles (eqn (13)). The thick interphase regions around the nanoparticles can generate network structures, which quickens the percolation threshold for mechanical properties. Accordingly, a thick interphase can stimulate the percolating of nanoparticles at small filler fractions causing a positive effect on the modulus besides its reinforcing role. In conclusion, the positive effects of thin CNTs and a thick interphase are well explained by the developed model.

The roles of the interphase volume fraction  $(\phi_i)$  and modulus  $(E_i)$  on the modulus of PCNTs based on the developed model are also plotted in Fig. 8 at  $E_{\rm m}=2$  GPa,  $\phi_{\rm f}=0.01$  and  $E_{\rm f}=1000$  GPa. The highest relative modulus of 12 is obtained at  $\phi_i = 0.1$  and  $E_i = 500$  GPa, while an " $E_R$ " level of 2 is observed at  $\phi_i < 0.02$ . This means that the highest modulus is calculated with the greatest values of the " $\phi_i$ " and " $E_i$ " parameters, while a low " $\phi_i$ " is adequate for the main decrement of the modulus which demonstrates the key effect of " $\phi_i$ " on the modulus. So, we should aim to produce high levels of interphase concentrations in PCNTs. The role of the interphase in nanocomposites becomes more important if a high level of " $\phi_i$ " can be reached. In other words, the reinforcing and percolating productivities of interphase regions in nanocomposites mostly depend on the " $\phi_i$ " parameter. A high level of " $\phi_i$ " enlarges its effects on reinforcement and percolation, while the minor role of a slight interphase can be disregarded from nanocomposites. As a result, the observed influence of " $\phi_i$ " on the modulus is logical. According to eqn (22), more " $\phi_i$ " is obtained with thinner nanotubes and a thicker interphase. Therefore, these levels should be controlled in nanocomposites by preventing the accumulation of nanoparticles and providing strong interfacial adhesion/interaction between the components.

The highest modulus in nanocomposites is achieved with the highest concentration of the strongest interphase based on

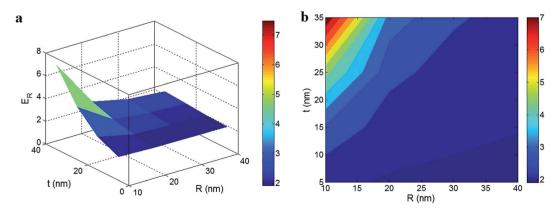


Fig. 7 (a) 3D and (b) contour plots to describe the influence of the "R" and "t" parameters on the calculated relative modulus at average values of  $E_{\rm m}=2$  GPa,  $\phi_{\rm f}=0.01$ ,  $E_{\rm f}=1000$  GPa and  $E_{\rm i}=100$  GPa.

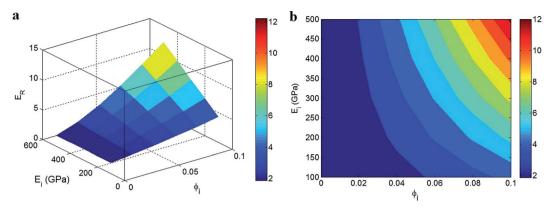


Fig. 8 The relative modulus as a function of the " $\phi_i$ " and " $E_i$ " parameters at  $E_m = 2$  GPa,  $\phi_f = 0.01$  and  $E_f = 1000$  GPa: (a) 3D and (b) contour plots.

Fig. 8. Therefore, the interphase modulus also plays an important role in the reinforcing of the interphase. A greater volume fraction of the strong interphase undoubtedly creates stronger regions (compared to the polymer matrix) in nanocomposites, which promotes the tensile modulus. Moreover, a strong interphase can resist high stress loading which is transferred through the interphase. As a result, the calculations of the developed model regarding the significance of the interphase content and modulus are sensible. These remarks implicitly indicate that thin nanotubes, and a thick and strong interphase result in the maximum level of modulus. This evidence has also been reported in previous studies 19,30 which confirms the correct development of the Kolarik model for the modulus of PCNTs.

Finally, it should be stated that the effects of the " $\phi_i$ " and " $E_i$ " parameters on the modulus are more pronounced that those of " $\phi_f$ " and " $E_f$ ", although the nanoparticles' modulus is much higher than that of the interphase. According to Fig. 6 and 8, the concentration and modulus of the nanoparticles improve the modulus from 1 to about 6.5, while the interphase properties can improve the modulus by 1100% ( $E_R = 12$ ). As a result, the interphase concentration and modulus are very important factors in the stiffness of nanocomposites.

### 4 Conclusions

The Kolarik model based on the COS structure for the tensile modulus of co-continuous blends was developed for PCNTs by the reinforcing and percolating roles of nanoparticles and interphases. The Ouali model for the modulus of nanocomposites above the percolation threshold was also applied to express the "f" parameter. In addition, the interphase region was assumed to be a separate phase in addition to the matrix and the nanoparticles in the Kolarik model. The experimental results from some samples containing interphases and filler networks suggest an acceptable agreement with the model predictions. However, the modulus is overpredicted in the samples which do not include interphases and network structures, because the absence of these terms significantly worsens the stiffness of nanocomposites.

The modulus does not improve at very low levels of filler concentration, but the highest relative modulus of about 6.5 is obtained with the highest values of  $\phi_f = 0.03$  and  $E_f = 1300$  GPa, due to the reinforcing role of the nanoparticles. The worst relative modulus of about 2 is also observed at values of R >30 nm and t < 10 nm, where  $E_R = 7$  is achieved by R = 10 nm and t = 35 nm demonstrating the positive effects of thin CNTs and a thick interphase on the modulus. The effects of these parameters were well explained based on the reinforcing and percolating roles of the nanoparticles and the interphase region. Moreover, the highest relative modulus of 12 is obtained with the highest values of  $\phi_i = 0.1$  and  $E_i = 500$  GPa, while  $E_R =$ 2 is observed at  $\phi_i$  < 0.02 which means that the maximum modulus is calculated with the greatest values of the interphase parameters. According to these calculations, the developed model shows a greater significance of the interphase properties for the stiffness of nanocomposites compared to the nanoparticles' modulus and concentration, but the size of nanoparticles is more effective for the interfacial area and percolation threshold.

### Conflicts of interest

There are no conflicts to declare.

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