PORTLAND PRESS

Review Article

Environment-coupled models of leaf metabolism

🅾 **Nadine Töpfer**

Leibniz Institute of Plant Genetics and Crop Plant Research, Gatersleben, Germany

Correspondence: Nadine Töpfer (toepfer@ipk-gatersleben.de)

OPEN ACCESS

The plant leaf is the main site of photosynthesis. This process converts light energy and inorganic nutrients into chemical energy and organic building blocks for the biosynthesis and maintenance of cellular components and to support the growth of the rest of the plant. The leaf is also the site of gas–water exchange and due to its large surface, it is particularly vulnerable to pathogen attacks. Therefore, the leaf's performance and metabolic modes are inherently determined by its interaction with the environment. Mathematical models of plant metabolism have been successfully applied to study various aspects of photosynthesis, carbon and nitrogen assimilation and metabolism, aided suggesting metabolic intervention strategies for optimized leaf performance, and gave us insights into evolutionary drivers of plant metabolism in various environments. With the increasing pressure to improve agricultural performance in current and future climates, these models have become important tools to improve our understanding of plant–environment interactions and to propel plant breeders efforts. This overview article reviews applications of large-scale metabolic models of leaf metabolism to study plant–environment interactions by means of flux-balance analysis. The presented studies are organized in two ways — by the way the environment interactions are modelled — via *external constraints or data-integration* and by the studied environmental interactions — abiotic or biotic.

Introduction

The plant leaf is the main photosynthetic organ where light energy is converted into chemical energy to support the maintenance and growth of the leaf and the rest of the plant. The leaf is also the site of gas-exchange (O_2, CO_2 and water vapour) through the stomata and different forms of photosynthesis and leaf architecture — C3, C4 and crassulacean acid metabolism (CAM) — have evolved to cope with different environments. However, given its large surface area the plant leaf is also vulnerable to pathogen attacks. Due to these various factors, the leaf is a main determinant of plant growth and health. Therefore, gaining a better understanding of leaf–environment interactions is key to developing strategies to better equip our crop plants for productivity requirements in current and future climates. Computational models of leaf metabolism can aid this quest by explaining metabolic, architectural, and evolutionary aspects to guide the engineering of more productive and resistant crop species. In this review, I focus on flux-balance models of leaf metabolism and highlight their applications to study plant–environment interactions.

Flux-balance models rely on the stoichiometry of the metabolic network under consideration and an optimality assumption based on which metabolic steady-state fluxes can be predicted [1,2]. In the past decade, plant stoichiometric network models have been reconstructed for a large range of species and to varying extent, covering cell suspension models, multi-cell type, and whole-plant models [3–6]. Several pipelines for the automated reconstruction of plant metabolic network models are available [7–10]. The optimality assumption or 'objective function' depends on the metabolic system under consideration and reflects its function in the plant. For instance, for a growing leaf the objective function could be the maximization of biomass production and for a mature leaf the export of photosynthetic assimilates to the phloem [11]. Other optimality criteria have also been applied, such as the minimization of internal fluxes or photon usage efficiency [12,13]. The latter objectives are often chosen when metabolic outputs, such as growth rates, have been experimentally determined and can

119

be applied as constraints. Additionally, external constraints, such as limited nutrient or light availability, can be modelled by constraining the respective uptake fluxes. Depending on these constraints the model then predicts optimal metabolic steady-state flux modes which can then be analyzed with respect to changes between conditions and complement experimental observations. See Figure 1 for a schematic representation.

As an extension to this, various data-integrative approaches have been proposed to model condition-specific metabolic fluxes or to extract context-specific metabolic networks. Most of these approaches employ transcript, protein or metabolite abundances to constraint the flux boundaries of the respective reactions [14–17].

While any flux-balance model of leaf metabolism is inherently coupled to the environment via exchange reactions, such as light influx, CO_2 and O_2 exchange, and nutrient uptake; the focus here will be on studies that investigate the leaf's metabolic response to changes in those parameters or which integrate data collected from leaf material exposed to different environments. The highlighted studies are divided into two groups — *environmental constraint-driven* and *data-integrative* — based on how the environment-specificity is achieved. Moreover, the studies are organized according to the modelled interaction, i.e. abiotic or biotic. A schematic overview of the various modelling approaches is shown in Figure 2 and summarized in Table 1.

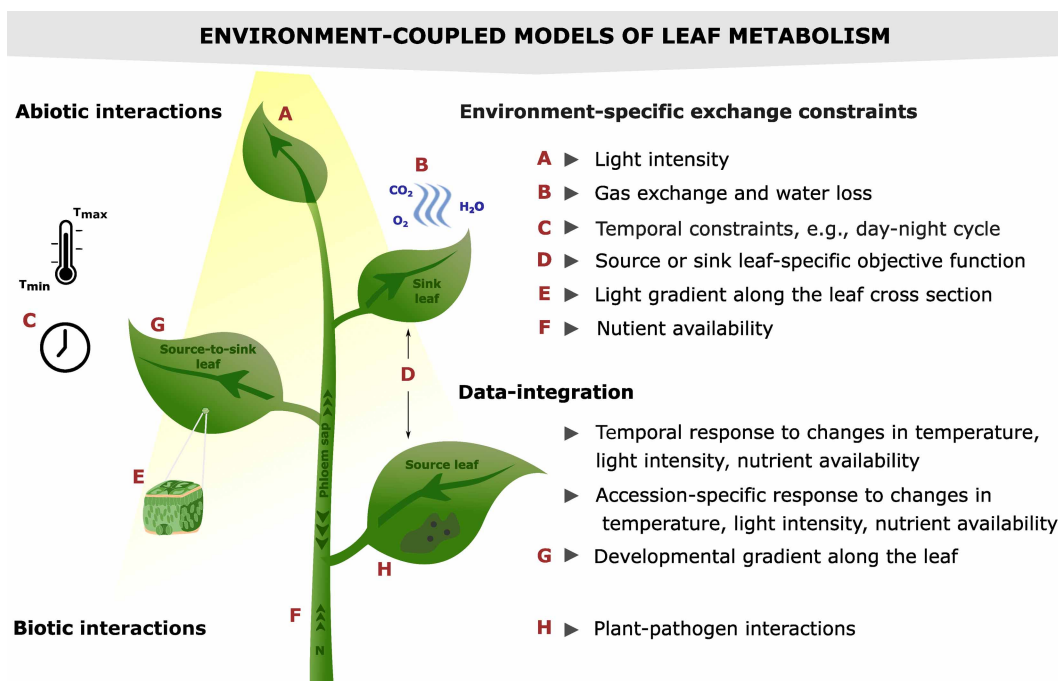# Abiotic interactions
Environmental constraint-driven models
Response to different light intensities
In one of the earliest studies in 2013, Poolman et al. [18] analyzed a genome-scale model representing a developing rice leaf cell to identify changes in reaction fluxes in response to changes in light influx. One of their
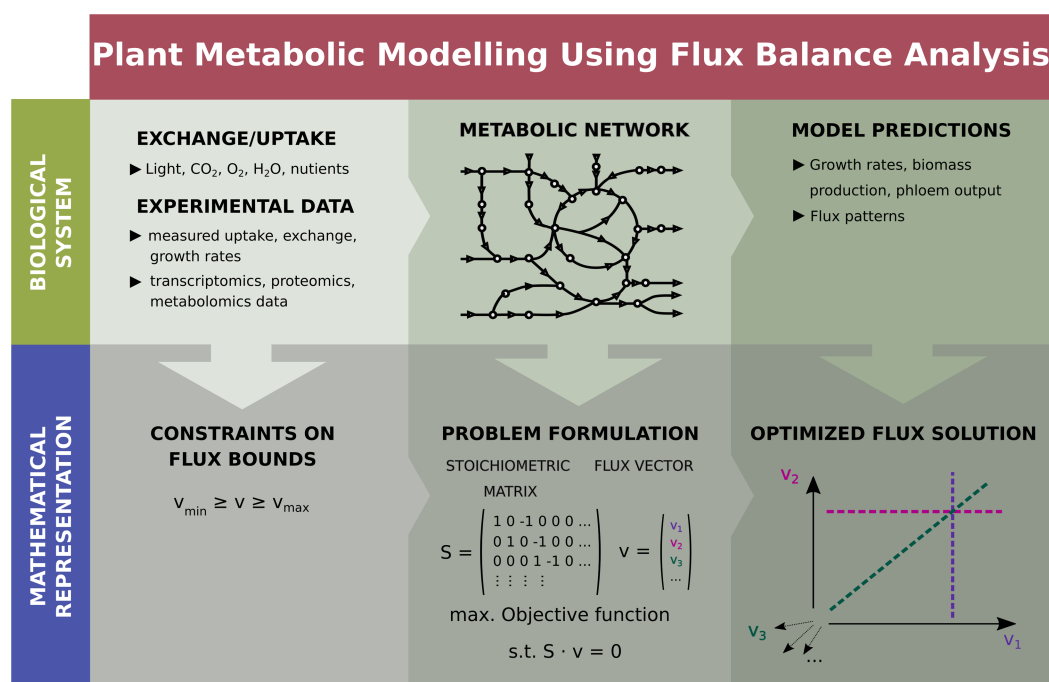
Figure 1. Schematic representation of flux-balance modelling.
The top part illustrates the metabolic system under consideration. (Left) External constraints, such as exchange and uptake rates and biochemical properties constrain the allowed metabolic fluxes. (Middle) The metabolic network coverts input compounds and generates a metabolic output via a series of biochemical reactions. (Right) This metabolic output can be measured as e.g. growth rate, biomass composition or flux patterns. The bottom part illustrates the mathematical representation of the metabolic system under consideration. (Left) External constraints as well as experimental data can serve to constrain the lower and upper flux bounds ($v_{min} \geq v \geq v_{max}$). (Middle) The metabolic network and fluxes are represented as a stoichiometric matrix, S and the metabolic flux vector, v, respectively. The (usually) linear optimization problem optimizes the biological objective, e.g. growth or phloem output, in a metabolic steady-state ($S \times v = 0$). (Right) Result of this optimization is a set of flux distributions captured in v. These optimal solutions can then be subjected to further analysis.

Figure 2. Representation of environment-coupled models of leaf metabolism.
(Left) Abiotic as well as biotic interactions between a plant leaf and the environment have been modelled using flux-balance analysis. (Middle) These interactions can occur at various sites of the leaf, e.g. light uptake through photosynthesis in the chloroplasts or gas-exchange through the stomata (marked *A* to *H* and listed on the right). (Right) Studies investigating abiotic constraints can be further classified based on environment-specific exchange constraints, such as light intensity or nutrient availability, data-integrative approaches, such as temporal response or accession specific outputs, or combinations of both. Data-integrative approaches have also been used to model biotic interactions.

findings put forward a beneficial role for the energy-consuming photorespiratory pathway under supraoptimal light conditions. The photorespiratory pathway recycles toxic intermediates which are formed due to the dual activity of ribulose-1,5-bisphosphate carboxylase-oxygenase (rubisco), the main enzyme to convert atmospheric carbon dioxide to energy-rich molecules. With increasing temperature rubisco's ratio of carboxylation to oxygenation (v_C/v_O) shifts towards O_2-fixation. This side reaction forms byproducts which are then recycled in the energy-wasting process of photorespiration. The model predicted that the photorespiratory pathway was spontaneously activated at supraoptimal light intensities and thereby dissipated excess light energy to prevent cell damage or overreduction.

A year later the same authors extended this study by exploring flux rearrangements during the transition from a growing to a mature leaf [11]. This was modelled as a transition from synthesizing leaf biomass to export of nutrients to the phloem as a function of light intensity. The authors found that the predicted flux patterns were relatively insensitive to the specific metabolic function of the leaf and attributed flux differences to changes in energy and redox requirements for the different metabolic outputs.

Cheung et al. [19] used the effect of light intensity on leaf metabolism together with a cost-weighted flux-balance formulation to study alternative metabolic pathways in *Arabidopsis*. The authors simulated C-limited conditions by fixing cellular output and maintenance costs and varied photon influx. They then simulated flux distributions for sets of randomly chosen flux weighting factors using flux minimization as the objective function. Their results emphasized the potential contribution of alternative fluxes in rebalancing and consuming ATP and NADPH, such as the chlorophyll and xanthophyll pigment cycles and various futile cycles, in different environmental and physiological conditions.

Later, Chatterjee et al. [20] used a different rice leaf model to study its responses to different light intensities and varying v_C/v_O ratios of rubisco, thereby mimicking increased photorespiration under drought stress,

Table 1. Environment-coupled flux-balance models of leaf metabolism

Author and year	Species	Biological question	Modelling approach
Abiotic interactions — environmental constraint-driven models			
Poolman et al. [18], Poolman et al. [11], Chatterjee et al. [20], Cheung et al. [19]	Rice, *Arabidopsis*	Response to different light intensities	Different light constraints
Simons et al. [21], Arnold and Nikoloski [22], Arnold et al. [25]	Maize, *Arabidopsis*	Response to different nitrogen levels and sources	Condition-specific biomass compositions
Shaw and Cheung [27]	*Arabidopsis*	Resource partitioning in whole-plant model	Dynamic FBA and different nutrient availability
Lakshmanan et al. [28], Chatterjee et al. [20], Yuan et al. [29], Shameer et al. [30]	Rice, Tomato, Generic CAM model	Response to different CO_2 levels	Constraints on rubisco's v_C/v_O ratio
Mallmann et al. [33]	*Flaveria* genus	Response to different CO_2 levels	Flux-balance model coupled to a kinetic model of photosynthesis
Blätke and Brautigam [34]	Generic C_4 model	Evolutionary drivers of C_4 photosynthesis	CCM-dependent rubisco population, cell type-specific light availability
Töpfer et al. [36]	Generic C_3 — CAM model	Water-saving flux modes in a C_3 leaf	24 hour diel resolution, flux-balance model coupled to a biophysical model of gas–water exchange
Abiotic interactions — data-driven models			
Töpfer et al. [44,64], Töpfer et al. [50]	*Arabidopsis*	Response to changes in light and temperature	Transcript and metabolomics data integration
Lakshmanan et al. [46]	Rice	Response to changes in light	Transcriptomics data integration
Liu et al. [65]	*Arabidopsis*	Response to low and elevated CO_2	Transcriptomics data integration
Bogart and Myers [48]	Maize	Source to sink transition along the leaf	Transcriptomics data integration, non-linear constraints
Nägele and Weckwert [49]	*Arabidopsis*	Metabolite compartmentation in different accessions exposed to low temperature	Metabolomics data integration
Sajitz-Hermstein et al. [51]	*Arabidopsis*	High to low CO_2 acclimation in wild type and photorespiratory mutants	Metabolomics data integration
Biotic interactions — data-driven models			
Botero et al. [56]	Potato	Effect of pathogen attack on photosynthetic activity	Transcriptomics data integration
Rodenburg et al. [58]	Tomato	Nutrient exchange between host leaf and pathogen	Transcriptomics data integration

Overview of studies which analyze plant–environment interactions by coupling mathematical models of leaf metabolism to the environment. The presented approaches are organized by abiotic and biotic interactions and by the applied modelling approach — environmental constraint-driven and data-integrative.

normal and suppressed photorespiration. Their comprehensive environment-scan combined with cost-weighted flux-balance analysis revealed different metabolic modes for maintaining redox and ATP balance including flux rearrangements across compartments and shifts in transport reactions. These findings highlighted alternative routes and metabolic flexibility for stress adaptation in leaf metabolism.

Response to different nitrogen levels and sources

Plant species, such as maize, sugarcane, and sorghum perform C4 photosynthesis. This specialized form of photo-synthesis involves a carbon-concentration mechanism in which initial CO_2 fixation and internal re-fixation by rubisco are separated in two adjacent cell types — the bundle sheath and mesophyll cells. This separation increases both nitrogen (N) and water use efficiency compared with C3 plants. To investigate the metabolic impact of N availability in maize Simons et al. [21] presented a C4 model capturing the interactions between bundle sheath and mesophyll cells. The authors used condition-specific biomass compositions and explored the effect of two knockdown mutants of glutamine synthetase (GS) — an enzyme essential for N assimilation. The authors used transcriptomic and proteomic data to introduce regulatory constraints that represented the metabol-ism of wild type and GS mutants under N-complete and -deficient conditions. This way, between nine and 100 reaction fluxes per condition were constrained. Using these condition-specific models they determined flux-sum ranges as a flux measure for the reactions associated with either the production or consumption of a given metab-olite. They achieved up to 90% accuracy when comparing their model predictions with measured metabolite levels. Furthermore, the authors identified a set of genes for further testing which the model's predictions had related to changes in biomass formation in the considered conditions.

In the same year, Arnold and Nikoloski [22] presented an *Arabidopsis* core model equipped with three biomass compositions to simulate carbon-limited, N-limited, and optimal growth conditions. This core model and two previous *Arabidopsis* models [23,24] were later used to *in silico* analyze the effect of N supply (nitrate/ ammonium) on individual amino acid synthesis costs under autotrophic/heterotrophic and day/night growth conditions [25]. The authors quantified the synthesis costs of amino acids in terms of ATP demand and found these costs to be highly dependent on the environment — most amino acid costs for night conditions were higher than those for heterotrophic day conditions and the costs for autotrophic conditions were higher than the costs for heterotrophic conditions. The study further confirmed NH_4^+ uptake to be cheaper than NO_3^- uptake to meet the plant's N demand due to the extra cost for nitrate reduction.

Shaw and Cheung used their previously developed diel *Arabidopsis* [26] model to generate a sophisticated dynamic multi-tissue, day–night modelling framework in which they studied the effect of both N-rich and -limiting conditions on *Arabidopsis* leaf and root growth [27]. Their framework demonstrated the power of integrated whole-plant analysis to uncover optimal growth strategies. More specifically, their model showed that it is energetically most efficient to store nitrate taken up into the root during the night in the vacuole and to then transport and fix it in the leaf during the day when light energy is available.

Response to different CO_2 levels

Studies that investigated the effect of different CO_2 levels on leaf metabolism and particularly photorespiration include models of rice [20,28], tomato [29] and generic models of CAM photosynthesis [30]. Typically, constraints on rubisco's v_C/v_O ratio were implemented to model the leaf's metabolic response to changing CO_2 levels or temperature (as v_C/v_O is temperature-dependent, see also section 'Response to different light intensities').

Of particular sophistication is a study by Mallmann et al. which combined a kinetic model of photosynthesis [31] and a stoichiometric model [32] to explore the evolution of C4 photosynthesis in the genus *Flaveria* [33]. Here, environment-specificity of the model was achieved by using the output of the kinetic model of C3–C4 intermediate photosynthesis to constrain key C4 parameters, such as net CO_2 uptake, rubisco's v_C/v_O ratio in mesophyll and bundle sheath cells, CO_2 leakage from the bundle sheath, PEP-carboxylase activity in the meso-phyll, the activity of NADP-malic enzyme (ME) in the bundle sheath, plasmodesmatal flux of glycine and serine, and decarboxylation by the glycine decarboxylase complex in the genome-scale stoichiometric model of C4 photosynthesis. This way, the authors found that C2 photosynthesis, an intermediate state where CO_2 is relocated from the mesophyll to the bundle sheath cells via the photorespiratory intermediates glycolate and glycerate, caused a N missbalance and that rebalancing N metabolism was a driving force for the evolution of C4 photosynthesis.

Spatial and temporal constraints as metabolic drivers

In a related study, Blätke and Bräutigam [34] studied the evolutionary trajectory of C4 metabolism by examin-ing selective pressures that potentially have led to the occurrence of this C-fixation mechanism in a two-celled stoichiometric model representing the C4-typical mesophyll-bundle sheath cell Kranz anatomy. In contrast

with earlier studies of C4 metabolism [21,32,33] in their model C4 photosynthesis was not enforced by fixing a priori defined flux patterns between the two cell types but the C4 syndrome was allowed to emerge under a set of different input constraints. The authors employed an artifice in which they approximated the CO_2 concentration-dependent changes in rubisco's v_C/v_O ratio by modelling two rubisco populations in the bundle sheath cells — the native rubisco, which performs both carboxylation and oxygenation at a typical C3 plant ratio of 3 : 1 [35], and a carbon-concentration mechanism-dependent rubisco population which only catalyzed the carboxylation of ribulose 1,5-bisphosphate and used exclusively CO_2 released in the bundle sheath cells. Using this setup, they tested several scenarios and found that high photorespiration and N limitation drove the emergence of C4 flux patterns in the model. The model also predicted that light availability and distribution across the leaf section, i.e. between mesophyll and bundle sheath cells could play a role in the evolutionary choices of possible decarboxylation enzymes NAD-ME, NADP-ME, and PEP-carboxykinase. Finally, the model predicted that C2 photosynthesis was optimal under particular conditions and supported the hypothesis of C2 photosynthesis as a stable intermediate state between C3 and C4 photosynthesis.

In our recent work, we focussed on studying the tradeoff between water-saving and leaf productivity and the analysis of alternative CAM-like flux modes in a C3 metabolic network [36]. In contrast with C4 photosynthesis, in CAM photosynthesis initial and re-fixation of CO_2 are not spatially but temporally separated between day and night. This way CO_2 can be taken up through the stomata at colder and more humid night-time hours, thereby minimizing water loss through transpiration. To capture this behaviour, we coupled a biophysical model of gas–water exchange to a time-resolved diel leaf metabolic model. This way, we were able to model the effect of three main abiotic parameters — temperature, relative humidity, and light intensity — on leaf metabolism. We used this environment-coupled model to study the emergence of water-saving flux modes on the Pareto frontier for water-saving and leaf productivity. Our analysis revealed that vacuolar storage capacity is a main determinant of the extent of CAM. Additionally, we identified the mitochondrial enzyme isocitrate dehydrogenase (ICDH) and an isocitrate-citrate-proline-2-oxo-glutarate cycle as a potential contributor to initial carbon fixation at night. Model analysis across a wide range of environmental parameters showed that the water-saving potential of CAM-like flux modes strongly depends on the environment and that under certain conditions CAM with night-time carbon fixation by ICDH could reach 11% total water saving for the conditions tested.

Environment-specific leaf models through data integration

The approaches highlighted so far all have in common that the environment-specificity was achieved by constraining input parameters, such as light intensity, CO_2 or N uptake, the light gradient in the leaf cross section, the gas–water exchange or few reaction fluxes based on experimental data. Most of the fluxes were left unconstrained and could vary between a generic lower and upper boundary. In contrast, several approaches that rely on the integration of Omics data and typically constrain several hundreds to thousands of reaction fluxes have been applied to plant metabolic models and resulted in environment-specific models and flux mode predictions. The majority of the methods employ transcriptomics data to constrain flux boundaries and can be grouped based on whether they employ binarized (e.g. PROM [37], iMAT [37,38], MADE [39], GIMME [40], AdaM [41]) or continuous gene-expression levels (e.g. E-Flux [42]) to constrain fluxes through the respective reactions.

Transcriptomics data integration

In an earlier study, we used an *Arabidopsis* metabolic network model accounting for both primary and secondary metabolism [43] and applied a transcriptomics data integrative approach to study changes in leaf metabolism in response to changes in temperature and light intensities [44,45]. The data integration was achieved by using a modified version of the E-Flux approach and enabled us to define three optimization-based indices to characterize different aspects of metabolic pathway behaviour in the context of the entire network. Our study highlighted pathways that showed differential behaviour with respect to a null model and their involvement in the different acclimation responses.

Lakshmanan et al. [46] investigated the effect of four different light treatments and darkness on rice leaf metabolism by combining a rice genome-scale model with transcriptome profiles. The authors performed flux sampling based on the E-Flux method and analyzed the up- and down-regulation of individual metabolic pathways. Additionally, they compared their modelling results to previously measured metabolomics data [47]. Using these combined approaches, they found that photosynthesis and secondary metabolism were up-regulated in blue light and reserve carbohydrates degradation was pronounced in the dark. The analysis

further identified phytohormones, such as abscisate, ethylene, gibberellin, and jasmonate as keymarkers of light-mediated regulation and helped elucidate the transcriptional control of red and blue light signals.

Another data-integrative study explored *Arabidopsis*'s response to low and elevated CO_2 by generating condition-specific models based on the integration of transcriptomics data using the iMat approach. Liu et al. showed that the simulated CO_2-fixation at different CO_2 concentrations was consistent with measured CO_2-assimilation curves. Additionally, they predicted post-transcriptionally regulated reactions across different CO_2 concentrations and that low CO_2 stress requires stronger metabolic adjustment than elevated CO_2 conditions.

While the above-outlined approaches incorporated time-resolved and/or compartment-specific data, Bogart and Myers [48] used spatially resolved data to study the transition from source to sink tissue along the leaf gradient. Their analysis predicted metabolic fluxes by integrating spatially resolved transcriptomics and enzyme activity data with a genome-scale model of maize leaf metabolism. Additionally, they modelled the non-linear relationships between CO_2 and O_2 levels and reaction rates in the C4 system. This resulted in a non-linearly constrained model describing mesophyll and bundle sheath cells in 15 segments of the developing maize leaf. The analysis successfully recaptured results from radiolabeling experiments and the observed base-to-tip transition between C-importing and -exporting tissue along the leaf axis. Thus, this approach laid the foundation for studying the response of various heterogeneous metabolic systems to environmental and biochemical perturbations by means of flux-balance analysis.

Metabolomics data integration

Nägele and Weckwerth [49] proposed a metabolomics data integrative approach which they applied to study metabolite compartmentation in leaves of different *Arabidopsis* accessions exposed to low temperature. The authors used a compartmentalized *Arabidopsis* network reconstruction [43] and compartment-specific metabolomics data to generate a reduced metabolic interaction matrix, i.e. a matrix that contains only measurable metabolites and their respective compartmentation. The extracted subcellular metabolic network comprised over 500 metabolic intermediates and interactions and was integrated with metabolite covariances of different *Arabidopsis thaliana* accessions. Analysis of these data-integrated networks revealed differences in the regulation of carbohydrate compartmentation in the three investigated accessions and highlighted differential regulation of the interconversion and transport of vacuolar glucose and fructose.

In a followup study to the above-mentioned analysis of *Arabidopsis*'s response to changes in temperature and light intensities [44] we tested the informative value of the transcriptomics data-integrative approach with respect to inferences that could be made on the level of metabolites [50]. We observed that substrates in pathways which our transcript-data integrative study had classified as important for the adjustment processes showed less temporal fluctuations. Moreover, these pathways had on average fewer substrates than the average pathway investigated. This led us to the conclusion that the observed substrate robustness is an inducible genetic mechanism, both depending on the metabolic network structure and the specific environmental condition.

In an attempt to model flux re-routing upon external perturbations we developed a metabolomics data-integrative approach and applied it to predict reactions and pathways with altered fluxes in wild type *Arabidopsis* leaves and four photorespiratory mutants undergoing high-to-low CO_2 acclimation [51,52]. The approach relied on relative metabolite abundances for at least two metabolic states and employed a mass-action like representation of differential fluxes. We found that the observed flux alterations in the knock-out mutants were mainly attributed to ATP synthase and the photosystem I, and fluxes through reactions from the Calvin–Benson–Bassham cycle, proline biosynthesis, N and redox metabolism and glycolysis. The study highlighted the power of integrated differential flux analysis to complement labor-intensive flux measurements which are usually restricted to small-scale networks.

Biotic interactions — plant–pathogen interactions

In recent years, several studies have focussed on modelling plant-microbe interactions by analyzing, both beneficial symbiont relationships, such as interactions between the roots and N fixing soil bacteria [53,54] and plant–pathogen interactions. Two studies have focused on modelling the plant leaf–pathogen interactions between the solanaceous species potato (*Solanum tuberosum*) and tomato (*Solanum lycopersicum*) and the late blight causing oomycete *Phytophthora infestans*.

Botero et al. aimed at gaining a better understanding of the molecular basis of the previously identified decrease in photosynthetic activity of infected potato plants [55,56]. To this end, the authors reconstructed a

genome-scale model of potato and integrated gene-expression data from three time-points after pathogen infection [57] using the maximization of biomass as an objective function. They predicted decreased photophosphorylation, the activity of the Calvin–Benson–Bassham cycle and starch synthesis as well as transiently increased photorespiration during the host–pathogen interaction and compared their results to experimental observations from the literature.

In contrast with this host-centric study, Rodenburg et al. studied the nutrient flux from the host to the pathogen during the infection [59]. Thus, the authors coupled a genome-scale model of tomato leaf metabolism [29] and *P. infestans* [58] by allowing all common metabolites to be exchanged between the plant and the pathogen. Using this combined plant-pathogen model they analyzed four scenarios in which they maximized biomass production of the pathogen and determined (*i*) the minimal set of nutrients *P. infestans* needed to import from the tomato leaf, (*ii*) and (*iii*) the minimum and maximum number of reactions used by *P. infestans*, (*iv*) a combination of (*i*) and (*ii*) where they determined the minimal nutrient uptake combined with minimal usage of pathogen reactions. The authors reasoned that the four investigated scenarios represented extreme cases and that the pool of imported nutrients would likely be a combination of the metabolite pools predicted in these scenarios. Additionally, the authors integrated dual-transcriptome time series data of a full late blight infection cycle on tomato leaves. Analysis of these contextualized models indicated that, as the infection progresses, *P. infestans* performed less *de novo* synthesis of metabolites and more scavenging from the tomato plant.

Perspectives

- Environment-coupled flux-balance models of leaf metabolism are a versatile means for multi-omics data integration and interpretation [17,60], they have closed gaps in our understanding of plant metabolism and led to the suggestion of engineering strategies to enhance plant's performance [36].

- Yet, one should be aware that flux-balance models are best suited to model plant systems in optimal growth conditions for which an objective function as well as a cellular maintenance costs can be readily defined. For non-optimal growth conditions determining an adequate objective function is less obvious and cellular maintenance costs might vary substantially and could account for a significant portion of the total energy budget [13].

- In the future, we will see continued efforts to integrate the here discussed environment-coupled flux-balance models into multi-scale modelling frameworks which can cover computational models of gene regulation, protein synthesis, metabolic pathways, and plant architecture up to the level of ecosystem models [61–63]. With the advancement and automatization of plant computational modelling I anticipate these models to play a crucial role in future agriculture research by guiding the development of crop species with improved yield and resistance in current and future climates.

Abbreviations
CAM, crassulacean acid metabolism; GS, glutamine synthetase; ICDH, isocitrate dehydrogenase; ME, malic enzyme.

PORTLAND
PRESS

References

1   Orth, J.D., Thiele, I. and Palsson, B.Ø. (2010) What is flux balance analysis? *Nat. Biotechnol.* **28**, 245–248 https://doi.org/10.1038/nbt.1614

2   Collakova, E., Yen, J.Y. and Senger, R.S. (2012) Are we ready for genome-scale modeling in plants? *Plant. Sci.* **191–192**, 53–70 https://doi.org/10.1016/j.plantsci.2012.04.010

3   Shaw, R. and Cheung, C.Y.M. (2019) Multi-tissue to whole plant metabolic modelling. *Cell. Mol. Life Sci.* **77**, 489–495 https://doi.org/10.1007/s00018-019-03384-y

4   Nikoloski, Z., Perez-Storey, R. and Sweetlove, L.J. (2015) Inference and prediction of metabolic network fluxes. *Plant Physiol.* **169**, 1443–1455 https://doi.org/10.1104/pp.15.01082

5   Sweetlove, L.J. and Ratcliffe, R.G. (2011) Flux-Balance modeling of plant metabolism. *Front. Plant Sci.* **2**, 38 https://doi.org/10.3389/fpls.2011.00038

6   de Oliveira Dal'Molin, C.G. and Nielsen, L.K. (2018) Plant genome-scale reconstruction: from single cell to multi-tissue modelling and omics analyses. *Curr. Opin. Biotechnol.* **49**, 42–48 https://doi.org/10.1016/j.copbio.2017.07.009

7   de Oliveira Dal'Molin, C.G. and Nielsen, L.K. (2013) Plant genome-scale metabolic reconstruction and modelling. *Curr. Opin. Biotechnol.* **24**, 271–277 https://doi.org/10.1016/j.copbio.2012.08.007

8   Seaver, S.M.D., Henry, C.S. and Hanson, A.D. (2012) Frontiers in metabolic reconstruction and modeling of plant genomes. *J. Exp. Bot.* **63**, 2247–2258 https://doi.org/10.1093/jxb/err371

9   Seaver, S.M.D., Gerdes, S., Frelin, O., Lerma-Ortiz, C., Bradbury, L.M.T., Zallot, R. et al. (2014) High-throughput comparison, functional annotation, and metabolic modeling of plant genomes using the PlantSEED resource. *Proc. Natl. Acad. Sci. U.S.A.* **111**, 9645–9650 https://doi.org/10.1073/pnas.1401329111

10   Seaver, S.M.D., Lerma-Ortiz, C., Conrad, N., Mikaili, A., Sreedasyam, A., Hanson, A.D. et al. (2018) PlantSEED enables automated annotation and reconstruction of plant primary metabolism with improved compartmentalization and comparative consistency. *Plant J.* **95**, 1102–1113 https://doi.org/10.1111/tpj.14003

11   Poolman, M.G., Kundu, S., Shaw, R. and Fell, D.A. (2014) Metabolic trade-offs between biomass synthesis and photosynthate export at different light intensities in a genome-scale metabolic model of rice. *Front. Plant Sci.* **5**, 656 https://doi.org/10.3389/fpls.2014.00656

12   Holzhütter, H.-G. (2004) The principle of flux minimization and its application to estimate stationary fluxes in metabolic networks. *Eur. J. Biochem.* **271**, 2905–2922 https://doi.org/10.1111/j.1432-1033.2004.04213.x

13   Cheung, C.Y.M., Williams, T.C.R., Poolman, M.G., Fell, D.A., Ratcliffe, R.G. and Sweetlove, L.J. (2013) A method for accounting for maintenance costs in flux balance analysis improves the prediction of plant cell metabolic phenotypes under stress conditions. *Plant J.* **75**, 1050–1061 https://doi.org/10.1111/tpj.12252

14   Blazier, A.S. and Papin, J.A. (2012) Integration of expression data in genome-scale metabolic network reconstructions. *Front. Physiol.* **3**, 299 https://doi.org/10.3389/fphys.2012.00299

15   Åkesson, M., Förster, J. and Nielsen, J. (2004) Integration of gene expression data into genome-scale metabolic models. *Metab. Eng.* **6**, 285–293 https://doi.org/10.1016/j.ymben.2003.12.002

16   Estévez S, R. and Nikoloski, Z. (2014) Generalized framework for context-specific metabolic model extraction methods. *Front. Plant Sci.* **5**, 491 https://doi.org/10.3389/fpls.2014.00491

17   Töpfer, N., Kleessen, S. and Nikoloski, Z. (2015) Integration of metabolomics data into metabolic networks. *Front. Plant Sci.* **6**, 49 https://doi.org/10.3389/fpls.2015.00049

18   Poolman, M.G., Kundu, S., Shaw, R. and Fell, D.A. (2013) Responses to light intensity in a genome-Scale model of rice metabolism. *Plant Physiol.* **162**, 1060–1072 https://doi.org/10.1104/pp.113.216762

19   Cheung, C.Y.M., Ratcliffe, R.G. and Sweetlove, L.J. (2015) A method of accounting for enzyme costs in flux balance analysis reveals alternative pathways and metabolite stores in an illuminated Arabidopsis leaf. *Plant Physiol.* **169**, 1671–1682 https://doi.org/10.1104/pp.15.00880

20   Chatterjee, A., Huma, B., Shaw, R. and Kundu, S. (2017) Reconstruction of oryza sativa indica genome scale metabolic model and Its responses to varying RuBisCO activity, light intensity, and enzymatic cost conditions. *Front. Plant Sci.* **8**, 2060 https://doi.org/10.3389/fpls.2017.02060

21   Simons, M., Saha, R., Amiour, N., Kumar, A., Guillard, L., Clément, G. et al. (2014) Assessing the metabolic impact of nitrogen availability using a compartmentalized maize leaf genome-scale model. *Plant Physiol.* **166**, 1659–1674 https://doi.org/10.1104/pp.114.245787

22   Arnold, A. and Nikoloski, Z. (2014) Bottom-up metabolic reconstruction of Arabidopsis and Its application to determining the metabolic costs of enzyme production. *Plant Physiol.* **165**, 1380–1391 https://doi.org/10.1104/pp.114.235358

23   Poolman, M.G., Miguet, L., Sweetlove, L.J. and Fell, D.A. (2009) A genome-scale metabolic model of Arabidopsis and some of its properties. *Plant Physiol.* **151**, 1570–1581 https://doi.org/10.1104/pp.109.141267

24   de Oliveira Dal'Molin, C.G., Quek, L.-E., Palfreyman, R.W., Brumbley, S.M. and Nielsen, L.K. (2010) AraGEM, a genome-scale reconstruction of the primary metabolic network in Arabidopsis. *Plant Physiol.* **152**, 579–589 https://doi.org/10.1104/pp.109.148817

25   Arnold, A., Sajitz-Hermstein, M. and Nikoloski, Z. (2015) Effects of varying nitrogen sources on amino acid synthesis costs in *Arabidopsis thaliana* under different light and carbon-source conditions. *PLoS One* **10**, e0116536 https://doi.org/10.1371/journal.pone.0116536

26   Cheung, C.Y.M., Poolman, M.G., Fell, D.A., Ratcliffe, R.G. and Sweetlove, L.J. (2014) A diel flux balance model captures interactions between light and dark metabolism during day-night cycles in C3 and crassulacean acid metabolism leaves. *Plant Physiol.* **165**, 917–929 https://doi.org/10.1104/pp.113.234468

27   Shaw, R. and Cheung, C.Y.M. (2018) A dynamic multi-tissue flux balance model captures carbon and nitrogen metabolism and optimal resource partitioning during Arabidopsis growth. *Front. Plant Sci.* **9**, 884 https://doi.org/10.3389/fpls.2018.00884

28   Lakshmanan, M., Mohanty, B. and Lee, D.-Y. (2013) Identifying essential genes/reactions of the rice photorespiration by in silico model-based analysis. *Rice* **13**, 20 https://doi.org/10.1186/1939-8433-6-20

29   Yuan, H., Cheung, C.Y.M., Poolman, M.G., Hilbers, P.A.J. and van Riel, N.A.W. (2016) A genome-scale metabolic network reconstruction of tomato (*Solanum lycopersicum* L.) and its application to photorespiratory metabolism. *Plant J.* **85**, 289–304 https://doi.org/10.1111/tpj.13075

30   Shameer, S., Baghalian, K., Cheung, C.Y.M., Ratcliffe, R.G. and Sweetlove, L.J. (2018) Computational analysis of the productivity potential of CAM. *Nat. Plants* **4**, 165–171 https://doi.org/10.1038/s41477-018-0112-2

31   Von Caemmerer, S. (2000) *Biochemical Models of Leaf Photosynthesis*, CSIRO Publishing, Clayton, Victoria, Australia

32 de Oliveira Dal'Molin, C.G., Quek, L.-E., Palfreyman, R.W., Brumbley, S.M. and Nielsen, L.K. (2010) C4GEM, a genome-scale metabolic model to study C4 plant metabolism. *Plant Physiol.* **154**, 1871–1885 https://doi.org/10.1104/pp.110.166488

33 Mallmann, J., Heckmann, D., Bräutigam, A., Lercher, M.J., Weber, A.P.M., Westhoff, P. et al. (2014) The role of photorespiration during the evolution of C4 photosynthesis in the genus Flaveria. *Elife* **3**, e02478 https://doi.org/10.7554/eLife.02478

34 Blätke, M.-A. and Bräutigam, A. (2019) Evolution of C4 photosynthesis predicted by constraint-based modelling. *Elife* **8**, e49305 https://doi.org/10.7554/eLife.49305

35 Gutteridge, S. and Pierce, J. (2006) A unified theory for the basis of the limitations of the primary reaction of photosynthetic CO_2 fixation: was Dr. Pangloss right? *Proc. Natl. Acad. Sci. U.S.A.* **103**, 7203–7204 https://doi.org/10.1073/pnas.0602075103

36 Töpfer, N., Braam, T., Shameer, S., Ratcliffe, R.G. and Sweetlove, L.J. (2020) Alternative CAM modes provide environment-specific water-saving benefits in a leaf metabolic model. *Plant Cell* **32**, 3689–3705 https://doi.org/10.1105/tpc.20.00132

37 Chandrasekaran, S. and Price, N.D. (2010) Probabilistic integrative modeling of genome-scale metabolic and regulatory networks in *Escherichia coli* and *Mycobacterium tuberculosis*. *Proc. Natl. Acad. Sci. U.S.A.* **107**, 17845–17850 https://doi.org/10.1073/pnas.1005139107

38 Shlomi, T., Cabili, M.N., Herrgård, M.J., Palsson, B.Ø and Ruppin, E. (2008) Network-based prediction of human tissue-specific metabolism. *Nat. Biotechnol.* **26**, 1003–1010 https://doi.org/10.1038/nbt.1487

39 Jensen, P.A. and Papin, J.A. (2011) Functional integration of a metabolic network model and expression data without arbitrary thresholding. *Bioinformatics* **27**, 541–547 https://doi.org/10.1093/bioinformatics/btq702

40 Becker, S.A. and Palsson, B.O. (2008) Context-specific metabolic networks are consistent with experiments. *PLoS Comput. Biol.* **4**, e1000082 https://doi.org/10.1371/journal.pcbi.1000082

41 Töpfer, N., Jozefczuk, S. and Nikoloski, Z. (2012) Integration of time-resolved transcriptomics data with flux-based methods reveals stress-induced metabolic adaptation in *Escherichia coli*. *BMC Syst. Biol.* **6**, 148 https://doi.org/10.1186/1752-0509-6-148

42 Colijn, C., Brandes, A., Zucker, J., Lun, D.S., Weiner, B., Farhat, M.R. et al. (2009) Interpreting expression data with metabolic flux models: predicting *Mycobacterium tuberculosis* mycolic acid production. *PLoS Comput. Biol.* **5**, e1000489 https://doi.org/10.1371/journal.pcbi.1000489

43 Mintz-Oron, S., Meir, S., Malitsky, S., Ruppin, E., Aharoni, A. and Shlomi, T. (2012) Reconstruction of Arabidopsis metabolic network models accounting for subcellular compartmentalization and tissue-specificity. *Proc. Natl. Acad. Sci. U.S.A.* **109**, 339–344 https://doi.org/10.1073/pnas.1100358109

44 Töpfer, N. and Niokoloski, Z. (2013) Large-scale modeling provides insights into Arabidopsis's acclimation to changing light and temperature conditions. *Plant Signal. Behav.* **8**, e25480 https://doi.org/10.4161/psb.25480

45 Caldana, C., Degenkolbe, T., Cuadros-Inostroza, A., Klie, S., Sulpice, R., Leisse, A. et al. (2011) High-density kinetic analysis of the metabolomic and transcriptomic response of Arabidopsis to eight environmental conditions. *Plant J.* **67**, 869–884 https://doi.org/10.1111/j.1365-313X.2011.04640.x

46 Lakshmanan, M., Lim, S.-H., Mohanty, B., Kim, J.K., Ha, S.-H. and Lee, D.-Y. (2015) Unraveling the light-specific metabolic and regulatory signatures of rice through combined in silico modeling and multi-omics analysis. *Plant Physiol.* **169**, 3002–3020 https://doi.org/10.1104/pp.15.01379

47 Jung, E.S., Lee, S., Lim, S.-H., Ha, S.-H., Liu, K.-H. and Lee, C.H. (2013) Metabolite profiling of the short-term responses of rice leaves (*Oryza sativa* cv. Ilmi) cultivated under different LED lights and its correlations with antioxidant activities. *Plant Sci.* **210**, 61–69 https://doi.org/10.1016/j.plantsci.2013.05.004

48 Bogart, E. and Myers, C.R. (2016) Multiscale metabolic modeling of C4 plants: connecting nonlinear genome-scale models to leaf-scale metabolism in developing maize leaves. *PLoS One* **11**, e0151722 https://doi.org/10.1371/journal.pone.0151722

49 Nägele, T. and Weckwerth, W. (2013) A workflow for mathematical modeling of subcellular metabolic pathways in leaf metabolism of *Arabidopsis thaliana*. *Front. Plant Sci.* **4**, 541 https://doi.org/10.3389/fpls.2013.00541

50 Töpfer, N., Scossa, F., Fernie, A. and Nikoloski, Z. (2014) Variability of metabolite levels is linked to differential metabolic pathways in Arabidopsis's responses to abiotic stresses. *PLoS Comput. Biol.* **10**, e1003656 https://doi.org/10.1371/journal.pcbi.1003656

51 Sajitz-Hermstein, M., Töpfer, N., Kleessen, S., Fernie, A.R. and Nikoloski, Z. (2016) iReMet-flux: constraint-based approach for integrating relative metabolite levels into a stoichiometric metabolic models. *Bioinformatics* **32**, i755–i762 https://doi.org/10.1093/bioinformatics/btw465

52 Timm, S., Mielewczik, M., Florian, A., Frankenbach, S., Dreissen, A., Hocken, N. et al. (2012) High-to-low CO_2 acclimation reveals plasticity of the photorespiratory pathway and indicates regulatory links to cellular metabolism of Arabidopsis. *PLoS One* **7**, e42809 https://doi.org/10.1371/journal.pone.0042809

53 Pfau, T., Christian, N., Masakapalli, S.K., Sweetlove, L.J., Poolman, M.G. and Ebenhöh, O. (2018) The intertwined metabolism during symbiotic nitrogen fixation elucidated by metabolic modelling. *Sci. Rep.* **8**, 12504 https://doi.org/10.1038/s41598-018-30884-x

54 diCenzo, G.C., Tesi, M., Pfau, T., Mengoni, A. and Fondi, M. (2020) Genome-scale metabolic reconstruction of the symbiosis between a leguminous plant and a nitrogen-fixing bacterium. *Nat. Commun.* **11**, 2574 https://doi.org/10.1038/s41467-020-16484-2

55 Restrepo, S., Myers, K.L., del Pozo, O., Martin, G.B., Hart, A.L., Buell, C.R. et al. (2005) Gene profiling of a compatible interaction between *Phytophthora infestans* and *Solanum tuberosum* suggests a role for carbonic anhydrase. *Mol. Plant Microbe Interact.* **18**, 913–922 https://doi.org/10.1094/MPMI-18-0913

56 Botero, K., Restrepo, S. and Pinzón, A. (2018) A genome-scale metabolic model of potato late blight suggests a photosynthesis suppression mechanism. *BMC Genomics* **19**, 863 https://doi.org/10.1186/s12864-018-5192-x

57 Gyetvai, G., Sønderkær, M., Göbel, U., Basekow, R., Ballvora, A., Imhoff, M. et al. (2012) The transcriptome of compatible and incompatible interactions of potato (*Solanum tuberosum*) with *Phytophthora infestans* revealed by DeepSAGE analysis. *PLoS One* **7**, e31526 https://doi.org/10.1371/journal.pone.0031526

58 Rodenburg, S.Y.A., Seidl, M.F., de Ridder, D. and Govers, F. (2018) Genome-wide characterization of *Phytophthora infestans* metabolism: a systems biology approach. *Mol. Plant Pathol.* **19**, 1403–1413 https://doi.org/10.1111/mpp.12623

59 Rodenburg, S.Y.A., Seidl, M.F., Judelson, H.S., Vu, A.L., Govers, F. and de Ridder, D. (2019) Metabolic model of the *Phytophthora infestans*-tomato interaction reveals metabolic switches during host colonization. *mBio* **10**, e00454-19 https://doi.org/10.1128/mBio.00454-19

60 Töpfer, N., Seaver, S.M.D. and Aharoni, A. (2018) Integration of plant metabolomics data with metabolic networks: progresses and challenges. *Methods Mol. Biol.* **1778**, 297–310 https://doi.org/10.1007/978-1-4939-7819-9_21

61 Benes, B., Guan, K., Lang, M., Long, S.P., Lynch, J.P., Marshall-Colón, A. et al. (2020) Multiscale computational models can guide experimentation and targeted measurements for crop improvement. *Plant J.* **103**, 21–31 https://doi.org/10.1111/tpj.14722

62   Marshall-Colon, A., Long, S.P., Allen, D.K., Allen, G., Beard, D.A., Benes, B. et al. (2017) Crops in silico: generating virtual crops using an integrative and multi-scale modeling platform. *Front. Plant Sci.* **8**, 786 https://doi.org/10.3389/fpls.2017.00786

63   Chew, Y.H., Seaton, D.D. and Millar, A.J. (2017) Multi-scale modelling to synergise plant systems biology and crop science. *Field Crops Res.* **202**, 77–83 https://doi.org/10.1016/j.fcr.2016.02.012

64   Töpfer, N., Caldana, C., Grimbs, S., Willmitzer, L., Fernie, A.R. and Nikoloski, Z. (2013) Integration of genome-scale modeling and transcript profiling reveals metabolic pathways underlying light and temperature acclimation in Arabidopsis. *Plant Cell* **25**, 1197–1211 https://doi.org/10.1105/tpc.112.108852

65   Liu, L., Shen, F., Xin, C. and Wang, Z. (2016) Multi-scale modeling of *Arabidopsis thaliana* response to different CO_2 conditions: From gene expression to metabolic flux. *J. Integr. Plant Biol.* **58**, 2–1l https://doi.org/10.1111/jipb.12370