Value construction through sequential sampling explains serial dependencies in decision making

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Abstract Many decisions are expressed as a preference for one item over another. When these items 11 are familiar, it is often assumed that the decision maker assigns a value to each of the items and chooses 12 the item with the highest value. These values may be imperfectly recalled, but are assumed to be stable 13 over the course of an interview or psychological experiment. Choices that are inconsistent with a stated 14 valuation are thought to occur because of unspecified noise that corrupts the neural representation of 15 value. Assuming that the noise is uncorrelated over time, the pattern of choices and response times in 16 value-based decisions are modeled within the framework of Bounded Evidence Accumulation (BEA). 17 similar to that used in perceptual decision-making. In BEA, noisy evidence samples accumulate over 18 time until the accumulated evidence for one of the options reaches a threshold. Here, we argue that 19 the assumption of temporally uncorrelated noise, while reasonable for perceptual decisions, is not 20 reasonable for value-based decisions. Subjective values depend on the internal state of the decision 21 maker, including their desires, needs, priorities, attentional state, and goals. These internal states 22 may change over time, or undergo revaluation, as will the subjective values. We reasoned that these 23 hypothetical value changes should be detectable in the pattern of choices made over a sequence of 24 decisions. We reanalyzed data from a well-studied task in which participants were presented with pairs 25 of snacks and asked to choose the one they preferred. Using a novel algorithm (Reval), we show that the 26 subjective value of the items changes significantly during a short experimental session (about 1 hour). 27 Values derived with Reval explain choice and response time better than explicitly stated values. They 28 also better explain the BOLD signal in the ventromedial prefrontal cortex, known to represent the value 29 of decision alternatives. Revaluation is also observed in a BEA model in which successive evidence 30 samples are not assumed to be independent. We argue that revaluation is a consequence of the process 31

³² by which values are constructed during deliberation to resolve preference choices.

33 Introduction

A central idea in decision theory and economics is that each good can be assigned a scalar utility value

that reflects its desirability. The concept of utility, or subjective value, provides a common currency

³⁶ for comparing dissimilar goods (e.g., pears and apples) such that decision-making can be reduced

to estimating the utility of each good and comparing them (von Neumann and Morgenstern, 1944; Samuelson, 1937; Montague and Berns, 2002). The idea is supported by studies that have identified

³³ neurons that correlate with the subjective value of alternatives in various brain structures, most notably

the ventromedial prefrontal cortex, and it is so pervasive that decisions based on preferences are often

referred to as "value-based decisions" (Kable and Glimcher, 2007; Kim et al., 2008; Padoa-Schioppa

42 and Assad, 2006).

43 Choice and response time (RT) in simple perceptual and mnemonic decisions are often modeled within

the framework of bounded evidence accumulation (BEA). The framework posits that evidence samples

45 for and against the different options are accumulated over time until the accumulated evidence for one of

the options reaches a threshold or bound (Ratcliff, 1978; Gold and Shadlen, 2007). A case in point is

47 the random dot motion (RDM) discrimination task, in which participants must decide whether randomly

noving dots have net rightward or leftward motion, while the experimenter controls the proportion of

- dots moving coherently in one direction, termed the motion strength (e.g., Gold and Shadlen, 2007).
- 50 BEA models explain the choice, RT, and confidence in the RDM task under the assumption that the rate
- of accumulation, often termed the *drift rate*, depends on motion strength (van Den Berg et al., 2016;
- 52 Kiani et al., 2014). Value-based decisions have also been modeled within the framework of BEA. The
- sa key assumption is that at any given time, decision-makers only have access to a noisy representation of
- the subjective value of each item, and the drift rate depends on the difference between the subjective
- values of the items (Kraibich et al., 2010; Thomas et al., 2019; Sepulveda et al., 2020; Bakkour et al.,
- 56 2019).
- 57 A condition that renders the BEA framework normative is that the noise corrupting the evidence samples is
- ⁵⁸ independent, or equivalently, that the evidence samples are conditionally independent given the drift rate.
- ⁵⁹ For example, in modeling the RDM and other perceptual decision making tasks, evidence samples are
- assumed to be independent of each other, conditioned on motion strength and direction (e.g., Zylberberg
- et al., 2016). This assumption is sensible because (i) the main source of stochasticity in perceptual
- e2 decision making is the noise affecting the sensory representation of the evidence, which has a short-lived
- autocorrelation, and (ii) these decisions are often based on an evidence stream (e.g., a dynamic random
- dot display) that provides conditionally independent samples, by design. The assumption of conditional
- independence justifies the process of evidence accumulation, because accumulation (or averaging) can
- only remove the noise components that are not shared by the evidence samples.

For value-based decisions, the assumption of conditional independence is guestionable. Alternatives 67 often differ across multiple attributes (e.g., Busemever and Townsend, 1993; Tversky, 1977). For 68 example, when choosing between different snacks, they may differ in calories, healthiness, palatability, 69 and so on (Suzuki et al., 2017). The weight given to each attribute depends on the decision-maker's 70 internal state (Noguchi and Stewart, 2018; Juechems and Summerfield, 2019). This internal state 71 includes desires, needs, priorities, attentional state and goals. We use the term mindset, or state of 72 mind, to refer to all of these internal influences on valuation. A mindset can be persistent. For example, 73 a famished decision-maker may prioritize the nutritional content of each food when making a choice. 74 Under less pressing circumstances, the salience of an attribute may be suggested by snack alternatives 75 themselves. For example, seeing French fries may make us aware that we crave something salty, and 76 saltiness becomes a relevant attribute informing the current decision and possibly future decisions too. 77 The examples illustrate how a decision-maker's mindset can shift rapidly or meander, based on the 78 attributes in focus or the identity of the items under consideration (Shadlen and Shohamy, 2016; Stewart 79 et al., 2006). Importantly, mindset is dynamic. It can change abruptly, motivated by a thought in an earlier 80 trial or by interoception during deliberation (e.g., thirst). Unlike perceptual decision-making, where the 81 expectation of a sample of evidence is thought to be fixed, conditional on the stimulus, the expectation of 82

the evidence bearing on preference is itself potentially dynamic.

We sought to test the notion that the desirability of an item changes as a result of the deliberation that leads to a choice. We hypothesized that if subjective values are dynamic, then value-based decisions should exhibit serial dependencies when multiple decisions are made in a sequence. A choice provides information not only about which option is preferred, but also about the decision maker's mindset at the moment of the choice (e.g., whether they prioritize satiation or palatability). Therefore, a choice is informative about future choices because the decision maker's *mindset* is likely to endure longer than a single decision, or even multiple decisions.

We reanalyzed data from Bakkour et al. (2019). Participants were presented with pairs of snacks and had to choose the one they preferred. This *Food choice task* has been used extensively to study the sequential sampling process underlying value-based decisions (e.g., Krajbich et al., 2010). Crucially, in the Bakkour et al. (2019) experiment, each item was presented multiple times, allowing us to infer how preference for an item changes during a single experimental session. Using a novel algorithm we call *Reval*, we show that the subjective value of items changed over the session. The revaluation was replicated in a sequential sampling model in which successive samples of evidence are not assumed to

- ⁹⁸ be conditionally independent. We argue that the revaluation process we observed reflects a process by
- ⁹⁹ which the value of the alternatives is constructed during deliberation by querying memory and prospecting
- for evidence that bears on desirability (Lichtenstein and Slovic, 2006; Johnson et al., 2007).

101 **Results**

102 Food choice task

We re-examined data from a previous study in which 30 participants completed a food choice task (Bakkour et al., 2019). Prior to the main experiment, participants were asked to indicate their willingness to pay for each of 60 snack items on a scale from 0 to US\$3 (Fig. 1A). We refer to these explicitly

- reported values as *s*-values, or v_s (where *s* stands for 'static' as opposed to the 'dynamic' values we define below). In the main experiment (conducted in an MRI scanner), participants were shown pairs of
- ¹⁰⁷ define below). In the main experiment (conducted in an MRI scanner), participants were shown pairs of ¹⁰⁸ images of previously rated snack items and had to choose which snack they would prefer to consume at
- the end of the study (Fig. 1B).



Figure 1. Food choice task

(A) In an initial 'ratings' task, participants were shown 60 individual appetizing snack items and asked to indicate how much they would be willing to pay for each item using a monetary scale ranging from \$0 to \$3.

(B) In the main experiment, participants were presented with pairs of snack items and asked to choose which one they would prefer to consume at the end of the session. After making their choice, the chosen item was highlighted by a square box for an additional 0.5 s. Each of the 30 participants completed 210 trials, with each item appearing 7 times during the experiment. A subset of 60 item pairs were repeated once.

(C) Proportion of trials in which participants selected the right item as a function of the difference in value between the right and left items (Δv_s). Proportions were first determined for each participant and then averaged across

participants. Error bars indicate the standard error of the mean (s.e.m.) across participants.

(D) Mean response time as a function of the difference in value between the right and left items. Error bars indicate the s.e.m. across participants. Red curves in panels C-D are fits of a drift-diffusion model (DDM).

¹¹⁰ The data from Bakkour et al. (2019) replicate the behavior typically observed in the task. Both choice

- and response time were systematically related to the difference in *s-value*, (Δv_s) , between the right and
- 112 left items. Participants were more likely to choose the item to which they assigned a higher value during
- the rating phase (p<0.0001; H_0 : $\beta_1 = 0$; Eq. 2). They were also more likely to respond faster when the
- absolute value of the difference between the items was greater (p<0.0001; H_0 : $\beta_1 = 0$; Eq. 3).
- The relationship between Δv_s , choice, and response time is well described by a bounded evidence
- accumulation model (Krajbich et al., 2010; Bakkour et al., 2019). The solid lines in Fig. 1C-D illustrate
- the fit of such a model in which the drift rate depends on Δv_s . Overall, the behavior of our participants in

the task is similar to that observed in other studies using the same task (e.g., Krajbich et al., 2010; Folke

et al., 2016; Sepulveda et al., 2020).

Limited power of explicit reports of value to explain binary choices

An intriguing aspect of the decision process in the food choice task is its highly stochastic nature. This 121 is evident from the shallowness of the choice function (Fig. 1C): participants chose the item with a 122 higher s-value in only 64% of the trials. This variability is typically attributed to unspecified noise when 123 recalling item values from memory (e.g., Krajbich et al., 2010). An alternative explanation is rooted 124 in constructive value theories, which suggest that the value of each item is constructed, not retrieved. 125 during the decision process (Lichtenstein and Slovic, 2006; Shadlen and Shohamy, 2016; Johnson et al., 126 2007). This construction process is sensitive to the context in which it is elicited (e.g., the identity of 127 items being compared), so the values reported during the valuation process may differ from those used 128 in the choice task. According to this idea, the apparently stochastic choice is a veridical reflection of the 129 constructed values. 130

If this were true, then the choice on any one *cynosure* trial—that is, the trial we are scrutinizing—would 131 be better explained by values inferred from the choices on the other trials than by the *s-values*. We 132 therefore compared two regression models that produce the log odds of the choice on each cynosure 133 trial. The first regression model uses the s-values plus a potential bias for the left or right item. The 134 second regression model includes one regression coefficient per item plus a left/right bias. It uses all the 135 other trials (except repetitions of the identical pair of items) to establish the weights. While this model 136 has more free parameters, the comparison is valid because we are using the models to predict the 137 choices made on trials that were not used for model fitting. The better model is the one that produces 138 larger log odds of the choice on the cynosure trial. As shown in Fig. 2, the second regression model is 139 superior. 140



Figure 2. Individual choices are better explained by values inferred from the other trials than values reported in the ratings task

Gray data points represent the total log-likelihood of each participant's choices, given two types of predictions: (*abscissa*) from a logistic regression, fit to the static values; (*ordinate*) from a procedure that infers the values based on choices on the other trials. Predictions derived from the other trials is better in all but four participants. The red markers were obtained using the same procedure, applied to choices simulated under the assumption that the *s-values* are the true values of the items. It shows that the inferential procedure is not guaranteed to improve predictions.

To ensure that this result is not produced artifactually from the algorithm, we performed the same analysis on simulated data. We fit the experimentally observed choices using a logistic regression model with Δv_s and an offset as independent variables, and simulated the choices by sampling from Bernoulli distributions with parameter, *p*, specified by the logistic function that best fit each participant's choices (i.e., weighted-coin flips). We repeated the model comparison using the simulated choices and found that, contrary to what we observed in the experimental data, the model using explicit value reports is the better predictor (Fig. 2, red).

Iaken together, these analyses show that explicit value reports have limited power to predict choices,
 which partially explains their apparent stochasticity (Konovalov and Krajbich, 2019; Verhoef and Franses,
 2003; Wardman, 1988). In the following sections, we elaborate on this observation. Not only do the
 values used to make the binary choices differ from the *s-values*, they drift apart during the experiment.

We show that these changes arise through the deliberative process leading to the preference decisions themselves.

¹⁵⁴ Preferences change over the course of the experiment

In the experiment, a subset of the 60 snack pairs were presented twice, in a random order within the 155 sequence of trials. These trials allow us to assess whether preferences change over the course of 156 a session. For these duplicated item pairs, we calculate the average number of times that the same 157 item was chosen on both presentations-which we refer to as the match probability. Participants were 158 more likely to select the same option when presentations of the same pair were closer in time (Fig. 3). 159 To assess the significance of this effect, we fit a logistic regression model using all pairs of trials with 160 identical stimuli to predict the probability that the same item would be chosen on both occasions. The 161 regression coefficient associated with the number of trials between repetitions was negative and highly 162 significant (p<0.0001; t-test, Eq. 8). It therefore follows that preferences are not fixed, not even over the 163

¹⁶⁴ course of a single experimental session.



Figure 3. Preferences change over time

Probability of making the same choice on the two trials with the same item pair, shown as a function of the difference in trial number between them (Δ tr). Trial pairs with identical items (N=1726) were sorted by Δ tr, and the match probabilities were smoothed with a boxcar function with a width of 100 observations.

165 Choice alternatives undergo revaluation

We propose a simple algorithm to characterize how preferences changed over the course of the session.

¹⁶⁷ It assumes that on each decision, the value of the chosen item increases by an amount equal to δ , and ¹⁶⁸ the value of the unchosen item decreases by the same amount (Fig. 4A). We refer to the updated values ¹⁶⁹ as *d*-values, or v_d , where *d* stands for 'dynamic'.

Fig. 4B illustrates how the value of the items changes over the course of the session, for a given value of

 δ , for three snack items. For example, while the item shown with the green curve is initially very valuable, as indicated by its high initial rating, its value decreases over the course of the session each time it was not selected.

¹⁷⁴ We determined the degree of revaluation that best explained the participants' choices. For each ¹⁷⁵ participant, we find the value of δ that minimizes the deviance of a logistic regression model that uses ¹⁷⁶ the *d*-values to fit the choices made on each trial,

$$logit[p_{choice}] = \beta_0 + \beta_1 v_d^{(left)} + \beta_2 v_d^{(right)},$$
(1)

where p_{choice} is the probability of choosing the item that was presented on the right. The *d-values* are initialized to the explicitly reported values for all items, and they are updated by plus or minus δ when an item is chosen or rejected, respectively. Importantly, the updated values only affect future decisions involving the items.

Fig. 4C shows the deviance of the logistic regression model for a representative participant, as a function of δ . For this participant, the best explanation of the choices is obtained with a value of $\delta \approx$ \$0.15. We fit the value of δ independently for each participant to minimize the deviance of the logistic regression



Figure 4. Revaluation algorithm

(A) Schematic example of the revaluation algorithm applied to one decision. After a choice between items A and B, the value of the chosen item is increased by δ and the value of the unchosen item is decreased by the same amount. (B) Example of value changes due to revaluation, for three items, as a function of the presentation number within the session. In the experiment, each item was presented 7 times. (C) For a representative participant, deviance of the logistic regression model that uses the revalued values to explain the choices, for different values of δ . The best fitting value is \sim \$0.15. The inset shows a histogram of the best-fitting δ values across participants.

model fit to the choices. On average, each choice changed the value of the chosen and unchosen items by 0.18 ± 0.016 (mean \pm s.e.m., Fig. 4C, *inset*).

¹⁸⁶ The values derived from the *Reval* algorithm explain the choices better than the explicit value reports.

The choices are more sensitive to variation in Δv_d , evidenced by the steeper slope (Fig. 5A). When Δv_d

and Δv_s are allowed to compete for the same binomial variance, the former explains away the latter. This

assertion is supported by a logistic regression model that incorporates both Δv_s and Δv_d as explanatory

variables (Eq. 7). The coefficient associated with Δv_s is not significantly different from zero while the one

associated with Δv_d remains positive and highly significant (*Figure 5–Figure Supplement 1*).

More surprisingly. Reval allows us to explain the response times better than the explicit value reports. 192 even though RTs were not used to establish the *d-values*. We used the *d-values* to fit a drift-diffusion 193 model to the single-trial choice and response time data, and compared this model with the one that was 194 fit using the s-values (Fig. 5A). To calculate the fraction of RT variance explained by each model, we 195 subtracted from each trial's RT the models' expectation, conditional on Δv_x (with $x \in \{e, r\}$) and choice. 196 The model that relies on the *d-values* explains a larger fraction of variance in RT than the model that 197 relies on the *s-values* (Fig. 5B). This indicates that the re-assignment of values following *Reval* improved 198 the capacity of a *DDM* to explain the response times. 199

The DDM that uses the dynamic values also explains the combined choice-RT data better than the 200 one that uses the static values. We compared their goodness of fit using the Bayesian Information 201 Criteria (BIC), penalizing the DDM that uses the dynamic values for the revaluation update parameter, 202 δ . For all participants, the *DDM* that uses the dynamic values provided a better fit than the *DDM* that 203 uses the static values (Figure 5-Figure Supplement 2A). To control for the possibility that the model 204 comparison is biased by the extra parameter in the dynamic model (δ), we simulated choice and RT 205 data for each participant from the DDM model fit to the static values, and fit these simulated data to the 206 DDMs using static and dynamic values (in the latter case applying the Reval algorithm prior to fitting). 207 For the simulated data, the model comparison favored the DDM using static values for most participants 208 (Figure 5-Figure Supplement 2B), indicating that the additional parameter in the dynamic model does 209



Figure 5. Revaluation explains choice and RT better than explicit values

(A) Proportion of rightward choices (top) and mean response time (bottom) as function of the difference in *d-value* between the two items. The red solid lines are fits of a drift-diffusion model that uses the *d-values*. The dashed line corresponds to the fits of a DDM that uses the *s-values* (same as in Fig. 1C-D). Error bars indicate s.e.m. across trials. Participants are more sensitive to *d-values* than *s-values* (top) and the *d-values* better explain the full range of RTs (bottom). (B) Percentage of variance in response times explained by a *DDM* in which the drift rate depends on either Δv_d (abscissa) or Δv_s (ordinate). Each data point corresponds to a different participant. For most participants, the model based on the dynamic values explained a greater proportion of the variance. (C) *d-values* are better than *s-values* at predicting the difficulty of a decision as reflected in the response times. Data points represent the difference in mean RTs between difficult and easy decisions. Positive values indicate that difficult decisions take longer on average than easy ones. *Difficult* and *easy* are defined relative to the median of the absolute value of Δv_s (left) or Δv_d (right). The lines connect the mean RTs of each participant. P-value is from a paired t-test.

Figure 5-Figure supplement 1. Dynamic values explain away the effect of static values on choice.

Figure 5-Figure supplement 2. Comparison of DDM fits using static and dynamic values.

Figure 5–Figure supplement 3. Similar δ values obtained by *Reval* and logistic regression.

²¹⁰ not strongly bias the model comparison.

The time it takes to make a decision, and the difference in value between the items under comparison, 211 can be considered complementary measures of decision difficulty. On average, the more similar in 212 value the two items are, the longer it would take to commit to a choice. Under this assumption, we can 213 compare how well the static and the dynamic values predict the difficulty of the choices as judged by 214 their response times. The application of Reval revealed that some decisions that were initially considered 215 difficult, because Δv_{e} was small, were actually easy, because Δv_{d} was large, and vice versa. Grouping 216 trials by the Δv_d led to a wider range of mean RTs compared to when we grouped them by Δv_s (Fig. 5C). 217 The effect can also be observed for individual participants. For each participant, we grouped trials into 218 two categories depending on whether the difference in value was less than or greater than the median 219 difference. We then calculated the mean RT for each of the two groups of trials. The difference in RT 220 between the two groups was greater when we grouped the trials using the *d-values* than when we used 221 the s-values. This implies the d-values were better than the s-values at assessing the difficulty of a 222 decision as reflected in the response time. 223

We verified that the improvement in fit was not just due to the additional free parameter (δ). To do this, we again used simulated choices sampled from logistic regression models fit to the participants' choices, as we did for Fig. 2. Because the choices are sampled from logistic functions fit to the choice data, they lead to a psychometric function that is similar to that obtained with the experimental data. We reasoned that if revaluation were an artifact of the analysis method, then applying the revaluation algorithm to these simulated data should lead to values of δ and goodness of fit similar to those of the real data. To the

> contrary, (*i*) the optimal values of δ for the simulated data were close to zero (Fig. 6A); (*ii*) the reduction in deviance after applying *Reval* was negligible compared to the reduction in the actual data (Fig. 6B); and (*iii*) we found no difference in the RT median splits between *s-values* and *d-values* (Fig. 6C). This shows that the improvements in fit quality due to *Reval* are neither guaranteed nor an artifact of the procedure.



Figure 6. No revaluation in simulated data

(A) Histogram of the best-fitting revaluation update (δ) for data simulated by sampling choices from a logistic function fit to the participants' choices. The best-fitting δ values for the simulated choices are centered around 0. For reference, we have also included a histogram of the δ values obtained from the fits to the participants' data, showing all positive values (gray). (B) Deviance of the logistic regression model used to explain the choices (Eq. 1), fit using either the static values (ordinate) or the *Reval* algorithm (abscissa). Each data point corresponds to a different participant. Experimental data are shown in gray and simulated data (as in panel A) are shown in red. The marked reduction in deviance in the experimental data is absent in the data simulated by sampling from logistic regressions fit to the static values. (C) Similar to Fig. 5C, for the simulated data. The values obtained from *Reval* were no better than the static values at explaining the RTs, as expected, since the δ values were ~0 and thus $v_d \approx v_s$.

235 Imperfect value reports do not explain revaluation away

The idea that a choice can induce a change in preference is certainly not new (Festinger, 1957). Choice-236 induced preference change (CIPC) has been documented using a free-choice paradigm (Brehm, 1956), 237 whereby participants first rate several items, and then choose between pairs of items to which they have 238 assigned the same rating, and finally rate the items again. A robust finding is that items that were chosen 239 are given higher ratings and items that were not chosen are given lower ratings relative to pre-choice 240 ratings, leading to the interpretation that the act of choosing changes the preferences for the items under 241 comparison. However, it has been suggested that the CIPC demonstrated with the free-choice paradigm 242 can be explained as an artifact (Chen and Risen, 2010). Put simply, the initial report of value may be a 243 noisy rendering of the true latent value of the item. If two items, A and B, received the same rating but A 244 was chosen over B, then it is likely that the true value for item A is greater than for item B, not because 245 the act of choosing changes preferences, but because the choices are informative about the true values 246 of the items, which are unchanging. 247

We examined whether *Reval* could be explained by the same artifact. We considered the possibility that the items' valuation in the choice phase are static but potentially different from those reported in the ratings phase. If the values are static, but different from those explicitly reported, then *Reval* could still improve choice and RT predictions by revealing the true subjective value of the items.

We reasoned that if values were static, the improvements we observed in the logistic fits when we applied 252 Reval should be the same regardless of how we ordered the trials before applying it. To test this, we 253 applied *Reval* in the direction in which the trials were presented in the experiment, and also in the reverse 254 direction (i.e., from the last trial to the first). If the values were static, then the quality of the fits should 255 be statistically identical in both cases. In contrast, we observed that the variance explained by Reval 256 was greater (i.e., the deviance was lower) when it was applied in the correct order than when it was 257 applied in the opposite order (Fig. 7A; p<0.0001, paired t-test). This rules out the possibility that the 258 values were static. Moreover, the values produced by applying Reval in the reverse direction explained 259 the choices better than the static values (Fig. 7B). This might seem counterintuitive, given that the initial 260 values for the *Reval* algorithm are the *s-values*, which are explicitly reported *before* the main experiment. 261



Figure 7. Reval is sensitive to trial order

(A) Deviance obtained by applying *Reval* to the trials in the order in which they were completed (abscissa) and in the reverse order (ordinate). Each data point corresponds to a different participant. The deviance is greater (i.e., the fits are worse) when *Reval* is applied in the reverse direction. (B) The deviance of the logistic regression model used to explain the choices (Eq. 1), obtained by applying *Reval* in the backward direction (ordinate), is lower than the deviance obtained using the static values (abscissa). Each data point corresponds to a different participant. Experimental data are shown in gray and data simulated from the logistic fits to the static values (as in Fig. 6A-B) are shown in red.

In a later section, we show that this effect stems from the same process that gives rise to revaluation (Is

revaluation a byproduct of deliberation?).

264 Asymmetric value-updating for chosen and unchosen options

So far we have assumed that a choice increases the value of the chosen option by δ and decreases the 265 value of the unchosen option by the same amount. Here, we evaluate the possibility that the degree 266 of revaluation is different for the chosen and unchosen options. We fit a variant of the Reval algorithm 267 with two values of δ , one for the chosen option (δ_{chosen}) and one for the unchosen option ($\delta_{unchosen}$). Fig. 8 268 shows the values that best fit the data for each participant. For each participant, $\delta_{\text{chosen}} > 0$ and $\delta_{\text{unchosen}} < 0$; 269 in other words, the value of the chosen item typically increases, while the value of the unchosen item 270 tends to decrease following a choice. Further, for most participants, the degree of revaluation is greater 271 for the chosen option than for the unchosen option. As we speculate in the discussion, this result may be 272 related to the unequal distribution of attention between the chosen and unchosen items (Krajbich et al., 273 2010). 274

275 Representation of revalued values in the ventromedial prefrontal cortex

Several brain areas, in particular the ventromedial prefrontal cortex (vmPFC), have been shown to 276 represent the value of decision alternatives during value-based decisions (Kennerley et al., 2009; 277 Plassmann et al., 2007; Bartra et al., 2013). Based on our finding that the *d-values* provide a better 278 explanation of the behavioral data than the *s*-values, we reasoned that the *d*-values might explain the 279 BOLD activity in these areas beyond that explained by the s-values. We included both the s-value and the 280 d-value of the chosen item in a whole-brain regression analysis of BOLD activity. This parameterization 281 reveals significant correlation of the BOLD signal in the vmPFC with *d-value*, controlling for *s-value* (Fig. 9 282 and Table S1). In fact, in a separate model that only included s-value, the effect of s-value on BOLD in 283 the vmPFC did not survive correction for familywise error rate at a whole-brain level (Figure 9-Figure 284 Supplement 1 and Table S2 top). In contrast, another model that only included d-value revealed a 285 robust effect of *d-value* on BOLD in vmPFC that survived whole-brain correction (Figure 9-Figure 286 Supplement 1 and Table S2 middle). Finally, to evaluate whether the effect shown in Fig. 9 is not 287 simply captured by the difference in *d-value* and *s-value*, we ran a fourth model that included only 288 (d-value - s-value). The effect of this difference between d-value and s-value on BOLD in vmPFC did 289 not survive whole-brain correction (Figure 9-Figure Supplement 1 and Table S2 bottom). Collectively, 290 these findings provide additional evidence for revaluation, as capturing a meaningful aspect of the data, 291 in the sense that it accounts for the activity of brain areas known to reflect the value of the choice 292 alternatives. 293



Figure 8. Stronger revaluation for the chosen than for the unchosen item

We fit a variant of the *Reval* algorithm that includes separate update values (δs) for the chosen and unchosen options. The best-fitting δ value for the chosen option (abscissa) is plotted against the best-fitting value for the unchosen option (ordinate). Each data point corresponds to one participant. The increase in value for the chosen option is greater than the decrease in value for the unchosen option (paired t-test).



Figure 9. Revaluation reflected in BOLD activity in ventromedial prefrontal cortex

Brain-wide fMRI analysis revealed a significant correlation between *d-values* and activity in the vmPFC, after controlling for s-values. The statistical map was projected onto the cortical surface. Shown here are the medial view of the right and left hemispheres of a semi-inflated surface of a template brain. Heatmap color bars range from z-stat = 3.1 to 3.6. The map was cluster corrected for familywise error rate at a whole-brain level with an uncorrected cluster-forming threshold of z = 3.1 and corrected extent of p < 0.05. The full unthresholded map can be viewed here: https://identifiers.org/neurovault.image:869963.

Figure 9-Figure supplement 1. Representation of *d-value*, *s-value* and their difference in BOLD activity.

Revaluation in other datasets of the food-choice task 294

To assess the generality of our behavioral results, we applied *Reval* to other publicly available datasets. 295

All involve binary choices between food snacks, similar to Bakkour et al. (2019). We analyze data from 296

experiments reported in Folke et al. (2016) and from the two value-based decision tasks reported in 297

Sepulveda et al. (2020). 298

Reval yields results that are largely similar to those observed in the data from Bakkour et al. (2019). 299

The values derived from Reval led to a better classification of choice difficulty than the explicit value 300

reports (Fig. 10A). In all three datasets, the δ values were significantly larger than those obtained from 301

simulated data under the assumption that the values were static and equal to the explicitly reported 302

values (Fig. 10B). Furthermore, the reduction in the deviance resulting from the application of Reval 303

(Eq. 7) was significantly greater than the reduction observed in simulated data (Fig. 10C). [All p-values, 304 derived from two-tailed paired t-tests, are shown in the figure].

305

In the dataset from Folke et al. (2016), the deviance was significantly smaller when Reval was applied in 306

³⁰⁷ the forward than in the backward direction, replicating the result in our main experiment. However, in the

dataset of Sepulveda et al. (2020), no significant difference in deviance was observed (Fig. 10D). We

³⁰⁹ do not know what explains this discrepancy, although we believe that the differences in experimental

design may play a role. In the experiment of Sepulveda et al. (2020), unlike the other two datasets that

we analyzed, participants performed the experiment in two framing conditions: one in which they chose

the item the liked the most, and another one in which the chose the item the disliked the most. These

two conditions alternated in short blocks of 40 trials. This alternation may affect valuation in a way that is

not captured by the *Reval* algorithm. We expand on this in Discussion.

Is revaluation a byproduct of deliberation?

We hypothesize that the sequential dependencies we identified with *Reval* may be a corollary of the process by which values are constructed during deliberation. The subjective value of an item depends on the decision-maker's *mindset*, which may change more slowly than the rate of trial presentations. Therefore, the subjective value of an item on a given trial may be informative about the value of the item the next time it is presented. Subjective values are not directly observable, but choices are informative about the items' value.

We assessed the plausibility of this hypothesis with a bounded evidence accumulation model that includes a parameter that controls the correlation between successive evidence samples for a given item. We call this the *correlated-evidence drift-diffusion model* (*ceDDM*). We assume that the decision is resolved by accumulating evidence for and against the different alternatives until a decision threshold is

326 crossed.

The model differs from standard drift-diffusion, where the momentary evidence is a sample drawn from a 327 Normal distribution with expectation equal to Δv_{z} plus unbiased noise, $\mathcal{N}(0, \sqrt{dt})$. Instead, the value of 328 each of the items evolves separately such that the expectations of its value updates are constructed as a 329 Markov chain Monte Carlo (MCMC) process thereby introducing autocorrelation between successive 330 samples of the unbiased noise (see Methods). Crucially, the correlation is not limited to the duration 331 of a trial but extends across trials containing the same item. When an item is repeated in another trial. 332 the process continues to evolve from its value at the time a decision was last made for or against the 333 item. 334 We fit the model to the data from Bakkour et al. (2019). The model was able to capture the relationship 335

between choice, response time and Δv_s (Fig. 11A). Fig. 11B shows the degree of correlation in the evidence stream as a function of time, for the model that best fit each participant's data. After 1 second of evidence sampling, the correlation was 0.1062 ± 0.0113 (mean \pm s.e.m. across participants). This is neither negligible (which would make the model equivalent to the DDM) nor very high (which would render sequential sampling useless, since it can only average out the noise that is not shared across time).

The assumptions embodied by the *ceDDM* are consistent with the results of the *Reval* analysis. We 342 applied the Reval algorithm to simulated data obtained from the best-fitting ceDDM. The results were in 343 good agreement with the experimental data. The best-fitting δ values were positive for all participants 344 and in a range similar to what we observed in the data (Fig. 11C). Reval increased the range of RTs 345 when trials were divided by difficulty, implying that Reval led to a better classification of easy and difficult 346 decisions (Fig. 11D). Reval applied to the trials in the true order explained the simulated choices better 347 than when applied in the opposite direction (Fig. 11E). This is because the model assumes that when an 348 item first appears, the last sample obtained for that item was the value reported in the ratings phase 349 for that item. As more samples are obtained for a given item, the correlation with the explicit values 350 gradually decreases. Additionally, the values obtained from applying Reval in the backward direction 351 provided a better explanation of the simulated choices than the static values (Fig. 11F), mirroring the 352 pattern observed observed in the behavioral data (Fig. 7B). Taken together, the success of ceDDM 353 implies that the sequential dependencies we identify with Reval may be the result of a value construction 354 process necessary to make a preferential choice. 355

356 Discussion





We applied the *Reval* method to other publicly available datasets of the food choice task. In the experiment of Folke et al. (2016) (first column), participants reported their willingness to pay (WTP) for each of 16 common snack items. In the choice task, they were presented with each unique pair of items and asked to choose the preferred item. Each unique pair was presented twice for a total of 240 trials per participant. In the experiment of Sepulveda et al. (2020) (second and third columns), participants (N=31) reported their willingness to pay (WTP) for each of 60 snack items. They were then presented with pairs of items from which to choose. Pairs were selected based on participants' WTP reports to provide comparisons between pairs of high-value, low-value and mixed-value items. The choice task was performed under two framing conditions: *like-framing*, selecting the more preferred item, and *dislike framing*, selecting the less preferred item. The task consisted of six alternating blocks of *like-* and *dislike-framing* (40 trials per block). (A) RT difference between *easy* and *difficult* trials, determined as a median split of $|\Delta v|$. Same analysis as in Fig. 5C. (B) Histogram of the best-fitting revaluation update (δ) for data simulated by sampling choices from a logistic function fit to the participant's choices (red), and for the actual data (gray). Same analysis as in Fig. 6A. (C) Comparison of the deviance with and without *Reval*. Same analysis as in Fig. 6A. (D) Comparison of the deviance applying *Reval* in the forward and backward directions. Same analysis as in Fig. 7A. All p-values shown in the figure are from paired t-tests.





A drift-diffusion model with non-independent noise (*ceDDM*) captures the main features of revaluation. (A) The *ceDDM* accounts for choices (top) and response times (bottom), plotted as a function of the difference in values obtained from explicit reports (Δv_s). Same data as in Fig. 1C-D. Red curves are simulations of the best-fitting model. Each trial was simulated 100 times. Simulations were first averaged within trials and then averaged across trials. Error bars and bands indicate s.e.m. across trials. (B) Noise correlations as a function of time lag, obtained from the best-fitting model. Each curve corresponds to a different participant. (C) δ parameters derived by applying *Reval* to simulated data from the best fitting *ceDDM* model to each participant's data. As in the data, $\delta > 0$ for all participants. (D) Similar analysis as in Fig. 5C applied to simulations of the *ceDDM*. As for the data, *Reval* increased the range of RTs obtained after grouping trials by difficulty (by *s-values* on the left and *d-values* on the right; p-value from paired t-test). (E) Similar analysis to that of Fig. 7A, using the simulated data. As observed in the data, the deviance resulting from applying *Reval* in the correct trial order (abscissa) is smaller than when applied in the opposite order (p-value from paired t-test). (F) Similar analysis to that of Fig. 7B, using the simulated data.

357 Sequential dependencies and choice-induced preference change

We identified sequential dependencies between choices in a value-based decision task. Participants performed a task in which they had to make a sequence of choices among a limited set of items. The best explanation for future choices was obtained by assuming that the subjective value of the chosen item increases and the value of the unchosen item decreases after each decision. Evidence for revaluation was obtained by analyzing the probability that participants make the same decision in pairs of trials with

- identical options. We also identified revaluation using an algorithm we call *Reval*. The same algorithm allowed us to identify revaluation in other datasets obtained with the food-choice task (Folke et al., 2016;
- 365 Sepulveda et al., 2020).

The sequential effects we identified can be interpreted as a manifestation of choice-induced preference 366 change. The usual paradigms for detecting the presence of CIPCs are based on the comparison of 367 value ratings reported before and after a choice (for a review see Izuma and Murayama, 2013; Enisman 368 et al., 2021). After a difficult decision, the rating of the chosen alternative often increases and that 369 of the rejected alternative often decreases—an effect termed the "spreading of alternatives". Many 370 variants of the free choice paradigm have been developed to control for or eliminate the statistical artifact 371 reported by Chen and Risen (2010). One common approach is to compare the "spreading of alternatives" 372 observed in the free-choice paradigm (rate-choose-rate, or RCR) with a control task in which a different 373 set of participants rate the items twice before the choice phase (RRC). Any spread observed in the RRC 374 condition cannot be explained by the CIPC, since in the RRC condition there is no choice between the 375 two rating phases. The CIPC is measured indirectly, as the difference in the spread of the alternatives 376 between the RCR and the RRC. Other approaches involve asking participants to rate an item that they 377 are led to believe they have chosen, when in fact they have not (Sharot et al., 2010; Johansson et al., 378

2014). Any change in ratings cannot be due to the information provided by a choice, since no real choice
 was made. In addition to the complications introduced by deceiving the participants (e.g., participants
 may suspect the deception but not mention it to the experimenter), the elimination of a real choice
 prevents these paradigms from being used to study the process through which subjective values undergo

³⁸³ revision during decision formation.

In contrast, our approach to identify changes in value does not require pre- and post-choice ratings. 384 Instead, it requires a sequence of trials in which the same items are presented multiple times (as in 385 Luettgau et al., 2020). The revaluation effect we find cannot be explained by the artifact identified by 386 Chen and Risen (2010). Using trials with identical items, we show that the nearer in time the trials with 387 identical items are to each other, the more likely people are to choose the same option. Further, the 388 revaluation algorithm explains choices better when applied in the order in which the trials were presented 389 than when applied in the reverse order. These observations are inconsistent with the notion that item 390 values are fixed (i.e., do not change) during the experiment, regardless of whether values are the same 391 or different from those reported during the rating phase. 392

Revaluation during of after deliberation?

We cannot determine with certainty whether the revaluation occurs after the decision or during the 394 deliberation process leading up to the decision. At face value, it might seem that *Reval* implements 395 change after each decision (Festinger, 1957). Yet, Reval simply identifies a change in value, which may 396 well occur during the deliberation leading to the decision, perhaps owing to a comparison of other items 397 (on other trials) that happen to suggest a dimension of comparison that increases in importance on the 398 current trial (Lee and Daunizeau, 2020; Lichtenstein and Slovic, 2006). More broadly, the subjective 399 value of an option depends on the *mindset* of the decision maker. This internal state, which in the 400 food-choice task includes aspects such as degree of satiety or sugar craving, can vary over time, causing 401 the value of the items to vary as well. If changes in *mindset* are slow-that is, lasting longer than the 402 duration of a decision-then the value of items will be correlated over time. 403

We proposed a decision model (ceDDM) in which evidence samples are correlated over time. Fitting the 404 model to account for each participant's choices and response times produces a revaluation of magnitude 405 similar to what we observed experimentally. It also predicts that applying Reval in the direction in which 406 the trials were presented explains the choices better than applying it in the opposite direction, as we 407 observed in the data. This modeling exercise suggests that the CIPC-like effects we identified may be 408 due to processes that occur during the deliberation leading up to a choice, rather than post-decision 409 processes that attempt to reduce cognitive dissonance. To be clear, we interpret the ceDDM only as a 410 proxy for a variety of more nuanced processes. If the *mindset* endures many individual decisions, the 411 subjective value of an item will be correlated over time. While the *ceDDM* captures only a small aspect 412 of this complex process, it has allowed us to explain the sequential dependencies we identified with 413 Reval. 414

The *ceDDM* belongs to a class of sequential sampling models in which the drift rate varies over time. 415 Such models have already been studied in the context of value-based decisions. For example, in 416 the attentional drift-diffusion model (Kraibich et al., 2010), the drift rate varies depending on which 417 item is attended, as if the value of the unattended items are discounted by a multiplicative factor. In 418 Dynamic Field Theory (Busemever and Townsend, 1993), the drift rate varies depending on which 419 attribute is attended. Recently, Lee and Pezzulo (2022) showed that a sequential sampling model in 420 which the drift rate varies over time can explain the 'spreading of alternatives' (SoA) characteristic of 421 choice-induced preference change. Lee and Pezzulo (2022) propose that the initial rating of the items 422 may be constructed using only the most salient attributes of each item, while in a difficult decision 423 more attributes may be considered, leading to a revaluation that informs the rating reported after the 424 decision phase (see also Voigt et al., 2019). Consistent with our proposal, Lee and Pezzulo (2022) 425 argue that thinking about non-prominent features during decision-making increases the likelihood that 426 these features will be recalled when evaluating options in subsequent instances. 427

428 More revaluation for the chosen than the unchosen item

⁴²⁹ We observed that the degree of revaluation was higher for the chosen item than for the unchosen item.

430 This was revealed by a variant of the Reval algorithm in which we allowed both items to have different

⁴³¹ updates. We speculate that this difference can be explained by the asymmetric distribution of attention ⁴³² between the chosen and unchosen items. It is known that the chosen item is looked at longer than the

unchosen item (Krajbich et al., 2010). Further, CIPC is more likely for items that are remembered to

have been chosen or unchosen (Salti et al., 2014). So one possibility is that the revaluation is larger for

the chosen than for the unchosen item because participants spent more time looking at the chosen item

and thus are more likely to remember it, leading to a larger change in value (Voigt et al., 2019).

Another possibility derives from the constructive view of preferences and the potential role of attention 437 in decision-making. It is often assumed that value-based decisions involve gathering evidence from 438 different alternatives, and that more evidence is gathered from alternatives that are attended to for longer 439 (Callaway et al., 2021; Li and Ma, 2021; Krajbich et al., 2010). In the ceDDM, the correlation in value for a 440 given item decreases with the number of evidence samples collected from the item (Fig. 11B). Therefore, 441 the more that attention is focused on a given item, the greater the difference between the item's value 442 before and after the decision. Because chosen items are attended to for longer than unchosen items 443 (e.g., Kraibich et al., 2010), the chosen item should exhibit larger revaluation than the unchosen one. 444 which is what we observed in the data (Fig. 8). 445

446 Limitations of our study

One limitation of our study is that we only examined tasks in which static values were elicited from 447 explicit reports of the value of food items. It remains to be determined if other ways of eliciting subjective 448 values (e.g., Jensen and Miller, 2010) would lead to similar results. We think so, as the analysis of trials 449 with identical item pairs (Fig. 3) and the difference between forward and backward Reval (Fig. 7A) are 450 inconsistent with the notion that values are static, regardless of their precise value. It also remains to be 451 determined if our results will generalize to non-food items whose value is less sensitive to satiety and 452 other dynamic bodily states. Perceptual decisions also exhibit sequential dependencies, and it remains 453 to be explored whether these can be explained as a process of value construction, similar to what we 454 propose here for the food-choice task (Gupta et al., 2024; Cho et al., 2002; Zylberberg et al., 2018; 455 Abrahamvan et al., 2016). 456

Another limitation of our study is that, in one of the datasets we analyzed (Sepulveda et al., 2020). 457 applying *Reval* in the forward direction was no better than applying it in the backward direction (Fig. 10) 458 We speculate that this failure is related to idiosyncrasies of the experimental design, in particular, the 459 use of alternating blocks of trials with different instructions (select preferred vs. select non-preferred). 460 More importantly, Reval applied in the backward direction led to a significant reduction in deviance 461 relative to that obtained using the static values (Fig. 7B). This reduction was also observed in the ceDDM. 462 suggesting that the effect may be explained by changes in valuation during deliberation. However, 463 we cannot discard a contribution from other, non-dynamic changes in valuation between the rating 464 and choice phase including contextual effects (Lichtenstein and Slovic, 2006), stochastic variability in 465 explicit value reporting (Polanía et al., 2019), and the limited range of numerical scales used to report 466 value. 467

Finally, we emphasize that the *ceDDM* should be interpreted as a proof-of-principle model used to 468 illustrate how stochastic fluctuations in item desirability can explain many of our results. We chose to 469 model value changes following an MCMC process. However, other stochastic processes or other ways of 470 introducing sequential dependencies (e.g., variability in the starting point of evidence accumulation) may 471 also explain the behavioral observations. Furthermore, there likely are other ways to induce changes in 472 the value of items other than through past decisions. For example, attentional manipulations or other 473 experiences (e.g., actual food consumption) may change one's preference for an item. The current 474 version of the ceDDM does not allow for these influences on value, but we see no fundamental limitation 475 to incorporating them in future instantiations of the model. 476

477 Concluding remarks

⁴⁷⁸ Our research contributes to a growing body of work exploring the impact of memory on decision-making ⁴⁷⁹ and preference formation (Biderman et al., 2020), and in particular to the CIPC. It has been suggested ⁴⁸⁰ that the retrieval of an item's value during decision-making renders it susceptible to modification, leading

to a revaluation that influences subsequent valuations through a process that has a neural correlate in the

482 hippocampus (Luettgau et al., 2020). The link between memorability and preference is also supported

by experiments in which the presentation of an item coincides with an unrelated rapid motor response 483 that increases subsequent preference for the item (Botvinik-Nezer et al., 2021) and by experiments 484 demonstrating that people prefer items to which they have previously been exposed (Zajonc, 1968). As 485 in these studies, ours also highlights the role of memory in revaluation. Due to the associative nature 486 of memory, successive evidence samples are likely to be dependent (Rhodes and Turvey, 2007). A 487 compelling illustration of this effect was provided by Elias Costa and colleagues (Elias Costa et al., 488 2009). Participants were asked to report the first word that came to mind when presented with a word 489 generated by another participant, which was then shown to yet another participant. The resulting chain 490 resembled Lévy flights in semantic space, characterized by mostly short transitions to nearby words 491 and occasional large jumps. Similar dynamic processes have been used to describe eve movements 492 during visual search (Bella-Fernández et al., 2021) and the movement of animals during reward foraging 493 (Brown et al., 2007; Hills et al., 2015). It is intriguing to consider that a similar process may describe how 494 decision-makers search their memory for evidence that bears on a decision. 495

496 Methods

497 Food choice task

A total of 30 participants completed the snack task, which consisted of a rating and a choice phase. The
 experimental procedures were approved by the Institutional Review Board (IRB) at Columbia University,
 and participants provided signed informed consent before participating in the study. The data were
 previously published in Bakkour et al. (2019).

Rating Phase. Participants were shown a series of snack items in a randomized order on a computer 502 screen. They indicated their willingness to pay (WTP) by using the computer mouse to move a cursor 503 along an analog scale ranging from \$0 to \$3 at the bottom of the screen. The process was self-paced, and 504 each snack item was presented one at a time. After completing the ratings for all 60 items, participants 505 were given the opportunity to revise their ratings. The 60 items were re-displayed in random order, with 506 the original bids displayed below each item. Participants either chose to keep their original bid by clicking 507 "NO" or to revise the bid by clicking "YES." which re-displayed the analog scale for bid adjustment. We 508 take the final WTP that is reported for each item as the corresponding *explicit* value (*s-value*). 509

Choice phase. From the 60 rated items, 150 unique pairs were formed, ensuring variation in Δv_{a} . Each 510 of the 60 items was included in five different pairs. The 60 item pairs were presented twice, resulting in 511 a total of 210 trials per participant. Item pairs were presented in random order, with one item on each 512 side of a central fixation cross. Participants were instructed to select their preferred food item and were 513 informed that they would receive their chosen food from a randomly selected trial to consume at the 514 end of the experiment. The task took place in an MRI scanner. Participants indicated their choice on 515 each trial by pressing one of two buttons on an MRI-compatible button box. They had up to 3 seconds to 516 make their choice. Once a choice was made, the chosen item was highlighted for 500 ms. Trials were 517 separated by an inter-trial interval (ITI) drawn from a truncated exponential distribution with a minimum 518 ITI of 1 and a maximum ITI of 12 seconds. The resulting distribution of ITIs across trials had a true mean 519 of 3.05 seconds and a standard deviation of 2.0 seconds. 520

521 Data analysis

Association between the *s*-values, choice and RT. We used the following logistic regression model to evaluate the association between the *s*-values and the probability of choosing the item on the right:

 $\text{logit}[p_{\text{right}}] = \sum_{i=1}^{N_{\text{subj}}} \beta_{0,i} I_i + \beta_1 \Delta v_s \quad ,$

where I_i is an indicator variable that takes the value 1 if the trial was completed by subject i and 0

otherwise. We used a t-test to evaluate the hypothesis that the corresponding regression coefficient is

⁵²⁷ zero, using the standard error of the estimated regression coefficient.

Similarly, we used a linear regression model to test the influence of Δv_s on response times:

$$RT = \sum_{i=1}^{N_{subj}} \beta_{0,i} I_i + \beta_1 |\Delta v_s| + \beta_2 \Sigma v_s \quad ,$$
(3)

(2)

- see where $|\cdot|$ denotes absolute value and Σv_s is the sum of the value of the two items presented on each
- trial. The last term was included to account for the potential influence of value sum on response time
- 531 (Smith and Krajbich, 2019).

Predicting choices in *cynosure* trials. We used two logistic regression models to predict the choice
 in each trial using observations from the other trials. We refer to the trial under consideration as the
 cynosure trial (Fig. 2). One model uses the explicitly reported values:

$$logit[p_{right}] = \beta_0 + \beta_1 \Delta v_s \quad , \tag{4}$$

⁵³⁵ while the other model uses the choices made on other trials:

$$logit[p_{right}] = \beta_0 + \sum_{i=1}^{N_{items}} \beta_i f(i) \quad , \tag{5}$$

536 where

$$f(i) = \begin{cases} 1 & \text{if item } i \text{ is on the right} \\ -1 & \text{if item } i \text{ is on the left} \\ 0 & \text{otherwise} \end{cases}$$
(6)

⁵³⁷ For this model, we included an L2 regularization with $\lambda = 0.5$. Both models were fit independently for

each participant. We only included trials with the first appearance of each item pair (i.e., we did not
 include the repeated trials) so that the choice prediction for the *cynosure* trial is not influenced by the

choice made in the paired trial containing the same items as in the *cynosure* trial.

541 Association between *d-values* and choice. We tested the association between *d-values* and choice with

a logistic regression model fit to the choices. We included separate regressors for Δv_d and Δv_s :

$$logit[p_{right}] = \beta_0 + \beta_s \Delta v_s + \beta_d \Delta v_d \tag{7}$$

The model was fit separately for each participant. *Figure 5–Figure Supplement 1* shows the regression coefficients associated with Δv_s and Δv_d .

Choice and response time functions. When plotting the psychometric and chronometric functions (e.g., Fig. 1C-D), we binned trials depending on the value of Δv_s (or Δv_d). The bins are defined by the following edges: { $-\infty$, -1.5, -0.75, -0.375, -0.1875, -0.0625, 0.0625, 0.1875, 0.375, 0.75, 1.5, ∞ }. We averaged the choice or RT for the trials (grouped across participants) within each bin and plotted them aligned to the mean Δv_x of each bin.

Match probability. We used logistic regression to determine if the probability of giving the same
 response to the pair of trials with identical stimuli depended on the number of trials in between (Fig. 3).
 The model is:

$$logit[p_{match}] = \sum_{i=1}^{N_{subj}} \beta_{0,i} I_{i} + \sum_{i=1}^{N_{subj}} \beta_{1,i} I_{i} |\Delta v_{s}| + \beta_{2} \left(T_{2nd} - T_{1st} \right)$$
(8)

where p_{match} is the probability of choosing the same item on both occasions, I_i is an indicator variable that takes a value of 1 if the pair of trials correspond to subject *i*, and zero otherwise, and T_{1st} and T_{2nd} are the trial number of the first and second occurrences of the same pair, respectively. We used a t-test to evaluate the hypothesis that $\beta_2 = 0$ (i.e., that the separation between trials with identical stimuli had no effect on p_{match} .

558 Drift-diffusion model

We fit the choice and RT data with a drift-diffusion model. It assumes that the decision variable, x, is given by the accumulation of signal and noise, where the signal is a function of the difference in value between the items, Δv , and the noise is equal to \sqrt{dt} , where dt is the time step, such that the accumulated noise after 1 second of unbounded accumulation, the variance of the accumulated noise is equal to 1. The decision variable follows the difference equation,

$$x_{t+1} = x_t + \kappa \ dt \ (\mu + \mu_0) + \sqrt{dt} \ \eta_t \quad , \tag{9}$$

- where η_{i} is sampled from a normal distribution with a mean 0 and variance 1, κ is a signal-noise parameter. 564
- μ is the drift rate and μ_0 is a bias coefficient that is included to account for potential asymmetries between 565
- right and left choices. 566
- We assume that the drift rate is a (potentially nonlinear) function of Δv_{x} . We parameterize this relationship 567 as a power law, so that 568

$$\mu = \operatorname{sign}(\Delta v_x) |\Delta v_x|^{\gamma} \quad , \tag{10}$$

- where sign is the sign operation, || indicates absolute value, and γ is a fit parameter. 569
- The decision terminates when the accumulated evidence reaches an upper bound, signaling a rightward 570
- choice, or a lower bound, signaling a leftward choice. The bound is assumed to collapse over time. It is 571 constant until time d, and then it collapses at rate a:
- 572

$$B(t) = \pm \begin{cases} B_0 & \text{if } t < d \\ B_0 \exp^{-a(t-d)} & \text{otherwise.} \end{cases}$$
(11)

- Collapsing bounds are needed to explain why choices that are consistent with the value ratings are 573 usually faster than inconsistent choices for the same Δv_x . 574
- The response time is the sum of the the decision time, given by the time taken by the diffusing particle to 575 reach of the bounds, and a non-decision time which is assumed to be normally distributed with mean μ_{ud} 576 and standard deviation σ_{nd} . 577
- The model has 8 parameters: { κ , B_0 , a, d, γ , μ_0 , μ_{nd} , σ_{nd} }. The standard deviation of the non-decision times 578
- (σ_{nd}) was fixed to 0.05 s. For the fits shown in Fig. 1C-D and Fig. 5A, we fit the model to grouped data from 579
- all participants. For the analysis of variance explained (Fig. 5) and model comparison (Figure 5-Figure 580
- Supplement 2), we fit the model separately for each participant. The model was fit to maximize the log 581
- of the likelihood of the parameters given the single-trial choice and RT: 582

$$\log L(\text{parameters}) = \sum_{i=1}^{n_{\text{trials}}} \log \left(p\left(\text{choice}^{(i)}, \text{RT}^{(i)} | \Delta v^{(i)}, \text{parameters} \right) \right).$$
(12)

We evaluate the likelihood by numerically solving the Fokker-Planck (FP) equation that described the 583

dynamics of the drift-diffusion process, using the Chang-Cooper fully-implicit method (Chang and Cooper, 584

1970; Kiani and Shadlen, 2009; Zylberberg et al., 2016). For computational considerations, we bin

the values of Δv_{μ} to multiples of \$0.1. From the numerical solution of the FP equation, we obtain the 586 distribution of decision times, which is convolved with the truncated Gaussian distribution of non-decision 587

- latencies. The truncation ensures that the non-decision times are non-negative, which could otherwise 588
- occur during the optimization process for large values of σ_{ud} . The parameter search was performed 589
- using the Bayesian Adaptive Direct Search (BADS) algorithm (Acerbi and Ma, 2017). 590

Revaluation algorithm 591

The Reval algorithm was applied to each participant independently. The values are initialized to those 592 reported during the ratings phase. They are then revised, based on the outcome of each trial, in the 593 order of the experiment. The value of the chosen item is increased by δ and the value of the unchosen 594 item is decreased by the same amount. The revaluation affects future decisions in which the same item 595

is presented. 596

We searched for the value of δ^* that minimizes the deviance of the logistic regression model specified by 597 Eq. 1. The model's deviance is given by:

$$DEV = \sum_{i=1}^{N_{tr}} 2 \log_{e} \left(\frac{1}{\hat{c}_{i}}\right)$$
(13)

- where the sum is over trials and \hat{c}_i is the probability assigned to the choice on trial *i* obtained from the 590 best-fitting logistic regression model. 600
- We complemented this iterative algorithm with a second approach that estimates δ^* using the history 601 of choices preceding each trial. Nearly identical δ values are derived using a single logistic regression 602

model in which the binary choice made on each trial depends on the number of times each of the two
 items was selected and rejected on previous trials. The model is:

$$logit[p_{right}] = \sum_{i=1}^{N_{subj}} \beta_{0,i}I_i + \sum_{i=1}^{N_{subj}} \beta_{1,i}I_i \Delta v_s + \sum_{i=1}^{N_{subj}} \beta_{2,i}I_i \Delta_{ch}$$
(14)

where, as before, I_i is an indicator variable that takes a value of 1 if the trial was completed by subject *i* and 0 otherwise. The key variable is Δ_{ch} . It depends on the number of past trials in which the item presented on the right in the current trial was chosen (n_{ch}^{right}) and not chosen (n_{-ch}^{right}) , and similarly, the number of past trials in which the item presented on the left in the current trial was chosen (n_{ch}^{left}) and not chosen (n_{-ch}^{left}) :

$$\Delta_{ch} = n_{ch}^{\text{right}} - n_{\neg ch}^{\text{right}} + n_{\neg ch}^{\text{left}} - n_{ch}^{\text{left}}.$$
(15)

⁶¹⁰ The variable Δ_{ch} represents the influence of past choices. The signs in Eq. 15 are such that a positive ⁶¹¹ (negative) value of Δ_{ch} indicates a bias toward the right (left) item. To obtain the δ^* in units equivalent to ⁶¹² those derived with *Reval*, we need to divide the regression coefficient $\beta_{2,i}$ by the sensitivity coefficient $\beta_{1,i}$, ⁶¹³ separately for each subject *i*. As can be seen in *Figure 5–Figure Supplement 3*, the values obtained ⁶¹⁴ with this method are almost identical to those obtained with the *Reval* algorithm.

615 Correlated-evidence DDM

The model assumes that at each moment during the decision-making process, the decision-maker can only access a noisy sample of the value of each item. These samples are normally distributed, with parameters such that their unbounded accumulation over one second is also normally distributed with a mean equal to κv_s , where v_s is the explicit value reported during the Ratings phase and κ is a measure of signal-to-noise, and a standard deviation equal to 1.

Crucially, for each item, the noise in successive samples is correlated. To generate the correlated 621 samples, we sample from a Markov chain using the Metropolis-Hastings algorithm (Chib and Greenberg, 622 1995). The target distribution is the normally distributed value function described in the previous 623 paragraph. The proposal density is also normally distributed. Its width determines the degree of 624 correlation between consecutive samples. Typically, the correlation between successive samples is 625 considered a limitation of the Metropolis-Hastings algorithm. Here, however, it allows us to generate 626 correlated samples from a target distribution. The standard deviation of the proposal density is \sqrt{dt}/τ . 627 Higher values of τ result in a narrower proposal density, hence more strongly correlated samples. We 628 sample from the same Markov chain across different trials in which the same item is presented, so that 629 the last sample obtained about an item in a given trial is the initial state of the Markov chain the next 630 time the item is presented. 631 At each moment (dt = 40ms), we sample one value for the left item and another for the right item. 632

⁶³² or the control of the right terms, ⁶³³ compute their difference (right minus left), and accumulate this difference until it crosses a threshold at ⁶³⁴ $+B_0$, signaling a rightward choice, or at $-B_0$, signaling a leftward choice. The decision time is added to ⁶³⁶ the control of the control

the non-decision time, μ_{nd} , to obtain the response time.

We fit the model to the data as follows. For each item, we simulate many Markov chains. In each trial, *i*, we take samples from each chain until the accumulation of these samples reaches one of the two decision thresholds. Then we calculate the likelihood (*L*) of obtaining the choice and the RT displayed by the participant on that trial as:

$$L(\text{choice}_{i}, \text{RT}_{i}) = \frac{1}{N} \sum_{j=1}^{N} L_{j}(\text{choice}_{i}, \text{RT}_{i})$$

$$L_{j}(\text{choice}_{i}, \text{RT}_{i}) = \mathbb{1}_{i,j} \mathcal{N}(\text{RT}_{i}|\text{RT}_{i}^{(j)}, \sigma_{\text{nd}})$$
(16)

where N = 1,000 is the number of Markov chains, 1 is an indicator function that takes the value 1 if the choice made on chain *j* is the same as the choice made by the participant on trial *i* and 0 otherwise, $\mathcal{N}(x|y,z)$ is the normal probability density function with mean *y* and standard deviation *z* evaluated at *x*, and σ_{nd} is a parameter fit to the data.

⁶⁴⁴ When an item is presented again in a future trial, the initial state of each Markov chain depends on ⁶⁴⁵ the state it was in the last time the item was presented. The initial state of each chain is obtained by

- sampling 1,000 values (one per chain) from the distribution given by the final state of each chain. The sampling is weighted by the value of L_j of each chain (Eq. 16), so that chains that better explained the choice and RT in the last trial are more likely to be sampled from in future trials.
- The model has 5 parameters per participant: { κ , B_0 , τ , μ_{nd} , σ_{nd} }, which were fit to maximize the sum, across trials, of the log of *L* using BADS (Acerbi and Ma, 2017).
- The correlations in Fig. 11B were generated using the best-fitting parameters for each participant to simulate 100,000 Markov chains. We generate Markov chain samples independently for the left and right items over a 1-second period. To illustrate noise correlations, the simulations assume that the static value of both the left and right items is zero. We then calculate the difference in dynamic value (x) between the left and right items at each time (t) and for each of the Markov chains (i). Pearson's correlation is computed between these differences at time zero, $x_i(t=0)$, and at time $x_i(t=\tau)$, for different time lags τ . Correlations were calculated independently for each participant. Each trace in Fig. 11B
- ⁶⁵⁸ represents a different participant.

659 fMRI analysis

Acquisition. Imaging data were acquired on a 3T GE MR750 MRI scanner with a 32-channel head coil. 660 Functional data were acquired using a T2*-weighted echo planar imaging sequence (repetition time (TR) 661 = 2 s, echo time (TE) = 22 ms, flip angle (FA) = 70° , field of view (FOV) = 192 mm, acquisition matrix 662 of 96 x 96). Forty obligue axial slices were acquired with a 2 mm in-plane resolution positioned along 663 the anterior commissure-posterior commissure line and spaced 3 mm to achieve full brain coverage. 664 Slices were acquired in an interleaved fashion. We acquired three runs of the food choice task, each 665 composed of 70 trials. Each of the food choice task functional runs consisted of 212 volumes and lasted 666 7 minutes. In addition to functional data, a single three-dimensional high-resolution (1 mm isotropic) 667 T1-weighted full-brain image was acquired using a BRAVO pulse sequence for brain masking and image 668 registration. 669

Preprocessing. Raw DICOM files were converted into Nifti file format and organized in the Brain
 Imaging Data Structure (BIDS) using dcm2niix (Li et al., 2016). Results included in this manuscript come
 from preprocessing performed using *fMRIPrep* 22.1.1 (Esteban et al. (2018b); Esteban et al. (2018a);
 RRID:SCR_016216), which is based on *Nipype* 1.8.5 (Gorgolewski et al. (2011); Gorgolewski et al.
 (2018); RRID:SCR 002502).

Anatomical data preprocessing. The T1-weighted (T1w) image was corrected for intensity non-675 uniformity (INU) with N4BiasFieldCorrection (Tustison et al., 2010), distributed with ANTs 2.3.3 676 (Avants et al., 2008, RRID:SCR 004757), and used as T1w-reference throughout the workflow. The 677 T1w-reference was then skull-stripped with a *Nipvpe* implementation of the antsBrainExtraction.sh 678 workflow (from ANTs), using OASIS30ANTs as target template. Volume-based spatial normaliza-679 tion to one standard space (MNI152NLin2009cAsym) was performed through nonlinear registration 680 with antsRegistration (ANTs 2.3.3), using brain-extracted versions of both T1w reference and the 681 T1w template. The following template was selected for spatial normalization: ICBM 152 Nonlinear 682 Asymmetrical template version 2009c [Fonov et al. (2009), BRID:SCR 008796; TemplateFlow ID: 683 MNI152NLin2009cAsyml. 684 Functional data preprocessing. For each of the 3 BOLD runs per subject, the following preprocessing 685 was performed. First, a reference volume and its skull-stripped version were generated using a custom 686

methodology of *fMRIPrep*. Head-motion parameters with respect to the BOLD reference (transforma-687 tion matrices, and six corresponding rotation and translation parameters) are estimated before any 688 spatiotemporal filtering using mcflirt (FSL 6.0.5.1:57b01774, Jenkinson et al., 2002). The BOLD 689 time-series (including slice-timing correction when applied) were resampled onto their original, native 690 space by applying the transforms to correct for head-motion. These resampled BOLD time-series will be 691 referred to as preprocessed BOLD in original space, or just preprocessed BOLD. The BOLD reference 692 was then co-registered to the T1w reference using mri_coreg (FreeSurfer) followed by flirt (FSL 693 6.0.5.1:57b01774, Jenkinson and Smith, 2001) with the boundary-based registration (Greve and Fischl. 694 2009) cost-function. Co-registration was configured with six degrees of freedom. Several confounding 695 time-series were calculated based on the preprocessed BOLD: framewise displacement (FD) and 696 DVARS. FD was computed using two formulations following Power (absolute sum of relative motions, 697

Power et al. (2014)) and Jenkinson (relative root mean square displacement between affines, Jenkinson et al. (2002)). FD and DVARS are calculated for each functional run, both using their implementations in

Nipype (following the definitions by Power et al., 2014). The head-motion estimates calculated in the

correction step were also placed within the corresponding confounds file. The confound time series were

derived from head motion estimates (Satterthwaite et al., 2013). Frames that exceeded a threshold of
 0.5 mm FD or 1.5 standardized DVARS were annotated as motion outliers. The BOLD time-series were

703 0.5 mm FD or 1.5 standardized DVARS were annotated as motion outliers. The BOLD time-series were 704 resampled into standard space, generating a preprocessed BOLD run in MNI152NLin2009cAsym space.

First, a reference volume and its skull-stripped version were generated using a custom methodology

⁷⁰⁶ of *fMRIPrep*. All resamplings can be performed with *a single interpolation step* by composing all the

pertinent transformations (i.e. head-motion transform matrices, susceptibility distortion correction when

available, and co-registrations to anatomical and output spaces). Gridded (volumetric) resamplings were

709 performed using antsApplyTransforms (ANTs), configured with Lanczos interpolation to minimize the

⁷¹⁰ smoothing effects of other kernels (Lanczos, 1964).

711 Many internal operations of *fMRIPrep* use *Nilearn* 0.9.1 (Abraham et al., 2014, RRID:SCR_001362),

mostly within the functional processing workflow. For more details of the pipeline, see the section corresponding to workflows in *fMRIPrep*'s documentation.

Analysis. We conducted a GLM analysis to look at BOLD activity related to *d-values*, *s-values*, and the difference between the two. We ran four separate models.

Main fMRI Model included five regressors: (i) onsets for all valid trials, modeled with a duration equal to
 the average RT across all valid choices and participants; (ii) same onsets and duration as (i) modulated
 by RT demeaned across these trials within each run for each participant; (iii) same onsets and duration

719 as (i) but modulated by the s-value of the chosen item demeaned across trials within each run for

each participant; (iv) same onsets and duration as (i) but modulated by the *d-value* of the chosen item

demeaned across these trials within each run for each participant; (v) onsets for missed trials. The map

⁷²² in Fig. 9 was generated using this model.

fMRI Model of s-value only included four regressors; all but regressor *(iv)* in *Main fMRI Model*. The map in *Figure 9–Figure Supplement 1* top was generated using this model.

⁷²⁵ *fMRI model of d-value only* included four regressors; all but regressor *(iii)* in *Main fMRI Model*. The map ⁷²⁶ in *Figure 9–Figure Supplement 1* middle was generated using this model.

⁷²⁷ *fMRI model of d-value – s-value only* included four regressors; regressors (*i*) and (*ii*) were the same as

in Main fMRI Model, regressor (iii) had the same onsets and duration as (i) but modulated by (d-value -

s-value) of the chosen item demeaned across trials within each run for each participant, and regressor
 (*iv*) included onsets for missed trials. The map in *Figure 9–Figure Supplement 1* bottom was generated

⁷³¹ using this model.

All four models included the six x, y, z translation and rotation motion parameters, FD, DVARS, and motion outliers obtained from textitfmriprep (described above) as confound regressors of no interest. All regressors were entered at the first level of analysis, and all (except the added confound regressors) were convolved with a canonical double-gamma hemodynamic response function. The time derivative of each regressor (except the added confounding regressors) was included in the model. No orthogonalization between regressors was performed. Models were estimated separately for each participant and run.

GLMs were estimated using FSL's FMRI Expert Analysis Tool (FEAT). The first-level time-series GLM analysis was performed for each run per participant using FSL's FILM. The first-level contrast images were then combined across runs per participant using fixed effects. The group-level analysis was performed using FMRIB's Local Analysis of Mixed Effects (FLAME1) (Beckmann et al., 2003). Grouplevel maps were corrected to control the family-wise error rate using cluster-based Gaussian random

field correction for multiple comparisons, with an uncorrected cluster-forming threshold of z=3.1 and

⁷⁴⁵ corrected extent threshold of p < 0.05.

746 Author contributions

- The data were collected and published by Bakkour et al. (2019). AZ conceived and designed the present
- study, performed the analyses, implemented the models, and wrote a draft of the manuscript. AB
- conducted the fMRI analysis. All authors helped to revise the final manuscript. DS and MNS provided
 intellectual support throughout the study.
- 751 Data availability
- The data and code required to reproduce the analyses and figures are available at: https://github.com/
- 753 arielzylberberg/Reval_eLife_2024.

754 Acknowledgments

- 755 We thank Ari Pakman for helpful discussions.
- ⁷⁵⁶ This work was supported by the National Institutes of Health (R01NS113113 to M.N.S.), the Air Force
- ⁷⁵⁷ Office of Scientific Research under award (FA9550-22-1-0337 to M.N.S), the Howard Hughes Medical
- ⁷⁵⁸ Institute (M.N.S.), The McKnight Foundation Memory and Cognitive Disorders Award (D.S.), and the
- 759 National Science Foundation (1606916 to A.B.).

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Cluster #	Regions in cluster	Cluster size	p-value	Peak Z	х	У	z
1	R Parietal Operculum Cortex R Planum Temporale	58	0.00885	4.38	50.5	-29	29.5
2	L Superior Parietal Lobule	53	0.0149	4.08	29.5	-42.5	56.5
3	R Frontal Pole R Frontal Medial Cortex L Frontal Medial Cortex	51	0.0184	4.28	-0.5	56.5	-9.5

Table S1. Activation table for map in Fig. 9

The effect of *d-value* on BOLD in *Main fMRI model*. For each cluster, the list shows regions from the Harvard-Oxford atlas that contained a peak activation of a subcluster, along with the peak p-value, the peak effect size, and the peak X/Y/Z location for the cluster in MNI space.

		s-value of ch	osen item				
Cluster #	Regions in cluster	Cluster size	p-value	Peak Z	х	у	z
1	R Lateral Occipital Cortex R Angular Gyrus	903	4.6×10^{-23}	4.79	40	-66.5	50.5
2	L Lateral Occipital Cortex L Middle Temporal Gyrus L Supramarginal Gyrus L Angular Gyrus	786	6.28×10^{-21}	4.74	-45.5	-54.5	59.5
3	R Precuneous Cortex L Precuneous Cortex R Lateral Occipital Cortex	242	6.09×10^{-9}	4.32	10	-75.5	41.5
4	R Inferior Temporal Gyrus R Middle Temporal Gyrus	235	9.54×10^{-9}	4.77	58	-56	-12.5
5	R Caudate	116	4.76×10^{-5}	4.36	11.5	10	-3.5
6	L Caudate	111	7.18×10^{-5}	4.13	-9.5	10	-0.5
7	R Precuneous Cortex	80	0.00107	4.1	11.5	-48.5	38.5
8	L Precuneous Cortex L Intracalcarine Cortex	71	0.00248	4.43	-14	-62	11.5
9	L Cingulate Gyrus	49	0.023	3.7	-2	-44	38.5
10	R Middle Frontal Gyrus	43	0.0443	4.07 40	13	53.5	
		d-value of ch	osen item				
Cluster #	Regions in cluster	Cluster size	p-value	Peak Z	х	v	z
1	L Precuneous Cortex	614	6.56×10^{-17}	4.38	-11	-71	29.5
2	R Angular Gyrus R Lateral Occipital Cortex R Supramarginal Gyrus	271	2.39×10^{-9}	4.65	52	-56	14.5
3	L Lateral Occipital Cortex	252	$7.44 * 10^{-9}$	4.29	-41	-75.5	29.5
4	L Angular Gyrus L Supramarginal Gyrus L Lateral Occipital Cortex L Supramarginal Gyrus	136	1.66×10^{-5}	4.05	-57.5	-56	38.5
5	R Precuneous Cortex R Cingulate Gyrus	115	8.27×10^{-5}	4.09	11.5	-50	41.5
6	R Middle Temporal Gyrus R Inferior Temporal Gyrus R Lateral Occipital Cortex	103	0.000216	4.47	55	-53	2.5
7	L Caudate	94	0.000455	4.46	-9.5	10	-0.5
8	L Paracingulate Gyrus L Frontal Pole	88	0.000758	4.13	-12.5	43	-6.5
9	R Supramarginal Gyrus R Angular Gyrus	72	0.00313	3.88	59.5	-45.5	41.5
10	L Middle Frontal Gyrus	50	0.0263	4	-29	13	53.5
11	R Caudate	45	0.0443	4.14	11.5	10	-3.5
	(d	-value – s-value)	of chosen item				
Cluster #	Regions in cluster	Cluster size	p-value	Peak Z	х	У	Z
1	Parietal Operculum Cortex Planum Temporale	51	0.0182	4.48	50.5	-29	29.5

 Table S2. Activation tables for maps in Figure 9–Figure Supplement 1

The effect of *s*-value on BOLD in *fMRI Model of s*-value only (top), the effect of *d*-value on BOLD in *fMRI Model of d*-value only (middle), and the effect of (*s*-value – *d*-value) in *fMRI model of d*-value – *s*-value only (bottom). For each cluster, the list shows regions from the Harvard-Oxford atlas that contained a peak activation of a subcluster, along with the peak p-value, the peak effect size, and the peak X/Y/Z location for the cluster in MNI space.



Figure 5–Figure supplement 1. Static and dynamic values competing to explain choice. We fit the logistic regression model indicated in the figure separately for each participant, where Δv_s and Δv_d are the difference in static and dynamic values for each trial, respectively. The ordinate show the regression coefficient associated with Δv_s and the abscissa show the regression coefficient associated with Δv_s . Each data point corresponds to a different participant. Error bars indicate the standard error of the associated regression coefficient.



Figure 5–Figure supplement 2. Comparison of *DDM* fits using static and dynamic values. (A) BIC comparison between the *DDM* in which the drift rate depends on either Δv_d or Δv_s . The comparison favors the model that uses the dynamic values for all participants. (B) Same as A, but for choice and response time data simulated from the *DDM* fit to the participants' data using the static (i.e., explicitly reported) values.







Figure 9–Figure supplement 1. *d-value*, but to a lesser extent *s-value* and the difference between the two, is reflected in BOLD activity in ventromedial prefrontal cortex. Brain-wide fMRI analyses with whole-brain correction for multiple comparisons revealed 1) no significant correlation between *s-value* and activity in the vmPFC, but a significant correlation with BOLD in the striatum and in the precuneus when only *s-value* was included in the model (top), 2) a significant correlation between *d-value* and BOLD in vmPFC, striatum, and precuneus in a model that only included *d-value* (middle), and 3) no significant correlation between the difference between *d-value* and *s-value* in the vmPFC when only this difference is included in the model. The statistical maps from these three independent models were projected onto the cortical surface. Shown here are the medial view of the right and left hemispheres of a semi-inflated surface of a template brain. The heatmap color bar ranges from z-stat = 3.1 to 3.6. All maps were cluster corrected for familywise error rate at a whole-brain level with an uncorrected cluster-forming threshold of z = 3.1 and corrected extent of p < 0.05. Full unthresholded maps can be viewed here: https://identifiers.org/neurovault.collection:17498.

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