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Refining discordant gene trees

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Abstract

Background: Evolutionary studies are complicated by discordance between gene trees and the species tree in which they evolved. Dealing with discordant trees often relies on comparison costs between gene and species trees, including the well-established Robinson-Foulds, gene duplication, and deep coalescence costs. While these costs have provided credible results for binary rooted gene trees, corresponding cost definitions for non-binary unrooted gene trees, which are frequently occurring in practice, are challenged by biological realism.

Result: We propose a natural extension of the well-established costs for comparing unrooted and non-binary gene trees with rooted binary species trees using a binary refinement model. For the duplication cost we describe an efficient algorithm that is based on a linear time reduction and also computes an optimal rooted binary refinement of the given gene tree. Finally, we show that similar reductions lead to solutions for computing the deep coalescence and the Robinson-Foulds costs.

Conclusion: Our binary refinement of Robinson-Foulds, gene duplication, and deep coalescence costs for unrooted and non-binary gene trees together with the linear time reductions provided here for computing these costs significantly extends the range of trees that can be incorporated into approaches dealing with discordance.

Introduction

Gene trees represent estimates of evolutionary histories of gene families, and are fundamental for evolutionary biological research [1,2]. Often gene trees are assumed to reflect the evolutionary history of species, or *species tree*, from which their sequences were sampled, presenting a common approach of species tree inference [3-7]. Gene trees can also provide fundamental information to study the evolution of biochemical function in gene families [8].

Gene trees can be inferred from multiple sequence alignments of sequences culled from a gene family. The number of these sequences as well as their evolutionary complexity has expanded on an unprecedented scale in recent years [9], prompting the estimation of ever larger and more credible gene trees. Despite these potentials, evolutionary biologists have long recognized the potential for substantial discordance among the gene trees as

well as among the gene trees and the species tree in which they evolve [10-14], challenging traditional phylogenetic gene tree and species tree estimation. Discordance can be caused by error as well as major evolutionary processes, such as the duplication of genes or deep coalescence. Complicating matters further such error and evolutionary processes can occur on a staggering scale [15,16]. For example simulations with realistic parameters suggested that analyzes individual avian genes frequently resulted in trees with substantial error [17], and evolutionary processes cause discordance among evolutionary relationships of major avian groups [18]. Consequently, phylogenetic approaches are challenged to deal with error as well as complex histories of evolutionary processes in order to explain discordance in gene trees [19-21].

A common approach to deal with discordance in gene trees is by representing them with an estimate of the species tree that is thought to be the median tree of the gene trees under a particular (*topological comparison*) cost from a gene tree to a species tree, which is often referred to as a *supertree* [22]. A *median tree S* for a given cost and a collection of trees minimizes the sum of the pairwise costs

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from every gene tree to S . While various costs have been proposed [23-26], here we are concerned with the well-researched Robinson-Foulds, duplication, and deep coalescence costs. The Robinson-Foulds cost is measuring quantitative dissimilarities between two trees without relying on an evolutionary model, and is therefore well suited to address discordance caused by error [27,28]. In difference, the costs for the evolutionary events gene duplication and deep coalescence are both based on an evolutionary parsimony model allowing to resolve discord based on such events [29,30].

However, the presented costs are not well adapted to biological realism [31,32]. In practice gene trees are frequently inferred from sequences that do not permit reliable estimations of rootings or bifurcations [33], and therefore are unrooted and non-binary. The original evolutionary costs for gene duplication and deep coalescence can not be applied to such trees, since they are only defined for rooted and binary gene trees. In contrast the Robinson-Foulds distance is formally defined for unrooted and non-binary trees, but multifurcations in phylogenetic trees are interpreted as true evolutionary multifurcations (*hard multifurcations*). However, non-binary relationships in gene trees represent uncertainties about the correct binary relationships (*soft multifurcations*), rather than hard multifurcations which are rare [34]. Consequently, all of the the presented costs are not applicable to a large number of gene trees in practice.

More recently, a binary refinement model for the duplication cost [35] and the deep coalescence cost [36,37] for rooted gene trees that are non-binary were introduced. Here we propose a natural extension of this model for our costs to compare unrooted and non-binary gene trees with rooted binary species trees, and describe linear time reductions to compute these costs.

Related work

Here we provide definitions as well as computational and applicability results, first for the Robinson-Foulds cost, and then for the duplication and deep coalescence costs.

The Robinson-Foulds cost is an elementary tool for estimating quantitative dissimilarities between phylogenetic trees [38-40]. This cost is defined for two trees to be the cardinality of the symmetric difference of their split presentations for unrooted trees, and of their cluster presentations for rooted trees. The *split-presentation* of an unrooted tree is the set of all bipartitions, called *splits*, of the trees' taxon set induced by the removal of an edge [39,41]. Analogously, the *cluster presentation* of a rooted tree is the set of all taxon sets of its full subtrees [39]. The Robinson-Foulds cost for two trees, both either unrooted or rooted, satisfies the metric properties [38], and can be

computed in linear time [42]. A randomized approximation scheme computes, in sublinear time and with high probability, a $(1 + \epsilon)$ approximation of the Robinson-Foulds cost [43]. More recently, the Robinson-Foulds cost between an unrooted tree and a rooted tree was introduced in [44] to be the minimum cost under all pairs consisting of a rooting of the unrooted tree and the rooted tree. In fact, this cost is still computable in linear time [44]. Moreover, the distribution of the Robinson-Foulds distance relative to a fixed tree can be computed in linear time [45]. Note, the skewed distribution of the Robinson-Foulds metric suggests that it is only of use when the trees to be compared are quite similar [46]. While the Robinson-Foulds cost is wide-spread for the comparative analysis of phylogenetic trees, it does not rely on a biological model explaining the difference between trees. Therefore, the Robinson-Foulds cost is generally applicable to any type of trees, e.g. linguistic trees [47] and trees representing dominance hierarchies [48].

In contrast, the duplication and the deep coalescence costs rely on a biological model explaining the discordance between a gene tree and a species tree based on evolutionary events. For a gene and a species tree, both rooted and binary, the *duplication cost* and the *deep coalescence cost* are defined to be the minimum number of gene duplications and coalescences, respectively, required to reconcile the gene tree with the species tree [49,50]. While these costs are not symmetric, they are computable in linear time [51,52], and allow to infer credible species trees [53-57]. Furthermore, gene trees that are reconciled by the minimum number of evolutionary events allow studying complex histories of evolutionary events [54,58]. The gene duplication and deep coalescence costs can also be defined for binary unrooted gene trees and binary rooted species trees as the minimum cost under all rootings of the gene tree and computed in linear time [32,59,60]. However, often gene trees are unrooted and non-binary in practice. While existing definitions for such gene trees and rooted binary species trees are linear time computable [31,32], they are not well adapted to biological realism. More recently, cost definitions for such trees were introduced that are based on a binary refinement model, by choosing the minimum cost between every binary refinement of a rooted gene tree and a rooted binary species tree, which are polynomial time computable [35,61]. In contrast, finding the minimum cost between a rooted binary gene tree and all binary refinements of a rooted non-binary species tree is NP hard [37]. However, costs under a binary refinement model for unrooted and non-binary gene trees have not been addressed in the literature. For a detailed overview about gene tree reconciliation the interested reader is referred to [62].

Contributions

Here, we define the Robinson-Foulds, duplication, and deep coalescence costs for unrooted and non-binary gene trees and a rooted binary species tree under the binary refinement model. To compute the duplication cost we describe a linear time reduction from the problem of computing optimal binary refinements of unrooted gene trees to the problem of computing such refinements for rooted gene trees. The latter problem can be solved in linear time [37]. Then, based on the theory of unrooted tree reconciliation [32,44,63,59], we prove that the duplication cost has similar properties to the deep coalescence and Robinson-Foulds costs when comparing unrooted and non-binary gene trees with rooted species trees. From this follows that we can prove linear time reductions for the deep coalescence and the Robinson-Foulds costs that are similar to our reduction for the duplication cost. Since our reductions require only linear time, the runtime to compute the optimal binary refinements of unrooted gene trees is bound by the time complexity of computing optimal binary refinement for rooted binary gene trees.

Basic definitions and preliminaries

An *unrooted tree* T is an acyclic, connected, and undirected graph that has no degree-two nodes, and every degree-one node is labeled with a species name. The degree-one nodes are called *leaves*; and the remaining nodes are called *internal* nodes. A tree is binary if every internal node has degree three. A *rooted tree* is defined similar to an unrooted tree, with the difference that it has a distinguished node, called *root*. A *contraction* of an edge e of an (un)rooted tree T removes e from T and merges both ends of e into a single node. A *binary refinement* of an unrooted or rooted tree T is a binary tree that can be transformed into T by contractions. By $L(T)$ we denote the set of all leaf labels in T .

A rooted tree S with a unique leaf labeling is called a *species tree*. For two nodes a, b of S , $a \oplus b$ is the least common ancestor of a and b in S . Let T and S be a rooted tree (called rooted gene tree) such that $L(T) \subseteq L(S)$. By $M : T \rightarrow S$ we denote the *least common ancestor (lca) mapping* between the nodes of T and S that preserves the labeling of the leaves. The *duplication cost* between T and S , is defined by: $D(T, S) := |\{M(g) = M(c) : c \text{ is a child of an internal node } g \in T\}|$.

Let $G = \langle V_G, E_G \rangle$ be an unrooted tree (called unrooted gene tree). A *rooting* of G is defined by choosing an edge e from G on which the root is to be placed. Such a rooted tree will be denoted by G_e . Note that G_e has one more node (the root) than G . A *rooted binary refinement* of an unrooted gene tree G , is a binary refinement of a rooting of G .

The unrooted *duplication (urD)* cost between an unrooted gene tree G and a species tree S is defined as

$$urD(G, S) := \min\{D(G!, S) : G! \text{ is a rooting of } G\}.$$

The edges with minimal cost will be called optimal. In the remainder of this work we show first how to compute urD in linear time and space, and then solve the following problem. Observe, that in contrast to our previous study [44,32,64], here, for the first time, we extend the notion of rooting by incorporating rooting at nodes.

Problem 1 *For a given unrooted gene tree G and a binary species tree S , find the binary refinement of under all rootings of G that minimizes the duplication cost.*

A similar problem for rooted gene trees was solved in [35]. In the remaining section we show how to reduce Problem 1 to the rooted problem in linear time.

Unrooted reconciliation

First we provide definitions introducing the basics of unrooted reconciliation. This approach is partially based on our previous papers [32,44,63,59]. However, for the first time, we prove properties of urD for trees with multi-furcations. We assume that G is an unrooted gene tree and S is a species tree. We transform G into a directed graph \widehat{G} , by replacing each edge $\langle v, w \rangle$ by a pair of directed edges $\langle v, w \rangle$ and $\langle w, v \rangle$. We label the edges of \widehat{G} by the nodes of S as follows. If $v \in G$ is a leaf labeled by a , then the edge $\langle v, w \rangle$ in \widehat{G} is labeled by the node in S whose label is a . Let $v \in G$ have exactly k siblings w_1, w_2, \dots, w_k . If a_i and b_i are the labels of $\langle v, w_i \rangle$ and $\langle w_i, v \rangle$, respectively, then $a_i = \bigoplus_{j=1, j \neq i}^{j=k} b_j$. Let τ be the root of S . Each internal node $v \in G$ defines a *star* with the center v as indicated in Figure 1a. We refer to the undirected edge $\{v, w_i\}$ as e_{w_i} for all $i = 1, 2, \dots, k$.

There is a limited number of star types in gene trees [44]. Let K be a star with center v and k siblings as indicated in Figure 1a. Let α denote the number of edges satisfying $a_i = \tau$. Similarly, we define β for b_i 's. Then, K has type: **M1** if $\alpha = 1$ and $\beta = k - 1$ and all edges labeled by τ are connected to the k siblings of v , **M2** if $\alpha = 0$ and $\beta = k - 1$, **M3** if $\alpha = 1$ and $\beta = k$, **M4** if $\alpha = \beta = k$, **M5** if $1 < \alpha < \beta = k$ and **M6** if $\alpha = 0$ and $\beta = k$.

Proposition 1 *For a given unrooted gene tree G and a species tree S a gene tree G can have any number of stars M1. For the remaining stars we have three mutually exclusive cases: (i) G has an empty edge, (ii) G has a double edge or (iii) G has only single edges.*

Proof The proof follows easily from the properties of stars. See also Lemma 2 from [44]. \square

Observe that in case (i) G has one or two stars M2, in case (ii) G has a star of type M3-M5 and in (iii) G has exactly one star of type M6.

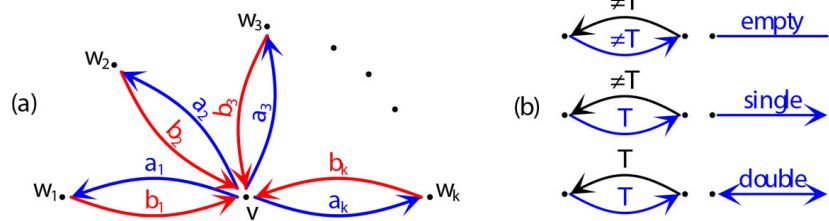


Figure 1 Star transformation. (a) A star with the center v in \widehat{G} and $k \geq 3$ edges. Here $e_i = \{v, w_i\}$ for $i = 1, 2, \dots, k$. (b) A simplified representation of edges (empty, single and double) that will be used through the rest of this work. The notation $\neq T$ denotes that the label is a non-root node from S .

The next propositions states a crucial difference between binary and general trees. For the proof please refer to [44].

Proposition 2 *If both an unrooted gene tree G and a species S are binary then G has at least one empty or double edge.*

Results

Polytomies and the duplication cost

The next two proposition shows how the cost changes when we move a position of the root in G .

Proposition 3 *Under the notation from Figure 1. If for some $i \in \{1, 2, \dots, k\}$ one of the following conditions are true:*

- *If the star type is M1 or M3 and $b_i = \tau$.*
- *If the star type is M2 and $a_i \neq \tau \neq b_i$.*

then $D(G_{e_i}, S) \leq D(G_{e_j}, S)$ for every $j = 1, 2, \dots, k$.

Proof All rootings of G share the same subtrees attached to w_1, w_2, \dots, w_k . Therefore, all costs share the same component c coming from the partial duplication cost for these subtrees. The remainder follows in from the definition of the duplication cost and Figure 1 and Figure 2. For $l \in \{1, 2, \dots, k\}$ let M_l be the lca-mapping from G_{e_l} to S . In the case of stars M1 or M3 we have $M_j(v) = M_j(w_i) = \tau$. Therefore, both nodes, w and the root of G_{e_i} , are duplication nodes; that is, $D(G_{e_i}, S) = c + 2$. However, in G_{e_j} , v can be a non-duplication node, thus $c + 1 \leq D(G_{e_i}, S) \leq D(G_{e_j}, S) = c + 2$.

In the case of M2, we have $M_l(w_i) \neq \tau \neq M_l(v)$ and $M_i(w_i) \oplus M_i(v) = \tau$, thus the root of G_i is a non-duplication node. On the other hand, $M_j(v) = \tau$ and the root of G_j is a duplication node. We conclude $c \leq D(G_{e_i}, S) \leq c + 1 \leq D(G_{e_j}, S)$. \square

Proposition 4 *Using the notation from Proposition 3. If the star type is M4 – M6 then $D(G_{e_i}, S) = D(G_{e_j}, S)$ for all i and j .*

Proof Similarly to the proof of the previous proposition, it is easy to show that the root of G_{e_i} is a duplication node while v is a duplication node, if and only if, the star is of type M4 or M5. Therefore, for every i ,

$D(G_{e_i}, S) = c + 2$ if the star type is M6 and $D(G_{e_i}, S) = c + 2$. Otherwise, where c is defined in the proof of Proposition 3. \square

We conclude from Propositions 1-4:

Theorem 1 *For an unrooted gene tree G and a species tree S . If e is an edge of G that is either empty, double or an element of a star M6, then e is optimal.*

This observation leads to a linear time and space reduction for *urD* computation similar to algorithms from [32,44]. Now we reduce Problem 1, to the problem where gene trees are rooted. In the special case of star M6, we need to root a tree at a node instead of edge. For a non-leaf node $v \in VG$ by G_v we denote the tree rooted at v . We refer to the algorithm for refining rooted gene trees from [65] by $Bin(T, S)$, where T is a rooted tree and S is a binary species tree. It is known that $Bin(T, S)$ runs in $O(|T| |S|)$ time [65].

Theorem 2 *Algorithm 1 infers a rooted binary refinement G^* of an unrooted gene tree G such that $D(G^*, S) = \min \{urD(G', S) : G' \text{ is a binary refinement of } G\}$.*

Proof The correctness of Algorithm 1 follows from the property that the refinement operation will not change the labels of an existing edge in \widehat{G} and properties of stars for binary trees [63]. We analyze the cases from Proposition 1. (i) If G has a double edge e , then in every (unrooted) binary refinement of G e is a double edge. Thus, by Proposition 1 e is optimal in every binary refinement of G . We conclude that rooting G at e and removing polytomies from G_e by applying the solution for rooted trees will infer an optimal rooted refinement of G . (ii) The same result applies when G has an empty edge. (iii) When G has only single edges, then the elements of the unique star M6 in G are optimal edges in G . Similarly, to previous cases these single edges will be present in any (unrooted) binary refinement of G (see Figures 3, 4, 5 for example). However, by Proposition 2 and Proposition 1 they are not necessarily optimal in such refinements. To address this problem, observe that any binary unrooted refinement of G will have either empty or double edges “surrounded” by the edges previously present in the star of type M6. Thus, we can

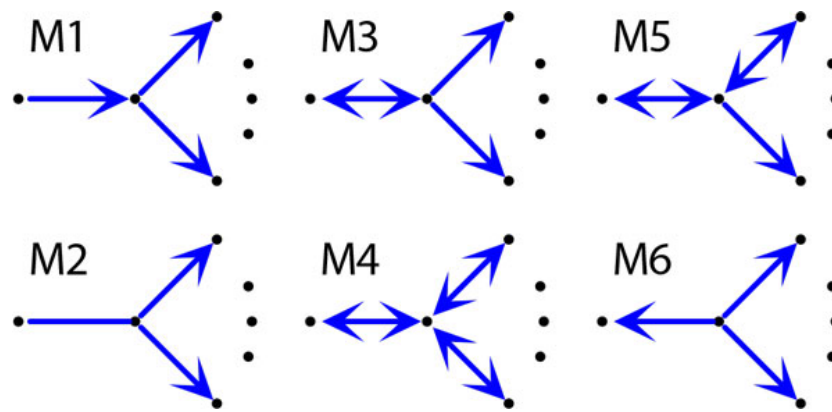


Figure 2 Stars. Star topologies that can be present in gene trees. On the right side of stars there are at least 2 edges. M5 has at least two double edges and at least one single edge.

simply root G at the center of the star M6 and then proceed with the refinement procedure for rooted trees. Clearly, the refinement procedure, will infer a rooted gene tree T such that its unrooted variant is a binary refinement of G with the minimal duplication cost. An example of a gene tree with star M6 with all binary refinements is depicted in Figure 5.

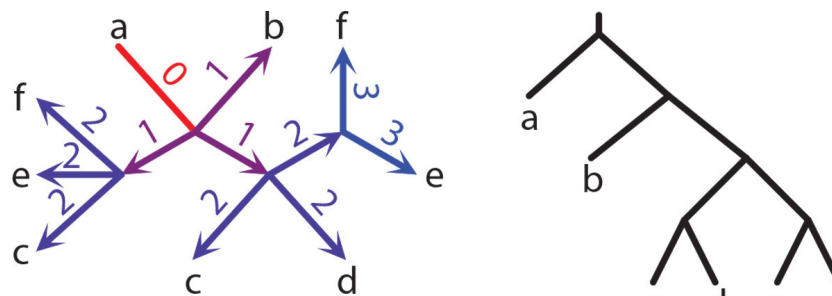
In summary, it is sufficient to identify an optimal edge in G , and then proceed accordingly with the refinement procedure. In steps 3-5 the algorithm is evaluating labels of edges from \widehat{G} . The optimal edge is found in the loop present in steps 6-7. Finally, the refinement procedure is called in steps 9-10 depending on the type of the star. □

Theorem 3 *Algorithm 1 requires $O(|G||S|)$ time, while the reduction (steps 1-7) can be completed in $O(|G| + |S|)$ time and space.*

Proof As desired, the result follows from [44] and [37].

Algorithm 1 Resolving polytomies in unrooted gene trees

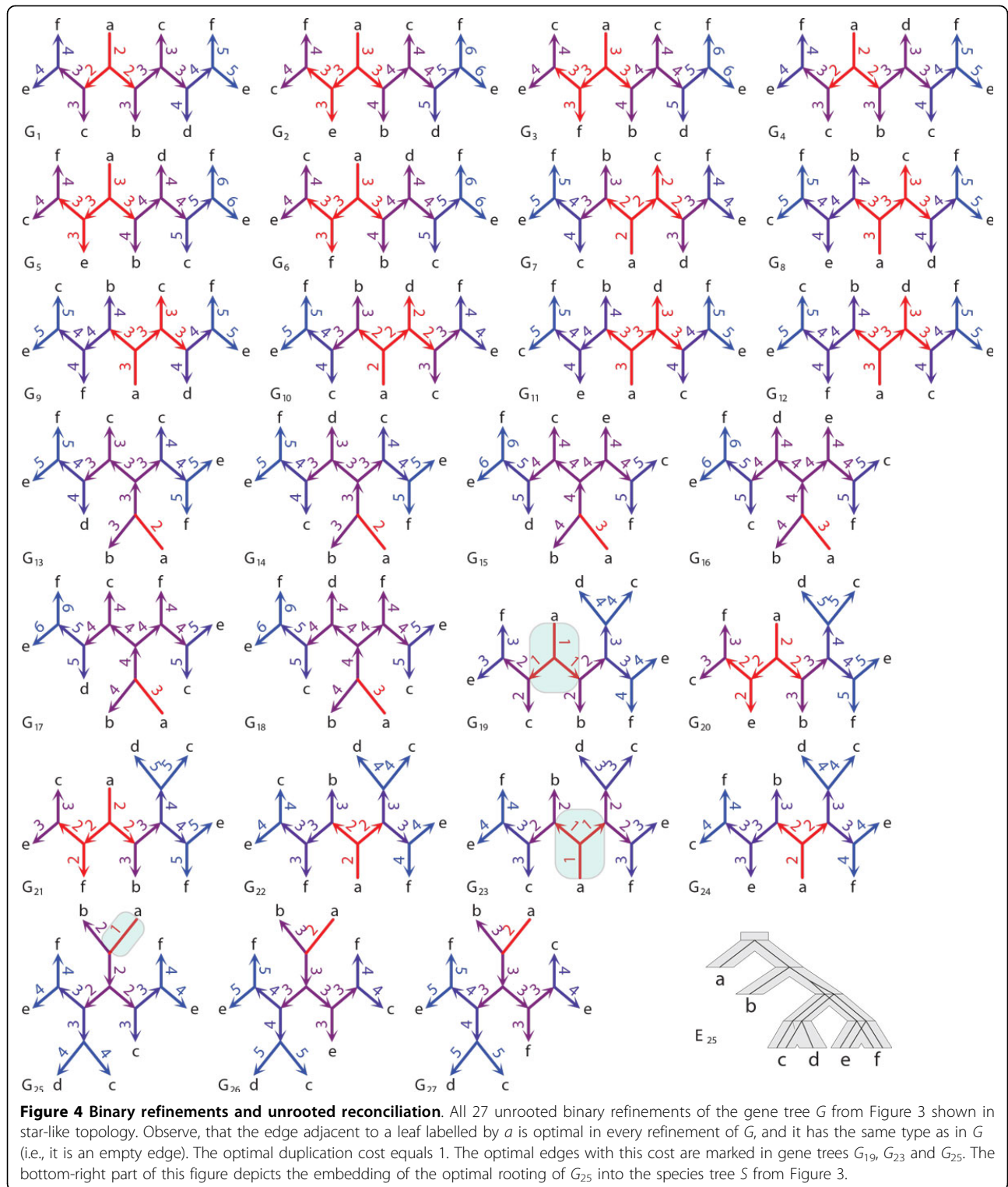
- 1: **Input** A binary species tree S , an unrooted gene tree G with at least three leaves $L(G) \subseteq L(S)$.
- 2: **Output** The rooted binary refinement of G with the minimal duplication cost.
- 3: **Let** $m_{x,y}$ be the label (a node from S) of $\langle x, y \rangle$ in \widehat{G} .
 // can be computed in $O(|G|)$ steps [44].
- 4: **Let** v be a node from VG .
- 5: **Let** $\tau := m_{v,w} \oplus m_{w,v}$ for some edge $\langle v, w \rangle$ in G .
- 6: **While** there exists a node w adjacent with v such that $m_{w,v} = \tau \neq I = m_{v,w}$
- 7: **do**: set $v := w$ (star M1).
- 8: **f** v is incident with a empty/double edge $\langle v, w \rangle$, that is, $m_{v,w} = \tau = m_{w,v}$ or $m_{v,w} \neq \tau \neq m_{w,v}$
- 9: **then return** $\text{Bin}(G_{\langle v,w \rangle}, S)$ (optimal edge found in star M2-M5)
- 10: **else return** $\text{Bin}(G_v, S)$ (v is the center of star M6).



Unrooted gene tree G with 3 multifurcations

Species tree S

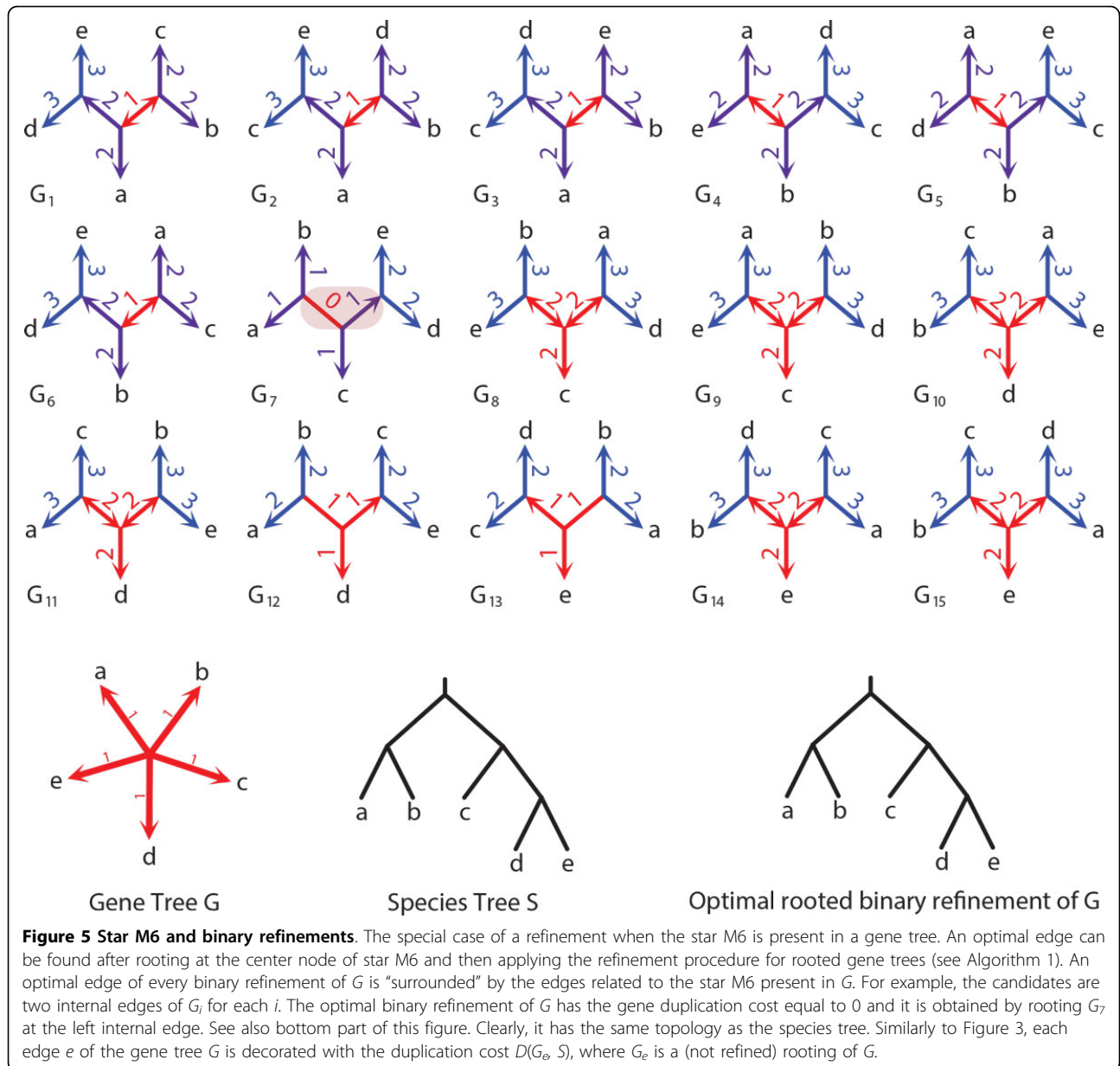
Figure 3 Gene tree and species trees. An example of an unrooted gene tree G with three multifurcations and a species tree S . The gene tree G is depicted with a star topology, and it has one star of type M2 and three stars of type M1. Every edge e of G is decorated with the duplication cost $D(G_e, S)$ (note that the rooting G_e is not refined). Observe, that the optimal edge (empty edge) is adjacent to a leaf labelled by a . Rooting at this edge yields the duplication cost 0.



Examples of (unrooted) binary refinements with costs of all rootings of an unrooted gene tree with multifurcations are depicted in Figures 3, 4 and 5.

Polytomies and other cost functions

Similarly to the gene duplication cost we show results for other cost functions that are related to the duplication cost [63]. Here, we introduce for the first time a



general approach, similar to [32,44], for the case where both trees, i.e., a gene tree and a species tree can be non-binary.

Costs can be defined for rooted trees as follows:

$$\rho_K(T, S) = \sum_{g \in I(T)} \xi_K(g),$$

where T is a rooted gene tree and S is a species tree such that $L(T) \subseteq L(S)$, $I(T)$ is the set of all internal nodes of T , K is a cost name and $\xi_K : I(T) \rightarrow R$ is a contribution function that for an internal node ν of T defines a contribution of ν to the cost K when comparing T and S . For a node ν in a rooted tree, by $c(\nu)$ we

denote the cluster of ν defined as the set of all leaf labels visible from ν . The contribution functions for standard costs are defined as follows. Let g be an internal node of T and M be the lca-mapping from T to S .

- Gene duplication (D) cost function: $\xi_D(g) = 1$ if g has a child c such that $M(g) = M(c)$, and $\xi_D(g) = 0$ otherwise.
- Deep coalescence (DC): $\xi_{DC}(g) = \sum_{g' \text{ is a child of } g} ||LM(g), M(g')||$, where $||x, y||$ is the number of edges on the shortest path connecting nodes x and y in S .
- Robinson-Foulds cost (RF): $\xi_{RF}(g) = 1$ if $c(g) \neq c(M(g))$ and $\xi_{RF}(g) = 0$ otherwise.

Note that the classical Robinson-Foulds distance can be obtained by $RF(T, S) = |I(S)| + 2 * \rho RF(T, S) - |I(T)|$. Additionally, we have to assume that for the RF distance T is bijectively labelled by the labels present in $L(S)$. For more details and discussion please refer to [44,63].

For an unrooted gene tree G , a species tree S , the unrooted cost is defined by:

$$\Delta(G, S, f) = \min_{e \in E_G} f(e),$$

where $f: E_G \rightarrow R$ is a cost function usually defined for a cost K by $f(e) = \rho_K(G_\emptyset, S)$. Assume that $f_S(e) = D(G_\emptyset, S)$, then it can be proved that $ur D(G, S) = \Delta(G, S, f_S)$.

In the previous section we described the solution to Problem 1 defined for the duplication cost by reducing the unrooted problem to a rooted one in linear time and space. Here, we show that the same kind reduction can be applied for the DC and RF cost functions.

Problem 2 (Unrooted refinement under DC cost) *For a given unrooted gene tree G and a binary species tree S , find a binary refinement under all rootings of G that minimizes the DC cost.*

Problem 3 (Unrooted refinement under RF cost) *For a given unrooted gene tree G and a binary species tree S , find a binary refinement under all rootings of G that minimizes the RF cost.*

The result for the DC and the RF cost follows from [32] (Proposition 1 and Proposition 2) and [44] (Proposition 1 and Proposition 2), respectively. We conclude, that the statement from Theorem 1 also holds for the DC and RF cost functions. Therefore, Algorithm 1 can be used for locating an optimal edge or star M6 in an unrooted gene tree with multifurcations. Then after such a rooting is identified, one can apply the solution that removes polytomies from rooted gene trees. Clearly this reduction can be performed in linear time and space for both cost functions.

Problem 4 (Rooted refinement under DC cost) *For a given rooted gene tree G and a binary species tree S , find a binary refinement under all rootings of G that minimizes the DC cost.*

Problem 5 (Rooted refinement under RF cost) *For a given rooted gene tree G and a binary species tree S , find a binary refinement under all rootings of G that minimizes the RF cost.*

According to our knowledge Problem 4 and Problem 5 are open, with the exception that Problem 4 can be solved in quadratic time for the case when the gene tree has a bijective leaf labelling [36]. We conjecture that these two problems can be solved in polynomial time similarly to the problem under the duplication cost [35] (see $Bin(G_e, S)$ in Algorithm 1). Our reduction shows that Problem 2 and Problem 3 have the same time complexity as the rooted ones.

Conclusion

To deal with discordance in practice we introduced a binary refinement model for the well-studied Robinson-Foulds, duplication, and deep coalescence costs. To compute these costs we described novel linear time reductions, from which quadratic time algorithms follow for the duplication cost and for the deep coalescence cost when constrained to bijective labelings. Our binary refinement model together with the efficient algorithms allows the exploitation of the full range of available gene trees. Finally, our algorithms not only compute optimal binary refinement costs efficiently, but also simultaneously root and refine gene trees optimally. However, the time complexity of the Robinson-Foulds cost for unrooted and non-binary gene trees will depend on the time complexity of computing this cost for rooted non-binary gene trees, which is unknown to the best knowledge of the authors.

Competing interests

The authors declare that they have no competing interests.

Authors' contributions

PG and OE contributed equally to the writing of the paper. Both authors read and approved the final manuscript.

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Declarations

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