



# Article Features Importance Analysis of Diesel Vehicles' NO<sub>x</sub> and CO<sub>2</sub> Emission Predictions in Real Road Driving Based on Gradient Boosting Regression Model

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Abstract: In order to have an accurate and fast prediction of the artificial intelligence (AI) model, the choice of input features is at least as important as the choice of model. The effect of input features selection on the emission models of light diesel vehicles driven on real roads was investigated in this paper. The gradient boosting regression (GBR) model was used to train and to predict the emissions of nitrogen oxide (NOx), carbon dioxide (CO2), and the fuel consumption of real driving diesel vehicles in urban scenarios, the suburbs, and on highways. A portable emissions measurement system (PEMS) system was used to collect data of vehicles as well as environmental conditions. The vehicle was run on two routes. The model was trained with the first route data and was used to predict the emissions of the second route. There were ten features related to the NO<sub>x</sub> model and nine features associated with the CO<sub>2</sub> model. The importance of each feature was sorted, and a different number of features were used as input to train the models. The best  $NO_x$  model had the coefficient of determination ( $\mathbb{R}^2$ ) values of 0.99, 0.99, and 0.99 in each driving pattern (urban, suburbs, and highways). Predictions of the second route had the  $R^2$  values of 0.88, 0.89, and 0.96 respectively. The best CO<sub>2</sub> model had the R<sup>2</sup> values of 0.98, 0.99, and 0.99 in each driving pattern, respectively. Predictions of the second route had the  $R^2$  values are 0.79, 0.82, and 0.83, respectively. The most important features for the NO<sub>x</sub> model are mass air flow rate (g/s), exhaust flow rate ( $m^3/min$ ), and  $CO_2$  (ppm), while the important features for the  $CO_2$  model are exhaust flow rate (m<sup>3</sup>/min) and mass air flow rate (g/s). It is noted that the regression models based on the top three features may give predictions very close to the measured data.

**Keywords:**  $NO_x$  and  $CO_2$  emission; diesel vehicle; gradient boosting regression; features importance; PEMS

## 1. Introduction

The problem of air pollution in many metropolises has been gaining more and more attention recently. According to the report of the World Health Organization (WHO), about 7 million people died of diseases related to air pollution in 2018 [1]. Among the pollutants, nitrogen oxides (NO<sub>x</sub>) are severely concerning because they not only have a harmful effect on the human body but are also closely related to ozone (O<sub>3</sub>) formation in the troposphere and on the ground. Kuo et al. proposed research on the effects of ambient air pollutants on childhood asthma hospitalization. They found that the O<sub>3</sub> was positively associated with this childhood disease [2]. Zhong et al. studied the effects of air pollutants on human health. The results also indicated that the O<sub>3</sub> had the highest health impact, followed by particulate matter (PM<sub>10</sub> and PM<sub>2.5</sub>) [3]. In 2021, Wang et al. proposed an investigation on air pollution during pregnancy and childhood autism spectrum disorder (ASD). The results indicated that the O<sub>3</sub> had significant positive associations with childhood ASD and might have different effects before and after birth [4].



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**Copyright:** © 2021 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (https:// creativecommons.org/licenses/by/ 4.0/). There are many anthropogenic sources of  $NO_x$ . The combustion of diesel engines is one of the primary sources of  $NO_x$  in many areas [5]. The abatement of  $NO_x$  in the transportation sector has become an important issue.

In order to reduce the emission of nitrogen oxides effectively, both the automobile manufacturer and governments are betting on considerable research and development expenses, and the regulations of vehicle emissions are becoming more stringent. For example, the EURO 6 emission standard implemented by the European Union in 2014 is a milestone for the regulation of diesel vehicles [6]. It indicates that the government and industry must face the air pollution problem seriously.

It is required that all new vehicles should comply with the current emission standard. As the regulatory standards are becoming stricter and stricter, new vehicles will become cleaner and cleaner. Taking EURO 6 as an example, the emission standard of  $NO_x$  is only 0.08 g/km. However, studies of the emissions measured by the portable emission measurement system (PEMS) show that the actual emissions in real road driving are much higher than the emission standards [7]. The year 2000 model diesel vehicles met the regulation standards of  $0.5 \text{ g/km NO}_x$  in the laboratory test. However, the study found that the actual emissions of diesel vehicles on real roads reached 1.0 g/km. For the year 2014 model diesel vehicles, the legal limit was reduced to 0.08 g/km in the laboratory test, about 1/6 of the standard in 2000. However, the actual road emission in NO<sub>x</sub> was about 0.6 g/km. The regulation was tightened by 85% in 14 years, but the real road emissions did not decrease as much as expected. They were reduced by only 40%. Research conducted by Vicente et al. collected the real road emission data of a total of 541 EURO 5 and EURO 6 vehicles in Britain, Germany, France, and the Netherlands. The results of this investigation showed that only 10% of the EURO 6 vehicles might meet the EURO 6 standard, and 13% of vehicles exceeded by ten times the EURO 6 standards [8].

Therefore, the emissions of diesel vehicles in real road driving becomes an important issue, and the PEMS measurement becomes a valuable method for emission regulation. The impact of the vehicle emission control policy can be effectively evaluated by this method since the driving pattern on a real road is quite different from that in the laboratory. The US EPA also recommends PEMS as an accepted alternative to the laboratory-based chassis dynamometer measurement methods [9]. However, the real road measurement is time-consuming and the cost is very high, so it is helpful to develop a new method to predict the emissions of diesel vehicles on real roads to reduce the measurement cost [10]. Thus, using artificial intelligence techniques is a prospective method to cope with these problems.

Using PEMS measurements for emission evaluation has gained much attention recently, and many investigations have been conducted. Frey et al. proposed protocols of data collection, screening, processing, and analysis to assure data quality and to provide insights regarding the quantification of hot-stabilized emissions [11]. Frey et al. used PEMS to investigate the impact of routes, time of day, and road grade on the emissions of selected light duty gasoline vehicles [12].

McCaffery et al. conducted a study using PEMS to measure 50 heavy-duty vehicles and analyzed these data in the Emission Factor (EMFAC) model [13]. The investigation found that the temperature of selective catalytic reduction (SCR) influenced  $NO_x$  emissions strongly, and exhaust temperature showed the opposite trend.

The main objective of this paper is to find a feasible way to build a predictive model for diesel emissions. The emissions in a running vehicle are affected by many factors, including the engine operating conditions, the vehicle characteristics, and the environmental conditions. It will be a huge computational burden if all parameters are taken into account. Sorting of the relative importance for all the parameters is conducted in this research. It was found that three parameters are good enough to build a model. A lot of computational costs could be saved with this simplified model. However, the ranking order of the input features is not the same for different routes. The results of this paper would be very useful for the modelers, thereafter.

A structure diagram, Figure 1, of this article is presented to make it easier to read this paper.

1 Introduction	<ul> <li>Air pollution effect on human health</li> <li>NO<sub>x</sub> emission in transportation</li> <li>EURO 6 emission standard</li> <li>Emissions measured by PEMS</li> </ul>	<b>4</b> Results	• Features importance analysis • Model performance
2 Literature review of Al research	<ul> <li>Linear regression, Multilayer perceptron</li> <li>Support vector machine, Support vector regression</li> <li>Random forest, Artificial neuron network</li> <li>Nonlinear autoregressive exogenous</li> <li>Gradient boosting regression</li> </ul>	5 Discussion	<ul> <li>Best NO<sub>x</sub> model in urban, suburbs, and highway</li> <li>Best CO<sub>2</sub> model in urban, suburbs, and highway</li> </ul>
<b>3</b> Material and methods	<ul> <li>Experimental setup</li> <li>Data</li> <li>Gradient boosting</li> <li>Features importance</li> <li>Gradient boosting regression model</li> </ul>	<b>6</b> Conclusions	<ul> <li>The features importance analysis of NO<sub>x</sub> and CO<sub>2</sub> models for urban, suburbs, and highway</li> <li>Three or four input features are good enough to build an accurate and fast model</li> </ul>

Figure 1. Structure of this study.

#### 2. Literature Review of AI Research

Jaworski et al. presented an analysis of emission data from the PEMS system for real driving cycles of various types of vehicles, complying with EURO 2–EURO 6 standards and created the emission models with the Regression Learner applications in MATLAB R2018b. Among the methods of regression trees and support vector technologies that have been used, the boosted regression tree model was assessed to be the most appropriate to well represent the real data [14].

Donateo et al. proposed a neural network model based on the interpolation of the time-histories of driving conditions (speed, altitude, ambient temperature, humidity, and pressure) and emissions measured on a diesel start-and-stop vehicle while performing a series of real driving emission (RDE) tests. The Bayesian optimizer, implemented in the MATLAB environment, was used to deal with the high number of combinations. This method minimized the number of combinations examined by the model and significantly reduced the computational time [15].

As mentioned above, a lot of PEMS measurements in real road driving have been conducted before, but not many of them have used artificial intelligence (AI) to analyze the collected data and to establish models for further predictions and evaluations. The purpose of this study is to investigate the technique of AI models for diesel vehicles in real road driving to reduce the cost of calculation and to increase the accuracy of the model prediction.

The big data analysis technique is an important tool to reduce the cost of emission measurements on real roads. Compared with traditional ways of data analysis, the analysis of vast amounts of data is no longer difficult in today's big data era. For regression analysis, machine learning technology has been widely used in related topics, such as support vector machine (SVM), random forest (RF), and artificial neural networks (ANN).

Zeng et al. used SVM to estimate the fuel consumption of gasoline vehicles and found a relationship between the fuel consumption and the corresponding factors such as average speed and driving distance [16]. They also used the multiple linear regression (MLR) model and artificial neural network to link the fuel summation with the SVM model for comparisons. However, the measurement period took one month, which is too much of a cost in time.

Henrik Almer compared the effect of sampling rate on the model performance. He used the vehicle data, road data, and weather data collected in one year between 1 June 2013 and 31 May 2014 for training. The data collected between 1 June 2014 and 31 October

2014 were used for validation and testing. The results of comparison showed that the sampling rate of 10 min is better than the sampling rate of 1 min in model performance because of its smaller variance in predicting fuel consumption. Moreover, among machine learning models (linear regression, random forest, support vector regression (SVR), and ANN), the performance of the random forest model was the best [17].

L. Thibault et al. presented the use of information and communication technology (ICT) to transmit driving information to the cloud system through smartphones and to calculate pollutant emissions in real time [18]. This coupled a microscopic model with a real-world speed profile to estimate on-road pollutant emissions. However, it is not possible to use the existing microscopic model well for a large vehicle fleet because the input parameters of this model are not available for all vehicles. Thus, the modeling approach should be chosen according to the vehicle data available for each car.

Air pollution is one of the major concerns for citizens due to its impact on public health. Vehicle emissions are related to vehicle technology and driver behavior. Therefore, L. Thibault et al. created a vehicle IoT device that gives the driver real-time feedback about the emissions and reminds the driver of exposure during the trips [19]. The whole system includes an IoT device, a smartphone, and web-based simulation models. It provides a chance to improve the existing emissions through driving behavior.

Alimissis et al. used two interpolation methodologies to evaluate the ANN model and MLR model of urban air quality data. The predictions of air pollutants' concentrations were compared with statistical measurements. ANN models were found to have better performance than MLR models in most cases [20]. G. Bandyopadhyay and S. Chattopadhyay also compared the performance of the ANN model and MLR model for ozone data. They found that ANN models are perfect for an interpolation solution to nonlinear problems using one input variable [21].

M. Gardner and S. Dorling used multilayer perceptron (MLP) neural networks to model the  $NO_x$  pollutants and found that they perform well in predicting hourly variations of  $NO_x$  and  $NO_2$  [22]. This indicates that MLP neural networks are capable of coping with complex patterns of source emissions.

In addition, F. Perrotta et al. proposed a big data-type analysis of the driving fuel consumption records of 1010 trucks over a 300 km travel distance, and performed a large amount of data processing using three techniques (SVM, RF, ANN) in a machine learning model [23]. They successfully established a fuel consumption model with big data and found that the RF model outperformed the other two models.

The gradient boosting regression model is a very powerful tool in modeling and prediction, and has been applied in many different fields [24–28]. However, this model has not been used in pollution predictions widely. A review conducted in 2018 by Bai et al. [29] showed that many AI methods have been used for air pollution predictions, including ANN, adaptive neuro-fuzzy (ANF), MLP, SVM, and SVR. However, the GBR model was not included. An investigation of the predictive power of the GBR model was carried out in this paper. Wen et al. proposed another ANN nonlinear autoregressive exogenous model (NARX) to predict NO<sub>x</sub> emissions in real road driving [30]. It is an inexpensive way of conducting RD emission measurements using an NGK NO<sub>x</sub> sensor and an Arduino board with Can Bus to measure the instantaneous vehicle emissions on the road. The results of measurement seemed to be quite reasonable compared with a full PEMS system.

Yun et al. proposed a real-time model to predict vehicle instantaneous emissions such as  $NO_x$  and  $CO_2$  [31]. This is a practical model that integrates an ANN model with a vehicle dynamic model. The accuracy of both  $NO_x$  and  $CO_2$  models were evaluated by varying number of features.

Table 1 summarizes the key points of previous investigations conducted by other researchers related to the AI model applications in vehicle emissions measurements.

No.	Authors	Reference	Key Point
1	Donateo et al.	[15]	Proposed a neural network model based on the interpolation of the time-histories of driving conditions.
2	Zeng et al.	[16]	Used support vector machine (SVM), multiple linear regression, and artificial neural network (ANN) models.
3	Henrik Almer	[17]	Proposed machine learning models (linear regression, random forest, SVR, and ANN) and found that the performance of random forest model was the best.
4	Alimissis et al.	[20]	Found artificial neural networks had better performance than multiple linear regression in most cases.
5	Bandyopadhyay et al.	[21]	Used artificial neural network (ANN) models as an interpolation solution to nonlinear problems.
6	Gardner et al.	[22]	Indicated that MLP neural networks were capable of coping with complex patterns of source emissions.
7	Perrotta et al.	[23]	Performed a large amount of data processing using three techniques (SVM, RF, ANN) in the machine learning model.
8	Wen et al.	[30]	Proposed ANN nonlinear autoregressive exogenous model (NARX) model to predict NOx emissions.
9	Yun et al.	[31]	Proposed a real-time model that integrates an artificial neural network (ANN) model with a vehicle dynamics model.

Table 1. Key point of each study in the literature review.

The process of this study is to establish the AI model of one vehicle based on the PEMS data of that specific vehicle in urban, suburb, and highways situations and then use the data to predict the emission and fuel consumption for the second route of the same vehicle. One vehicle was used in this study. The model performance of the vehicle includes  $NO_x$  and  $CO_2$  emissions and fuel consumption.

The method of gradient boosting regression (GRB) was adopted in this study to model the  $NO_x$  and  $CO_2$  emissions in three routes (urban, suburbs, and highway) and use them to predict the  $NO_x$  and  $CO_2$  emissions and fuel consumption of the same vehicle on a second journey. A different number of input features were chosen for comparison to determine the best combinations of input features of the models.

## 3. Materials and Methods

#### 3.1. Experimental Setup

The HORIBA OBS-ONE PEMS was used in this research for emission measurements on the real road. It is vehicle-mounted pollution analysis equipment that can be used to measure CO, CO<sub>2</sub>, THC, NO<sub>x</sub>, and PN in driving vehicles continuously. The system also integrates with the satellite positioning system (Global Positioning System, GPS) and the environmental conditions such as atmospheric temperature, humidity, atmospheric pressure, etc., to obtain the actual emissions data when the vehicle is driving on real roads. The specifications of the PEMS are listed in Table 2 [32]. There are 35 parameters that can be collected during the real road testing.

The detailed settings of PEMS installation are shown in Figure 2, including the location of the analyzer, pitot tube flowmeter, atmospheric sensors, tailpipe temperature sensor, and primary control computer [10]. Figure 2 shows the installation of the system in the cabin of the test vehicle. The function of the primary control computer is using the HORIBA default software to collect the data from different sensors, store the data, and output the raw data.

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Species	Measurement Range	Measurement Principle
CO <sub>2</sub>	0–5~20 vol%	HNDIR
NO <sub>x</sub>	0–100~3000 ppm	HCLD

Table 2. S	Specifications	of HORIBA	<b>OBS-ONE PEMS</b>	[32].
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Rpm capture: OBD/ECU; Exh. volume: pitot tube meter; weight: 32 kg Dimension:  $350(W) \times 25(H) \times 470(D)$  (mm); Vehicle type: Gasoline/diesel vehicles Power: 24DC/110AC; Regulations: CFR Part 1065 subpart J/EC NO 582/2011/UN ECE R83

It is noted that the PEMS has the capability to measure five pollutants in exhaust pipe. However, only  $CO_2$  and NOx are used in the analysis of this study, so only the specifications of  $CO_2$  and NOx are listed in Table 2.



Figure 2. Detailed settings of PEMS installation [10].

The PEMS system was powered by an independent battery pack inside the cabin. All the instruments were well grounded to the negative pole of the battery to prevent any pulse damage. Moreover, standard gases were carried in the cabin for calibration of sensors before and after each test to ensure the accuracy of measurement.

The raw data were processed in the following way. Take the NO<sub>x</sub> data as an example. The direct measurements by the PEMS system include the instantaneous concentrations of NO<sub>x</sub> in the exhaust flow ( $x_{NO_x}$ ), the exhaust temperature ( $T_{exh.}$ ), the pressure in the exhaust pipe ( $P_{exh.}$ ), and the exhaust flow rate ( $Q_{ex}$ ). The density of NO<sub>x</sub> ( $\rho_{NO_x}$ ) was obtained using the equation of state for ideal gas with the exhaust temperature and the exhaust pressure. The instantaneous concentrations of NO<sub>x</sub> can then be converted to the mass flow rate by multiplying the exhaust mass flow rate as shown by Equation (1).

$$\dot{m}_{\rm NO_x} = Q_{ex} x_{\rm NO_x} \rho_{\rm NO_x} \tag{1}$$

One light duty diesel vehicle, Peugeot 208, produced in 2015, which meets EURO 5 emission standards, was used as the testing vehicle in this study. The engine displacement of this vehicle is 1.6 L. The testing vehicle was run on real roads with two routes. The driving route started from Zhangbin Industrial Park to Lukang, Puyan, and Huawei. The total distance of this route is about 64 km. The route was divided into three parts intentionally, including urban, suburbs and, highways. The vehicle speed in each part was well controlled in specific ranges. The driving speed was from 0 to 60 km/h in the urban,

from 60 to 90 km/h in suburbs, and above 90 km/h on highways. Figure 3 shows the speed variations of route 1. It is noted that vehicle speed varies a lot in the first part because of lots of traffic lights in the urban area. In the second part, we can see that the vehicle speed was much faster than that in the urban area. No traffic lights were observed in this part. In the last part of this route, the vehicle speed was in the range of 90~110 km/h. This is the highway part. However, the speed was not fixed in a constant value because acceleration and deceleration occurred quite often during overtaking, and the average speed was above 100 km/h.





Two vehicle routes were used in this study. The driving patterns of these two routes are shown in Table 3. It is noted that these two routes are not different by very much. The distance and the average speed were controlled so as not to deviate from each other. The driving data on the urban, suburbs, and highways sections were analyzed in this paper. One used for building the model, and the other was used for validating the model.

<b>Table 3.</b> Driving pattern of the testing vehicle on real roa
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Driving Pattern	Driving Distance		Accele	Acceleration		Average Speed	
-	Route 1	Route 2	Route 1	Route 2	Route 1	Route 2	
Urban	26.64 km	26.53 km	$-6.7 \sim 5.3 \text{ m/s}^2$	$-7.0 \sim 7.4 \text{ m/s}^2$	26.59 km/h	25.17 km/h	
Suburbs	11.08 km	11.04 km	$-3.9 \sim 5.5 \text{ m/s}^2$	$-4.8 \sim 3.6 \text{ m/s}^2$	69.02 km/h	67.36 km/h	
Highways	26.53 km	26.79 km	$-7.3 \sim 7.7 \text{ m/s}^2$	$-7.5 \sim 6.5 \text{ m/s}^2$	101.43 km/h	100.97 km/h	

#### 3.2. Data

The total time span for one route was about 90 min. The sampling rate of data collection was 10 H<sub>z</sub>. The 10 H<sub>z</sub> sampling rate is fast enough to capture the transient behavior of the vehicle in acceleration or deceleration. A higher sampling rate is feasible for the hardware capability of the PEMS system. However, it will cause a big burden for the following data analysis because a total of 35 data were collected at a time. In total, about 54,000 data sets could be collected in one testing. There were, in total, 35 raw data collected in the PEMS. The raw data can be divided into three groups. One is operating parameters of the vehicle, including exhaust volume flow rate (m<sup>3</sup>/min), exhaust temperature (°C), exhaust pressure (kPa), engine coolant temperature (°C), fuel pressure (kPa), engine speed (rpm), intake air temperature (°C), mass air flow rate (g/s), fuel rail pressure (kPa), fuel

rail pressure (direct inject) (kPa), commanded EGR (%), barometric pressure (kPa), fuel rail pressure (absolute) (kPa), engine oil temperature (°C), engine fuel rate (L/h), actual engine percent torque (%), and engine reference torque (Nm). The second group is the environmental parameters of the vehicle, including test time (s), test distance (km), GPS altitude (m), GPS latitude (deg), GPS longitude (deg), GPS speed (km/h), GPS course (deg), system battery voltage (V), ambient temperature (°C), ambient relative humidity (%), and ambient pressure (kPa). The third group is the outcome of the vehicle, including CO (ppm), CO<sub>2</sub> (ppm), H<sub>2</sub>O (%), NO (ppm), NO<sub>x</sub> (ppm), NO<sub>2</sub> (ppm), and THC (ppmC).

Since the goal of this research is to build the models of  $CO_2$  and  $NO_x$ , some parameters that are not closely related to the formation of  $CO_2$  and  $NO_x$  are not considered in this study to reduce the burden of model building.

The instantaneous NO<sub>x</sub> and CO<sub>2</sub> concentrations in the tailpipe are shown in Figure 4a,c. The raw data were recorded with a sampling rate of 10 Hz. A total of about 36,070 data are presented in this Figure. It is noted that the NO<sub>x</sub> concentrations in the urban part vary a lot at different vehicle speeds. The same trend could be found in suburbs and highways. Even on the highway, the vehicle speeds are quite stable, and the NO<sub>x</sub> concentrations vary a lot too. The variations of CO<sub>2</sub> concentrations are similar to NO<sub>x</sub> emissions mentioned above. The maximum values of CO<sub>2</sub> are about 120,000 ppm (12%), which corresponds to an air–fuel ratio of about 20 at full loads. The minimum values of CO<sub>2</sub> are about 1093 ppm, which corresponds to very lean combustion at idle condition. It is noted that the CO<sub>2</sub> concentrations of diesel engines are much lower than of gasoline counterparts because diesel engines run at much leaner conditions [33].



**Figure 4.** The instantaneous concentrations and the production rates of NO<sub>x</sub> and CO<sub>2</sub> in urban part. (**a**) NO<sub>x</sub> concentrations (ppm); (**b**) NO<sub>x</sub> production rates (g/s); (**c**) CO<sub>2</sub> concentrations (ppm); (**d**) CO<sub>2</sub> production rates (g/s).

The instantaneous concentrations can be converted to the mass flow rate by multiplying the exhaust mass flow rate by Equation (1). The results of the conversion calculation are shown in Figure 4b,d. Because of the limited space, only the variations in urban area are shown. It is noted that the maximum flow rate of NO<sub>x</sub> is about 0.022 g/s, which occurs at acceleration. The minimum flow rate of NO<sub>x</sub> is about 0.0004 g/s, which occurs at deceleration. For CO<sub>2</sub>, the maximum flow rate is about 2.79 g/s, which occurs at acceleration, and the minimum flow rate is about 0.0068 g/s, which occurs at deceleration.

The instantaneous flow rate can be integrated with time to obtain the total emission production factor. The results of the integration are shown in Table 4.

Table 4. Total emission rate.

Emissions	Urban	Suburbs	Highway	Average
NO <sub>x</sub>	0.78 g/km	0.62 g/km	0.95 g/km	0.78 g/km
CO <sub>2</sub>	154.12 g/km	105.54 g/km	142.68 g/km	134.11 g/km

## 3.3. Gradient Boosting

An introduction of gradient boosting was presented by Li [34]. This indicated that the gradient boosting consists of two sub-terms, gradient descent and boosting, and it could be applied in regression, classification, and ranking. These applications are based on the gradient boosting algorithm proposed by Friedman [35]. This algorithm is used to minimize the loss function of the model by adding weak learners using gradient descent. The regression function is shown in Equation (2). The ensemble of gradient boosting is a supervised learning algorithm that can learn nonlinear functions to solve regression and classification problems. It is a complex model built by combining several simple models in the best possible way. The high bias and low variance models can be combined additively to form an ensemble with reducing bias while maintaining the low variance in boosting.

$$f_m(x) = f_{m-1}(x) + \rho_m h(x; \alpha_m) \tag{2}$$

where f(x) is the loss function and  $h(x; \alpha)$  is the base-learner model. For each iteration  $m = 1, 2, \dots, M$ , compensating the residues is equivalent to optimizing the expansion coefficients  $\rho_m$  and  $\alpha_m$ .

#### 3.4. Features Importance

There are 35 parameters that were collected by the PEMS during the RD testing. Nine of them are closely related to the formation of  $NO_x$ , and they are considered as the input features for the  $NO_x$  model, including mass air flow rate (g/s), exhaust flow rate (m<sup>3</sup>/min),  $CO_2$  (ppm), engine speed (rpm), tailpipe exhaust temp (°C), GPS speed (km/h), ambient humidity (%), ambient temperature (°C), and GPS altitude (m). As for the  $CO_2$  model, eight input features were considered for building the model, including exhaust flow rate, mass air flow rate, engine speed, GPS speed, tailpipe exhaust temperature, ambient humidity, GPS altitude, and ambient temperature.

Since there are too many input features for the  $NO_x$  model as well as the  $CO_2$  model, a way of reducing input features should be considered to reduce the calculation burden. John et al. proposed the two main categories of reducing selected feature numbers [36]. One is the wrapper method that pluses and/or reduces the features to figure out the optimizer that could obtain the highest performance. The other is the filter method that evaluates the correlation between the variable and the predicted value, and excludes the least relevant variable.

Casimir et al. used the Sequential Backward Selection (SBS) algorithm to find the most relevant features [37]. The appropriate features are determined for better accuracy. Dewi et al. proposed a method to cope with the features selection by using random forest (RF) algorithm [38]. They found out that different combinations of features created different model accuracy. As a result, the model performance is higher after using the RF

features selection algorithm. The model performance statistic results of using four datasets (Wisconsin Cancer, Forest Fire, Wine Quality, and Bike Sharing) show that more input features do not guarantee obtaining higher performance because more features add more complexity to the model.

There are ten features (nine features from PEMS and acceleration derived from GPS speed) that were selected for the  $NO_x$  model and nine features (eight features from PEMS and acceleration derived from GPS speed) for the  $CO_2$  model. The rank and score of feature importance were generated by permutation techniques. This was written in python code by importing the permutation\_importance from sklearn library directly. The results showed their relative predictive power to the model. The process is used to break the input feature values by randomly shuffling. This step might decrease the model performance. If the decrease is small, it means the performance of the model is pretty good. Furthermore, if the decrease is large, there is a large impact on predictions.

#### 3.5. Gradient Boosting Regression Model

Python is an interactive, object-oriented programming language. It has hundreds of excellent libraries for developers to use. Python offers a programming language that is stable, flexible, and has tools available. Therefore, there are lots of Python AI applications today. The GBR model was built in Python code. The coding process includes preprocessing, data-loading, model-defining, and model-fitting.

In this study, the data are divided into two subsets, the training set and the testing set for building the GBR model. The percentage of each data set is listed in Table 5. In general, the train–test split procedure is used to estimate the performance of the model. In this study, the training data are 75%, and the testing data are 25%.

<b>Driving Pattern</b>	NO <sub>x</sub>		CO <sub>2</sub>	
	%	Instances	%	Instances
urban Training	75	27,052	75	27,052
Test	25	9018	25	9018
suburbs Training	75	4337	75	4337
Test	25	1446	25	1446
highways Training	75	7059	75	7059
Test	25	2353	25	2353

Table 5. Training and test sets.

In building the GRB model, several parameters should be assigned in the beginning. The main parameters for the  $NO_x$  model are listed in Table 6. The parameters of the GBR model include the following: N\_estimators denote the number of trees used for boosting, and the default value is 100. Its value was set at 500 in this model. More estimators may obtain better model performance but require more calculation cost. Max\_depth denotes the maximum depth of the tree, and the default value is 3. It was set at 12 in this code. Min\_samples\_split denotes the minimum number of samples needed to split an internal node, and it was set to 10. Max\_features denote the number of features. The subsample denotes the fraction of samples that can be used to fit the individual base learners, and the default value is 1.0. Its value was set at 0.8 in this model. Learning\_rate denotes a learning rate that determines the step size at each iteration while moving toward a minimum of a loss function and the value was set at 0.1. Loss denotes the loss function. Ls was selected in this code and meant the least square loss function. There is another loss function that can be selected such as lad (least absolute deviation), huber (combination of ls and lad).

Table 6. GBR model parameters.

N_Estimators: 500	
 Max_depth: 12	
Min_samples_split: 10	
Max_features: sqrt	
Subsample: 0.8	
Learning_rate: 0.1	
Loss: ls	

During the training process of the GBR model, the ensemble was imported from Python module sklearn (SciKit-Learn) and using the gradient boosting regressor defined with an ensemble. The GBR model was defined with the above parameters and was used to fit the experimental data. Figure 5 shows the flowchart of the proposed method for emissions prediction. The first step is collecting data from PEMS records. Then, feature extraction is conducted that uses the features selection method to determine the appropriate features for model input. It is noted that acceleration is not the raw data collected by PEMS directly. It needs to be calculated from the GPS speed. The third step is loading the data and splitting them into training and testing sub-datasets by fraction. Then starts the process of training and testing for the model. The fifth step is finishing the compile process and obtaining the model. Finally, the model is used to predict the emissions in the second route.



Figure 5. Flowchart of proposed method for emissions prediction.

The model performance is examined by using mean absolute error (MAE), root means square error (RMSE), and the coefficient of determination  $R^2$ . The statistical equations are given in Equations (3)–(5), respectively, where  $P_i$  is the predicted value obtained with the model and  $T_i$  is the measured value from PEMS.  $\overline{P}_i$  is the average of the predicted value for the whole dataset.

$$MAE = \frac{1}{n} \sum_{i=1}^{n} |T_i - P_i|$$
(3)

RMSE = 
$$\sqrt{\frac{1}{n} \sum_{i=1}^{n} (T_i - P_i)^2}$$
 (4)

$$R^{2} = 1 - \frac{\sum_{i=1}^{n} (P_{i} - T_{i})^{2}}{\sum_{i=1}^{n} (\overline{P}_{i} - T_{i})^{2}}$$
(5)

#### 4. Results

#### 4.1. Features Importance Analysis

The detailed scores ranking of feature importance for  $NO_x$  models in the urban, suburb, and highway driving patterns are shown in Figure 6. It is noted that the top three features of  $NO_x$  models are the same for urban, suburban, and highways. They are mass air flow rate, exhaust flow rate, and the concentration of  $CO_2$ . It is not surprising that mass air flow rate is the most important feature because it is closely related to engine load, and  $NO_x$ 

formation is known to be dominantly determined by engine load. The second important feature is exhaust flow rate, which is actually the sum of mass air flow rate and mass fuel flow rate. Air–fuel ratio is also known to be an important factor to determine the formation of NO<sub>x</sub>. No wonder it is the second important feature. The third important feature is the concentration of  $CO_2$  in the exhaust flow.  $CO_2$  is one of the products of combustion, just as  $NO_x$ . However, unlike the gasoline engine in which  $CO_2$  concentration in the exhaust flow is almost a constant value, the concentration of  $CO_2$  in diesel engines reflects the air–fuel ratio as well as the engine load. As a result, the  $CO_2$  concentration is also a good feature for the  $NO_x$  model.



Figure 6. Feature importance detailed scores of NO<sub>x</sub> model (a) Urban; (b) Suburbs; (c) Highway.

The fourth important feature in the urban, suburb and highway patterns is not the same for all. It is interesting to note that engine speed is important in urban and suburbs driving, while acceleration is important on the highways. Engine speed is related to vehicle speed. We can see that vehicle speed varies a lot in both urban and suburbs driving, as shown in Figure 6. However, the vehicle speed is almost fixed in a narrow range on highways. That is the reason engine speed is not so important on highways.

All of the other features are not important relative to the first four features. The order of importance of the last six features in urban, suburb, and highways patterns are not the same either. Since the importance of the last six features is much lower than the first four, the order of these features is actually not to be discussed in this study.

Table 7 shows the ranking of all features in urban, suburbs, and highways driving again for a clear comparison. It is noted that even though the actual order of the last six features is not exactly the same, the trend of descending of the order is quite similar. It

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could be concluded that the relative importance of the features of the  $NO_x$  model in urban, suburban, and highways driving are quite close to each other.

Π. (	Rank					
Feature	Urban	Suburbs	Highway			
Mass Air Flow Rate	1	1	2			
Exhaust Flow Rate	2	2	1			
CO <sub>2</sub>	3	3	3			
Engine Speed	4	4	6			
Acceleration	5	9	4			
Tailpipe Exhaust Temp	6	5	7			
GPS Speed	7	6	5			
Ambient Humidity	8	8	9			
Ambient Temp	9	10	10			
GPS Altitude	10	7	8			

Table 7. Feature importance rank of NO<sub>x</sub> model in urban, suburbs, and highway.

The number of features is nine for the  $CO_2$  model. All of the features are the same as the NO<sub>x</sub> model, except that  $CO_2$  is excluded. The ranking of feature importance of  $CO_2$ models for urban, suburbs, and highways patterns are shown in Figure 7. It is noted that the top two features of  $CO_2$  models are the same for urban, suburban, and highways driving. They are mass air flow rate and exhaust flow rate. This is reasonable because these two features are closely related to engine load and air–fuel ratio, and the  $CO_2$  concentration is determined by air–fuel ratio, while the  $CO_2$  production rate is determined by engine load.



Figure 7. Feature importance detailed scores of CO<sub>2</sub> model (a) Urban; (b) Suburbs; (c) Highway.

The third important features in urban, suburbs and highways are not the same. It is interesting to note that engine speed is important in urban and suburbs driving, while acceleration is important in highways, just as was the case in the NO<sub>x</sub> model. The reason is also the same. Vehicle speed varies a lot in both urban and suburbs driving, but it is almost fixed in a narrow range in highways driving. That is the reason engine speed is not so important on highways.

Nine input features were considered in the  $CO_2$  model. However, not every feature is important for prediction. According to our calculation, the importance of each feature is ranked in Table 8. It is noted that the order of relative importance is not the same in the urban, suburbs, and highways driving patterns. Table 8 shows the ranking of all features in urban, suburbs, and highways again for a clear comparison. The first three features contribute the most (above 70%) importance from Figure 7. This also means the other six features is not exactly the same, the trend of descending of the order is quite similar. It could be concluded that the relative importance of the features of the  $CO_2$  model in urban, suburbs, and highways driving are quite close to each other.

<b>F</b> (	Rank					
Feature	Urban	Suburbs	Highway			
Exh. Flow Rate	1	1	2			
Mass Air Flow Rate	2	2	1			
Engine Speed	3	3	6			
Acceleration	4	8	3			
GPS Speed	5	7	4			
Tailpipe Exh. Temp	6	5	5			
Ambient Humidity	7	6	7			
GPS Altitude	8	4	8			
Ambient Temp	9	9	9			

Table 8. Feature importance rank of urban, suburbs, and highway CO<sub>2</sub> model.

#### 4.2. Model Performance

In this study, ten input features and nine input features were selected for  $NO_x$  and  $CO_2$  models, respectively, and the targets were NO<sub>x</sub> emission gram per second (g/s) and  $CO_2$  emission gram per second (g/s). The statistics of model performance for  $NO_x$  and  $CO_2$  in the three parts of route 1 are listed in Tables 9 and 10. The R<sup>2</sup> value is an important index to determine how well the model fits the raw data. The feature importance rank shown in Tables 7 and 8 is used to check the fitting of the model. It is noted that the feature importance rank of urban driving was selected as the base, and the same order was used in suburbs and highways. It is found that for the NO<sub>x</sub> model, the R<sup>2</sup> values of train data are all very close to 1.0 in all three parts of route 1. As for the test data, the  $R^2$  values of the urban part increase from 0.78 to 0.98 as the number of features increase from 3 to 10. The more input features we use, the higher value of  $\mathbb{R}^2$  we have. It is a reasonable result since more features are used to model the raw data, it is expected that more characteristics of data can be captured. However, it is worthwhile to note that there is a big gap between three features and four features, and the  $R^2$  values vary very little as feature numbers increase more. This implies that four features are the minimum number to totally grasp the characteristics of  $NO_x$  in the urban area. In the suburbs part and the highways part, the same trends of  $\mathbb{R}^2$  values occur. The gap between three features and four features is not so big as that in urban and in highways, but it is still obvious that four features are the minimum number to totally grasp the characteristics of  $NO_x$  in the suburbs area and in the highways area.

	Urban R <sup>2</sup>			Suburbs R <sup>2</sup>			Highway R <sup>2</sup>	
Train	Test	All	Train	Test	All	Train	Test	All
0.99	0.78	0.94	0.99	0.93	0.98	0.99	0.98	0.99
0.99	0.93	0.98	0.99	0.98	0.99	0.99	0.99	0.99
0.99	0.93	0.98	0.99	0.98	0.99	0.99	0.99	0.99
0.99	0.96	0.98	0.99	0.99	0.99	0.99	0.99	0.99
0.99	0.97	0.99	0.99	0.99	0.99	0.99	0.99	0.99
0.99	0.97	0.99	0.99	0.99	0.99	0.99	0.99	0.99
0.99	0.98	0.99	0.99	0.99	0.99	0.99	0.99	0.99
	<b>Train</b> 0.99 0.99 0.99 0.99 0.99 0.99 0.99	Urban R <sup>2</sup> Train         Test           0.99         0.78           0.99         0.93           0.99         0.93           0.99         0.93           0.99         0.96           0.99         0.97           0.99         0.97           0.99         0.98	Urban R <sup>2</sup> Train         Test         All           0.99         0.78         0.94           0.99         0.93         0.98           0.99         0.93         0.98           0.99         0.96         0.98           0.99         0.97         0.99           0.99         0.97         0.99           0.99         0.98         0.99	$\begin{tabular}{ c c c c c c } \hline Urban \\ R^2 \\ \hline Train & Test & All & Train \\ \hline 0.99 & 0.78 & 0.94 & 0.99 \\ 0.99 & 0.93 & 0.98 & 0.99 \\ 0.99 & 0.93 & 0.98 & 0.99 \\ 0.99 & 0.96 & 0.98 & 0.99 \\ 0.99 & 0.97 & 0.99 & 0.99 \\ 0.99 & 0.97 & 0.99 & 0.99 \\ 0.99 & 0.98 & 0.99 & 0.99 \\ \hline 0.99 & 0.98 & 0.99 & 0.99 \\ \hline 0.99 & 0.98 & 0.99 & 0.99 \\ \hline 0.99 & 0.98 & 0.99 & 0.99 \\ \hline 0.99 & 0.98 & 0.99 & 0.99 \\ \hline 0.99 & 0.98 & 0.99 & 0.99 \\ \hline 0.99 & 0.98 & 0.99 & 0.99 \\ \hline 0.99 & 0.98 & 0.99 & 0.99 \\ \hline 0.99 & 0.98 & 0.99 & 0.99 \\ \hline 0.99 & 0.98 & 0.99 & 0.99 \\ \hline 0.99 & 0.98 & 0.99 & 0.99 \\ \hline 0.99 & 0.98 & 0.99 & 0.99 \\ \hline 0.99 & 0.98 & 0.99 & 0.99 \\ \hline 0.99 & 0.98 & 0.99 & 0.99 \\ \hline 0.99 & 0.98 & 0.99 & 0.99 \\ \hline 0.99 & 0.98 & 0.99 & 0.99 \\ \hline 0.99 & 0.98 & 0.99 & 0.99 \\ \hline 0.99 & 0.98 & 0.99 & 0.99 \\ \hline 0.90 & 0.91 & 0.91 \\ \hline 0.91 & 0.91 & $	$\begin{tabular}{ c c c c c c c c c c c c c c c c c c c$	$\begin{array}{c c c c c c c c c c c c c c c c c c c $	$\begin{tabular}{ c c c c c c c c c c c c c c c c c c c$	$\begin{array}{c c c c c c c c c c c c c c c c c c c $

**Table 9.** Performance  $R^2$  statistics results of NO<sub>x</sub> model.

Table 10. Performance R statistics results of CO<sub>2</sub> model.

Selected Features	Urban R <sup>2</sup>			Suburbs R <sup>2</sup>			Highway R <sup>2</sup>		
	Train	Test	All	Train	Test	All	Train	Test	All
Top 3 features	0.99	0.80	0.94	0.99	0.92	0.98	0.99	0.93	0.98
Top 4 features	0.99	0.83	0.95	0.99	0.91	0.98	0.99	0.92	0.98
Top 5 features	0.99	0.86	0.96	0.99	0.93	0.98	0.99	0.94	0.98
Top 6 features	0.99	0.91	0.98	0.99	0.95	0.99	0.99	0.96	0.99
Top 7 features	0.99	0.94	0.98	0.99	0.97	0.99	0.99	0.97	0.99
Top 8 features	0.99	0.95	0.98	0.99	0.97	0.99	0.99	0.98	0.99
Top 9 features	0.99	0.95	0.98	0.99	0.97	0.99	0.99	0.98	0.99

The performance of  $CO_2$  models is similar to that of  $NO_x$  models. The  $R^2$  values of train data are all very close to 1.0 in all three parts of route 1, implying that the training process goes very well. As for the test data, the  $R^2$  values of the urban part increase from 0.80 to 0.95 as the number of features increase from three to nine. However, unlike the  $NO_x$  model where a big gap between three features and four features can be observed, the  $R^2$  values increase almost linearly with the number of features up to seven features where the increase in the  $R^2$  value begins to slow down. In the suburbs part and the highways part, the same trends of  $R^2$  values occur. The  $R^2$  values increase linearly with the number of features to totally grasp the characteristics of raw data in all parts of the route.

In addition, Figure 8a,b show the performance statistics results of MAE and RMSE for  $NO_x$  models in route 1, respectively. They are other methods of performance evaluation used to check the model accuracy. An opposite trend of the R<sup>2</sup> value is found, that the more features we use, the lower value of MAE we obtain. A lower value of MAE means better accuracy by the definition of MAE in Equation (3). It is noted that the prediction values are very close to the target values. In the meantime, the results for RMSE statistics are very similar to those of MAE.

In Figure 8a, it is noted that the value of MAE decreases as the number of features increases in urban, suburbs, and highways routes. Four features might be the best choice for this case considering the computational cost and accuracy, but for reaching the best performance, all features are the only option, even when using more calculation cost. It is noted that the trend in Figure 8b is the same as MAE.

Figure 9 shows the MAE statistics for the  $CO_2$  model. Only the MAE statistics are shown because the trend of RMSE statistics is also very similar to that of MAE, just as the case of the  $NO_x$  model. It is interesting to note that the trend of MAE in the urban part is the same as that in the  $NO_x$  model, i.e., the value of MAE decreases as the number of features increases. However, in the suburbs and highways parts, different trends show that three features input has a lower value of MAE than four features input. As a result, using three features would be the best choice to obtain good performance and low computation cost for urban, suburbs, and highways driving in route 1. Increasing the number of features



can obtain better performance if computational cost needs are not to be considered. In that case, eight features might be the best choice.

Figure 8. Performance MAE and RMSE statistics results of NO<sub>x</sub> model (a) MAE; (b) RMSE.



Figure 9. Performance MAE statistics results of CO<sub>2</sub> model.

In this study, the NO<sub>x</sub> and CO<sub>2</sub> models obtained in route 1 were used to predict the vehicle emissions driving in the urban, suburbs, and highways parts of the second route to investigate the universality of the models. The results of NO<sub>x</sub> predictions in the second route are listed in Table 11. It is noted that the R<sup>2</sup> values in the urban part vary from 0.69 to 0.88. The R<sup>2</sup> values of route 2 are lower than route 1, even for the same vehicle. This is reasonable because the traffic flow, route conditions, and driver behaviors are different. The average speed of these two routes is quite similar, as shown in Table 3, but the acceleration of these two routes are different. The second route has wider acceleration ranges than route 1, probably reflecting the characteristics of the drivers. Taking a close look at the model performance, the lowest R<sup>2</sup> value occurs when using the top three features for input features. This is the same trend as for the route 1 urban NO<sub>x</sub> model. Unlike route 1's urban performance results, the maximum R<sup>2</sup> values were found using six and seven features for input, and the whole results show that the performance does not increase while the number of features increases.

In the suburbs part of the second route, the range of  $R^2$  varies from 0.79 to 0.89 and shows a different trend to the urban part. The maximum  $R^2$  value uses five features for input, and then the  $R^2$  values drop after five features and reach the lowest value when using all features for input. The  $R^2$  of the highways part varies from 0.93 to 0.96. All of these values are higher than the urban and suburbs values. It is noted that the  $R^2$  of highways is the best among the three driving patterns.

Selected Features	R <sup>2</sup> Urban Model	R <sup>2</sup> Suburbs Model	R <sup>2</sup> Highway Model
Top 3 features	0.69	0.88	0.94
Top 4 features	0.87	0.88	0.96
Top 5 features	0.87	0.89	0.96
Top 6 features	0.88	0.80	0.94
Top 7 features	0.88	0.79	0.94
Top 8 features	0.83	0.80	0.93
Top 9 features	0.86	0.80	0.93

Table 11. Performance statistics results of using NO<sub>x</sub> models to predict the second route NO<sub>x</sub> emission.

The performance results when using route 1  $CO_2$  models to predict the second route  $CO_2$  are listed in Table 12. The performance value increases while using three and four input features and reaches the maximum value of using five features, then drops with an increasing number of features for urban driving. The trend of R<sup>2</sup> variations agrees with the results of the  $CO_2$  models feature importance analysis shown in Figure 7a. It is noted that the features importance influences the model performance a lot and reflects the same trend of using this model to predict the second route.

Table 12. Performance statistics results of using  $CO_2$  models to predict the second route  $CO_2$  emission.

Selected Features	R <sup>2</sup> Urban Model	R <sup>2</sup> Suburbs Model	R <sup>2</sup> Highway Model
Top 3 features	0.69	0.81	0.80
Top 4 features	0.75	0.82	0.82
Top 5 features	0.79	0.81	0.83
Top 6 features	0.74	0.76	0.78
Top 7 features	0.67	0.79	0.75
Top 8 features	0.63	0.76	0.73
Top 9 features	0.61	0.78	0.74

According to the above results, GBR models present excellent  $R^2$  values, representing the model performance for NO<sub>x</sub> and CO<sub>2</sub> prediction.

Table 12 shows that the  $R^2$  values of suburbs driving are higher than for urban. This is the same result as using the route 1 NO<sub>x</sub> model to conduct prediction in the second route due to the similar feature importance, such as mass air flow rate, exhaust flow rate, and engine speed. It is interesting that the trend of  $R^2$  values of highway driving using three, four and five features are similar to urban, but the  $R^2$  values of highway driving using six, seven and eight features are similar to suburbs.

In summary, Figures 10–12 shows the comparisons of the  $R^2$  values of NO<sub>x</sub> and CO<sub>2</sub> models for the training sub-dataset, the test sub-dataset, all data, and the prediction of the second route using a different number of features in urban, suburbs, and highways according to Tables 9–12. The criterion for the best model is to obtain the highest  $R^2$  value in both route 1 and the second route. The best prediction is the highest  $R^2$  value of the second route. For example, the best NO<sub>x</sub> model in urban driving, as shown in Figure 10a, is the model with seven input features. However, the best prediction is the model with six input features. Figure 10b shows the best model with eight input features and the best prediction with five input features for the CO<sub>2</sub> model in urban driving, according to the same criterion. The statistics of the input number of features for the best model and best prediction in urban, suburbs, and highways routes are listed in Table 13. It can be found that the number of input features for the best prediction is less than that of the best model.



**Figure 10.** (a) Comparisons of the  $R^2$  value of NO<sub>x</sub> models for the training sub-dataset, the test sub-dataset, all data, and the route 2 prediction in urban; (b) Comparisons of the  $R^2$  value of CO<sub>2</sub> models for the training sub-dataset, the test sub-dataset, all data, and the route 2 prediction in urban.



**Figure 11.** (a) Comparisons of the  $R^2$  value of NO<sub>x</sub> models for the training sub-dataset, the test sub-dataset, all data, and the route 2 prediction in suburbs; (b) Comparisons of the  $R^2$  value of CO<sub>2</sub> models for the training sub-dataset, the test sub-dataset, all data, and the route 2 prediction in suburbs.



**Figure 12.** (a) Comparisons of the  $R^2$  value of NO<sub>x</sub> models for the training sub-dataset, the test sub-dataset, all data, and the route 2 prediction in highway; (b) Comparisons of the  $R^2$  value of CO<sub>2</sub> models for the training sub-dataset, the test sub-dataset, all data, and the route 2 prediction in highway.

	NO <sub>x</sub>			CO <sub>2</sub>		
	Urban	Suburbs	Highways	Urban	Suburbs	Highways
Best model	7	5	4	8	7	9
Best prediction	6	5	4	5	4	5

Table 13. Input number of features for best model and best prediction.

The models trained by GBR can not only predict the instantaneous emission production on the road, as shown in previous figures, but also can be used to evaluate the emission factors of the vehicle driven on real roads. Table 14 and Figure 13 present the results of the calculation for the  $NO_x$  emission factors with different input features. It is noted that the predicted emission factors are very close to the measured factors in the three parts of route 1 for all the cases of 3 input features to 10 input features.

Table 14. Results of  $NO_x$  and  $CO_2$  emission factor predictions.

Selected	Urban		Sub	urbs	Highway	
Features	NO <sub>x</sub> Prediction	CO <sub>2</sub> Prediction	NO <sub>x</sub> Prediction	CO <sub>2</sub> Prediction	NO <sub>x</sub> Prediction	CO <sub>2</sub> Prediction
Top 3 features	0.78	154.24	0.62	105.77	0.95	142.76
Top 4 features	0.78	154.05	0.62	105.83	0.95	142.72
Top 5 features	0.78	154.01	0.62	105.94	0.95	142.63
Top 6 features	0.78	153.91	0.62	108.79	0.95	142.76
Top 7 features	0.78	153.95	0.62	105.70	0.95	142.77
Top 8 features	0.78	153.97	0.62	105.72	0.95	142.70
Top 9 features	0.78	153.97	0.62	105.72	0.95	142.60
PEMS data	0.78	154.12	0.62	105.54	0.95	142.60





Figure 13. Results of NO<sub>x</sub> emission factor predictions (a) Urban; (b) Suburbs; (c) Highway.

Table 14 and Figure 14 show the results of  $CO_2$  emission factors calculations. The results are as good as those for  $NO_x$  predictions except in the suburbs part with six input features where the error between the predicted value and measured data is 0.4%, which is still very small.



Figure 14. Results of CO<sub>2</sub> emission factor predictions (a) Urban; (b) Suburbs; (c) Highway.

Table 15, and Figures 15 and 16 show that using route 1 NO<sub>x</sub> and CO<sub>2</sub> models to predict urban, suburbs, and highway emissions in the second route obtains the same results as Tables 11 and 12 in terms of emissions gram per kilometer. It is clear that model performance decides the error between measurement data and predictions. The best performances of NO<sub>x</sub> and CO<sub>2</sub> in the second route urban model use the top six features and top five features, respectively. The best performance of NO<sub>x</sub> prediction in the second route in the suburbs uses the top five features but CO<sub>2</sub> prediction uses the top four features. The best performance of the NO<sub>x</sub> prediction in the second route in the highway model uses the top four features, and using the top five features to fit the model obtains the best performance of CO<sub>2</sub> prediction in the highway model.

Table 15. Second Route  $NO_x$  and  $CO_2$  emission g/km predictions statistics results of using route 1 urbanmodels.

Selected	Urban		Sub	urbs	Highway	
Features	NO <sub>x</sub> Prediction	CO <sub>2</sub> Prediction	NO <sub>x</sub> Prediction	CO <sub>2</sub> Prediction	NO <sub>x</sub> Prediction	CO <sub>2</sub> Prediction
Top 3 features	0.77	141.11	0.86	124.24	0.90	129.28
Top 4 features	0.82	142.21	0.90	123.73	0.92	130.39
Top 5 features	0.82	143.9	0.89	141.75	0.92	129.04
Top 6 features	0.76	145.44	1.09	129.67	0.95	129.20
Top 7 features	0.76	159.57	1.04	133.34	0.96	121.81
Top 8 features	0.81	172.54	1.14	122.44	0.96	136.55
Top 9 features	0.81	172.58	1.07	127.40	0.97	136.47
PEMS data	0.78	141.2	0.85	119.14	0.94	124.20



**Figure 15.** Second route  $NO_x$  emission factor predictions by using route 1  $NO_x$  urban model (**a**) Urban; (**b**) Suburbs; (**c**) Highway.

Diesel is a volatile substance that consists of hydrocarbon. The diesel fuel chemical formula is  $C_{16}H_{30}$  with the density of 0.85 kg/L. The stoichiometric combustion reaction of diesel fuel with air in a diesel engine is as following.

$$C_{16}H_{30} + 23.5(O_2 + 3.76N_2) \rightarrow 16CO_2 + 15H_2O + 88.36N_2$$
(6)

According to Equation (6), fuel consumption can be calculated by utilizing  $CO_2$  emission gram per kilometer, as obtained above. The results of fuel consumption calculations in route 1 are shown in Table 16 and Figure 17. It is noted that the errors of fuel consumption are very similar to the errors of  $CO_2$ , as in Figure 12. This is very reasonable because the fuel consumption in a diesel engine is closely related to  $CO_2$  production. The results of fuel consumption predictions in the second route are shown in Table 16 and Figure 18. The same trends of model errors can be observed as in Figure 16.

160 -

140

120

80 -

60

40

20 -

0+ 2

160 -140 -

120

Highway CO<sub>2</sub> [g/km] 100 -80 -60 -40 -20 -0 + 2 3

3

Urban CO<sub>2</sub> [g/km] 100



Figure 16. Second route CO<sub>2</sub> emission factor predictions by using route 1 using CO<sub>2</sub> urban model (a) Urban; (b) Suburbs; (c) Highway.

Selected Features	Urban		Sub	urbs	Highway	
	Route 1 Prediction	Route 2 Prediction	Route 1 Prediction	Route 2 Prediction	Route 1 Prediction	Route 2 Prediction
Top 3 features	17.48	19.10	25.48	21.70	18.89	20.85
Top 4 features	17.50	18.95	25.47	21.79	18.89	20.67
Top 5 features	17.50	18.73	25.44	19.02	18.90	20.89
Top 6 features	17.51	18.53	24.78	20.79	18.89	20.86
Top 7 features	17.51	16.89	25.50	20.22	18.89	22.13
Top 8 features	17.51	15.62	25.50	22.01	18.89	19.74
Top 9 features	17.51	15.62	25.50	21.16	18.90	19.75
PEMS data	17.49	19.09	25.54	22.62	18.89	21.70





Figure 17. Fuel consumption statistics results in route 1 (a) Urban; (b) Suburbs; (c) Highway.



Figure 18. Second route fuel consumption predictions by using route 1 CO<sub>2</sub> urban model (a) Urban; (b) Suburbs; (c) Highway.

## 5. Discussion

According to Tables 9 and 10, the best model is built by selecting the top seven input features for the  $NO_x$  model and the top eight input features for the  $CO_2$  model in urban driving. The  $R^2$  values of the NO<sub>x</sub> model and the CO<sub>2</sub> model are 0.99 and 0.98, respectively. These results are the best  $R^2$  values among the NO<sub>x</sub> and CO<sub>2</sub> models when selecting different input numbers of features. It is noted that the choice was based on the prediction accuracy only, calculation cost was not considered. The prediction results of the best  $NO_x$ and  $CO_2$  models are plotted in Figure 19a,b, in which the red triangle represents the test sub-dataset and the blue square represents the training sub-dataset. Since the  $R^2$  value of the test sub-dataset for the best NO<sub>x</sub> model is 0.97, some small deviations between the predictions and the measurements can still be observed in Figure 19a. Furthermore, the bar chart located at the lower right corner shows the ground truth of the predictions. Ground truth is an evaluation of the results of model accuracy against the targets. The distribution of ground truth would concentrate on zero value for a perfect model. It can be seen for the best  $NO_x$  model the distribution of ground truth spreads a little bit around zero value, indicating the existence of deviations. Figure 19b shows the predictions of the best  $CO_2$ model. The same deviations can be observed as those in the  $NO_x$  model. However, since the  $R^2$  value of the test sub-dataset for the best  $CO_2$  model is 0.95, more deviations can be observed in Figure 19b. The bar chart of the ground truth also spreads more in the  $CO_2$ model. In general, both the  $NO_x$  and  $CO_2$  models show pretty good accuracy, as shown in Figure 19a,b.



**Figure 19.** (a) Deviations between the predictions and the measurements and ground truth plot of the best  $NO_x$  model in urban; (b) Deviations between the predictions and the measurements and ground truth plot of the best  $CO_2$  model in urban.

As for the suburbs part, the best models are built by using the top five features for  $NO_x$  and the top seven features for  $CO_2$  according to the results listed in Tables 9 and 10, respectively. The  $R^2$  values of both the  $NO_x$  model and the  $CO_2$  model are 0.99. Figure 20a,b shows the prediction results of the best  $NO_x$  and  $CO_2$  models. The red triangle represents the test sub-dataset, and the blue square represents the training sub-dataset. It can be observed that deviations are very small in the  $NO_x$  models because the  $R^2$  value is close to 1. However, since the  $R^2$  value of the test sub-dataset for the best  $CO_2$  model is 0.97, more deviations can be observed in Figure 20b. Taking a close look at the ground truth distributions, they are very close to the zero value, indicating only little deviations occur. Both the  $NO_x$  and  $CO_2$  models show pretty good accuracy, as shown in Figure 20a,b.



**Figure 20.** (a) Deviations between the predictions and the measurements and ground truth plot of the best  $NO_x$  model in suburbs; (b) Deviations between the predictions and the measurements and ground truth plot of the best  $CO_2$  model in suburbs.

The model performance in the highways part is examined in the following. The best model is built by using the top four features for  $NO_x$ , and the top nine features are used for the  $CO_2$  model according to the results listed in Tables 9 and 10, respectively. It is noted that the  $R^2$  values of both the  $NO_x$  model and the  $CO_2$  model are 0.99. The best  $NO_x$  and  $CO_2$  models prediction results of the test and training sub-datasets are plotted in Figure 21a,b with a red triangle and blue square, respectively. Very few deviations can be observed for the best  $NO_x$  model in Figure 21a. More deviations can be found for the best  $CO_2$  model in Figure 21b because the  $R^2$  value is 0.98. The bar charts located in the lower right corner show the ground truth distributions of the predictions. Both models show pretty good accuracy, with the distributions concentrating around zero value.



Figure 21. (a) Deviations between the predictions and the measurements and ground truth plot of the best  $NO_x$  model in highways; (b) Deviations between the predictions and the measurements and ground truth plot of the best  $CO_2$  model in highways.

Figure 22a shows the deviations between the predictions and the measurements by using the top four features as input to build the NO<sub>x</sub> model in the urban part. Comparisons between Figures 19a and 22a show that the deviations in Figure 22a are a little bit greater than Figure 19a. This is reasonable since the best model has the highest performance  $R^2$  value. It is also noted that a similar result as the NO<sub>x</sub> model is found for the CO<sub>2</sub> model in the urban part shown in Figure 22b. Moreover, taking a look at the second route prediction  $R^2$  values for the NO<sub>x</sub> model in the urban route would find that the  $R^2$  values of using the top four features for input are close to the  $R^2$  value of the best prediction. This is similar to

the  $CO_2$  model where the  $R^2$  values of using the top four features for input is 0.75, and the best prediction has the  $R^2$  value of 0.79. As a result, selections of the  $NO_x$  model and  $CO_2$  model that use the top four features could be the second choice for second route prediction.



**Figure 22.** (a) Deviations between the predictions and the measurements plot of using the top 4 features  $NO_x$  model in urban. (b) Deviations between the predictions and the measurements plot of using the top 4 features  $CO_2$  model in urban.

The purpose of this paper is to find a feasible way to build a predictive model for diesel emissions. It was found that three parameters are good enough to build a model. A lot of computational costs could be saved with the simplified model. The results of this paper would be very useful for the modelers thereafter. The strategy of emission reduction is not the purpose of this paper. However, according to the results of the emission model developed in this paper, the most important features are exhaust flow rate, air–fuel ratio, and engine speed. The implications of the findings are that reducing the engine load may abate the emissions of a running vehicle.

The  $NO_x$  emission factors calculation from Table 14 shows that the lowest value occurs in the suburbs. It is observed from Table 14 that there is the same trend in the  $CO_2$  emission factors calculation. The common reason might be acceleration and deceleration. It would be helpful to remind drivers to control their speed to reduce air pollution.

### 6. Conclusions

The features importance analysis of  $NO_x$  and  $CO_2$  models for urban, suburb, and highways are built successfully. The top three features of urban, suburban, and highway  $NO_x$  models are airflow rate, exhaust flow rate, and  $CO_2$  concentrations, and the top three features of urban and suburban  $CO_2$  models are exhaust flow rate, airflow rate, and engine speed. The top three features of highway  $CO_2$  models are airflow rate, exhaust flow rate, and acceleration.

In order to have an accurate prediction, generally, we need more input features. However, the accuracy is not proportional to the number of input features. More input features do not guarantee more accurate predictions. The best models need 4~9 input features to have the highest  $R^2$  value. The best predictions of the second route need 4~6 input features. The choice of input features depends on the route characteristics and the emissions.

If the computational cost is a major concern, the model could be simplified to reduce the number of input features. The  $R^2$  values of the simplified  $NO_x$  models using the top three and top four input features are very close to the best model. The difference in  $R^2$ values is as small as 0.01. The  $R^2$  values of the simplified  $CO_2$  models using the top three and top four input features are also very close to the best model. The difference in  $R^2$ values is about 0.04.

The purpose of this paper is to find a feasible way to build a predictive model for diesel emissions. It was found that three parameters are good enough to build a model. A

lot of computational costs could be saved with the simplified model. The results of this paper would be very useful for the modelers thereafter.

Moreover, the gradient boosting regression model is a very powerful tool in modeling and prediction, and has been applied in many different fields. However, this model has not been used in pollution predictions widely. The NO<sub>x</sub> and CO<sub>2</sub> GBR models were built successfully in this study to predict the emissions of diesel vehicles on real roads with pretty good R<sup>2</sup> values. The results show that the GBR is a practical approach to making accurate predictions.

It is recommended that three or four input features are good enough to build an accurate and fast model for the prediction of the  $NO_x$  and  $CO_2$  emissions of diesel vehicles running on real roads. However, the choice of input features is important. An inappropriate choice of input feature may give poor results.

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