

Accurate X-ray Absorption Spectra near L- and M-Edges from Relativistic Four-Component Damped Response Time-Dependent Density Functional Theory

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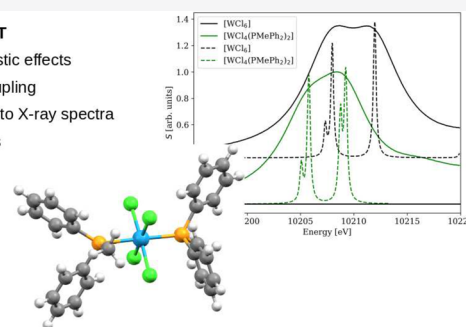


Supporting Information

ABSTRACT: The simulation of X-ray absorption spectra requires both scalar and spin-orbit (SO) relativistic effects to be taken into account, particularly near L- and M-edges where the SO splitting of core p and d orbitals dominates. Four-component Dirac-Coulomb Hamiltonian-based linear damped response time-dependent density functional theory (4c-DR-TDDFT) calculates spectra directly for a selected frequency region while including the relativistic effects variationally, making the method well suited for X-ray applications. In this work, we show that accurate X-ray absorption spectra near $L_{2,3}$ - and $M_{4,5}$ -edges of closed-shell transition metal and actinide compounds with different central atoms, ligands, and oxidation states can be obtained by means of 4c-DR-TDDFT. While the main absorption lines do not change noticeably with the basis set and geometry, the exchange-correlation functional has a strong influence with hybrid functionals performing the best. The energy shift compared to the experiment is shown to depend linearly on the amount of Hartree-Fock exchange with the optimal value being 60% for spectral regions above 1000 eV, providing relative errors below 0.2% and 2% for edge energies and SO splittings, respectively. Finally, the methodology calibrated in this work is used to reproduce the experimental $L_{2,3}$ -edge X-ray absorption spectra of $[\text{RuCl}_2(\text{DMSO})_2(\text{Im})_2]$ and $[\text{WCl}_4(\text{PMePh}_2)_2]$, and resolve the broad bands into separated lines, allowing an interpretation based on ligand field theory and double point groups. These results support 4c-DR-TDDFT as a reliable method for calculating and analyzing X-ray absorption spectra of chemically interesting systems, advance the accuracy of state-of-the-art relativistic DFT approaches, and provide a reference for benchmarking more approximate techniques.

4c-DR-TDDFT

- ✓ scalar relativistic effects
- ✓ spin-orbit coupling
- ✓ direct access to X-ray spectra
- ✓ large systems
- ✓ interpretation



1. INTRODUCTION

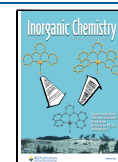
X-rays were included in the toolbox of chemists shortly after their discovery by Röntgen¹ and are used to probe both the molecular structure in diffraction experiments as well as the electronic structure in absorption, emission, and scattering X-ray spectroscopies. The wavelengths of X-rays are comparable to molecular dimensions, allowing the local electronic structure via excitations from localized core orbitals to be probed. X-ray spectroscopies thus offer high spatial resolution as well as elemental sensitivity due to the large energy separation of core levels in different atoms.² In addition, recent years have seen a surge in the development of X-ray instrumentation in the form of fourth-generation synchrotron facilities, including X-ray free-electron lasers producing intense short-duration pulses as well as tabletop X-ray sources via high-harmonic generation.^{3,4} These advances drive the widespread adoption of X-ray spectroscopies and, in turn, prompt the development of computational methods capable of accurately predicting and interpreting both standard and novel X-ray experiments.

In X-ray absorption spectroscopy (XAS), the spectrum is characterized by absorption edges, i.e., abrupt onsets of

absorption at resonant energies corresponding to inner-shell excitations. The spectral features close to the absorption edge are part of the near-edge X-ray absorption fine structure (NEXAFS), also known as X-ray absorption near-edge structure (XANES). Higher-energy signals constitute extended X-ray absorption fine structure (EXAFS) spectra that are characterized by weak oscillations originating from resonances in absorptions beyond the ionization energy.⁵ While XANES is used to determine the details of the electronic structure, such as oxidation states, EXAFS provides more information about the geometry around the absorbing center than about the electronic structure. In addition, low-intensity pre-edge peaks arising from excitations to singly occupied molecular orbitals may appear, particularly in transition-metal complexes.⁶ In

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recent years, techniques for high-resolution XANES⁷ have emerged including high-energy-resolution fluorescence detected XAS (HERFD-XAS),^{8,9} high energy resolution off-resonant spectroscopy (HEROS),^{10,11} and improved detectors.^{12–14}

A prerequisite for the reliable quantum-chemical modeling of X-ray spectroscopic processes is the inclusion of relativistic effects defined as differences between the full relativistic description of matter and an approximate Schrödinger equation-based description. This requirement stems from the fact that the inner-shell orbitals involved in XAS processes are most affected by relativity, manifestations of which are frequency shifts of spectral lines due to the scalar relativistic effects as well as spectral fine structure splitting arising from the spin–orbit (SO) coupling.^{15–18} The relativistic effects are significant even in light (third row) elements, highlighting the need for a relativistic description also in these cases,¹⁸ where perturbative treatment of SO coupling can yield accurate spectra,¹⁹ and increase in importance for heavier elements.²⁰ In K-edge spectra originating from excitations from $1s_{1/2}$ orbitals, only the scalar relativistic corrections have nonzero contributions and result in a constant shift of K-edge signals. In this case, one-component scalar relativistic Hamiltonians are convenient and sufficient for describing this XAS edge. On the other hand, XAS spectra near L- and M-edges originate from excitations from inner-shell atomic-like p and d orbitals split by the SO interaction into $p_{1/2}$ and $p_{3/2}$ or $d_{3/2}$ and $d_{5/2}$ levels, respectively. As a consequence of the SO splitting, the use of multicomponent, i.e., two-component (2c) or four-component (4c), relativistic Hamiltonians is mandatory to correctly assign X-ray spectra near L- and M-edges.^{18,21} Here, the 4c methodology based on the one-electron Dirac Hamiltonian combined with the instantaneous two-electron Coulomb interaction represents the “gold standard” of relativistic quantum chemistry, since all essential scalar and SO effects are included nonperturbatively.²² This is, in particular, important for L-edge XAS, which displays higher resolution due to higher intensities and longer core-hole lifetimes, and is therefore a popular technique in the study of transition metal complexes and solid-state materials.²¹ Further spin-related contributions can be accounted for by the inclusion of the Gaunt term that has been shown to contribute to the energy shifts of core orbitals.^{20,23}

When considering electronic structure models, a wide range of methods, including post-Hartree–Fock methods and Kohn–Sham density functional theory (DFT), have been developed and applied to XAS. For a comprehensive account of quantum-chemical methods addressing X-ray spectroscopies, we refer to recent reviews.^{24–27} Since our goal is to target large systems such as heavy-metal complexes, we focus on relativistic DFT that favorably combines computational cost and accuracy. There are two principal categories of DFT for XAS: (a) Δ SCF that adapts ground-state SCF optimization for core-hole electronic configurations;²⁸ (b) time-dependent DFT (TDDFT) that describes the response of molecular systems to external X-ray radiation by solving the time-dependent Kohn–Sham (TDKS) equation.²⁹ The latter can further be approached in three different ways: real-time TDDFT (RT-TDDFT),^{30,31} linear response TDDFT (LR-TDDFT),^{32,33} and damped response TDDFT (DR-TDDFT).^{34–36}

Of these, the RT-TDDFT solves the TDKS equation for a molecule subjected to an external electromagnetic pulse by

direct integration in the time domain^{37,38} and has been recently extended into the relativistic domain at both 4c^{39,40} and 2c exact two-component (X2C)^{41,42} level of theory. The spectrum is then obtained by transforming the induced electric dipole moment recorded during the simulation into the frequency domain. While the method holds promise for describing strong-field and time-resolved processes, its relatively high computational cost has so far prevented its widespread use for calculating X-ray spectra even though pioneering studies have been reported at both nonrelativistic⁴³ and relativistic levels of theory.^{18,44}

The next two approaches are based on perturbation theory. The foundation of LR-TDDFT is an eigenvalue equation (the Casida equation) yielding excitation energies as the eigenvalues and transition amplitudes as the eigenvectors. The linear response to an external field as well as an absorption spectrum can then be evaluated from these excitation energies and transition amplitudes. It is a popular approach due to the availability of efficient algorithms.^{45–50} However, using the well-known Davidson algorithm,⁵¹ the calculation of excitation energies proceeds from the lowest (valence) excitations, making such an approach to X-ray spectra prohibitively expensive. To mitigate these challenges, core–valence separation (CVS), also referred to as restricted excitation window (REW), techniques were developed in which only a subset of orbitals is considered.^{52–59} It has been shown that CVS causes only negligible errors.^{59,60} Applications of relativistic LR-TDDFT with variational SO interactions and focused on XAS have been reported at the level of the two-component zeroth-order regular approximation (ZORA) Hamiltonian⁶¹ as well as the X2C Hamiltonian.⁶²

Finally, DR-TDDFT (also called the complex polarization propagator (CPP) approach^{34–36}) describes the response of molecular systems to electromagnetic radiation directly in the frequency domain while focusing only on the spectral range of interest and, in addition, including relaxation effects by means of a damping parameter. By this means, the full complex response tensor covering both scattering and absorption processes is calculated. As such, DR-TDDFT is readily applicable for high-frequency (X-ray) or high density-of-states spectral regions that may otherwise prove challenging for methods like LR-TDDFT or RT-TDDFT, and so, it is well suited for XAS spectra of large molecules; therefore, it is the method of choice in this work. Here, we rely on our recent implementation of DR-TDDFT at the 4c relativistic level of theory.⁶³ Previous XAS applications of the 4c-DR-TDDFT have been reported to study the L₃-edge of UO₂²⁺⁶⁴ as well as XAS of carbon, silicon, germanium, and sulfur compounds.⁶⁵ In addition, a damped response Bethe–Salpeter equation at the X2C relativistic theory has been recently presented and applied.⁶⁶

When applied to X-ray spectra, DFT is known to suffer from frequency shifts with respect to experimental results, commonly attributed to self-interaction errors.⁶⁷ An established procedure for improving the performance of DFT is to use hybrid exchange–correlation (xc) functionals with an increased amount of exact Hartree–Fock exchange (HFX).^{68–70} Particularly good results have been achieved with B3LYP and B^{0.58}LYP, i.e., variants of B3LYP with 50% and 58% of HFX, respectively. In contrast, one study has suggested a smaller amount of HFX.⁷¹ A similar prescription in range-separated functionals is to increase the asymptotic amount of HFX in CAM-B3LYP from the usual 65% to

100%.^{70,72} Efforts have also been spent on developing special functionals and computational schemes for X-ray spectra, such as short-range corrected functionals,^{6,26} the long- and short-range corrected method LCGau-BOP,⁷³ core–valence⁷⁴ and core–valence–Rydberg functionals,^{75,76} or a many-body perturbation theory corrected LR-TDDFT⁷⁷ as well as a combination of restricted open-shell configuration interaction singles (ROCIS) and density functional theory.^{78,79} However, the majority of these studies relied on nonrelativistic, atomic orbital energy-corrected or scalar-relativistic calculations and focused predominantly on K-edges of light elements.

In the present work, we focus on the fully relativistic Dirac–Coulomb Hamiltonian-based 4c-DR-TDDFT level of theory and investigate the role of HFX in global hybrid functionals for reliable relativistic modeling of XAS spectral shifts and shapes. Because our approach is inherently *relativistic* and includes both *scalar and spin–orbit coupling effects variationally*, there is no longer a need to shift the absorption energies to compensate for the lack of relativistic corrections, allowing us to disentangle the contributions from relativity and the electronic structure model and thus avoiding accidental error cancellations. By considering transition metal and actinide compounds with different central atoms, ligands, and oxidation states and calibrating for other calculation parameters, including the molecular geometry and basis set, we propose an optimized computational protocol for calculating XAS spectra near L_{2,3}- and M_{4,5}-edges using 4c-DR-TDDFT. This is then applied to resolve XAS spectra of larger Ru and W complexes with up to 60 atoms.

The structure of this Article is as follows. Section 2 contains a brief summary of the 4c damped response TDDFT theory. Section 3 presents the computational details, and our results are presented in Section 4, first for the calibration set in Section 4.1 and then for the larger molecular systems in Section 4.2. The paper ends with some concluding remarks in Section 5.

2. THEORY

The linear response of a molecular system exposed to an external electric field (\mathbf{E}) of angular frequency (ω) is represented by the complex polarizability tensor ($\boldsymbol{\alpha}$) that parametrizes the induced electric dipole moment [$\boldsymbol{\mu}^{\text{ind}}(\omega)$]

$$\boldsymbol{\mu}_u^{\text{ind}}(\omega) = \alpha_{uv}(\omega)E_v(\omega) + \dots \quad (1)$$

The tensor $\boldsymbol{\alpha}$ is used to evaluate the dipole strength function as (in atomic units)

$$S(\omega) = \frac{4\pi\omega}{3c} \text{ImTr}[\boldsymbol{\alpha}(\omega)] \quad (2)$$

where c is the speed of light, Im denotes the imaginary part of the tensor, and Tr represents the trace over the Cartesian components. The function $S(\omega)$ defines the electronic absorption spectrum (EAS) across the entire frequency range, including those of relevance to XAS.

In DR-TDDFT, the $\boldsymbol{\alpha}(\omega)$ tensor components are calculated for a user-defined set of frequencies from the response vectors \mathbf{X} and \mathbf{Y} as

$$\alpha_{uv}(\omega) = X_{ai,v}(\omega)P_{ia,u} + Y_{ai,v}(\omega)P_{ai,u} \quad (3)$$

where \mathbf{P} is the matrix representation of the electric dipole moment operator. The indices u and v denote Cartesian components while a and i run over virtual and occupied

reference (ground-state) molecular orbitals (MO), respectively. Note that, in a 4c relativistic theory, index a runs in general over virtual positive-energy as well as negative-energy MOs. The response vectors are determined by solving the damped response equation^{63,80}

$$\left[\begin{pmatrix} \mathbf{A} & \mathbf{B} \\ \mathbf{B}^* & \mathbf{A}^* \end{pmatrix} - (\omega + i\gamma) \begin{pmatrix} \mathbf{1} & \mathbf{0} \\ \mathbf{0} & -\mathbf{1} \end{pmatrix} \right] \begin{pmatrix} \mathbf{X} \\ \mathbf{Y} \end{pmatrix} = - \begin{pmatrix} \mathbf{P} \\ \mathbf{P}^* \end{pmatrix} \quad (4)$$

where ω and γ are user-defined parameters specifying the external electric field frequency and a common relaxation (damping) parameter. The parameter γ models the finite lifetime of the excited states (corresponding to their inverse lifetimes) and leads to finite-width Lorentzian peaks in the spectra (with γ being the half width at half-maximum of the peaks). The right-hand side of eq 4 describes the interaction of the molecular system with the applied external electric field, which in the electric dipole approximation is mediated by the electric dipole moment operator \mathbf{P} . While the short wavelength of X-ray radiation may require terms beyond the electric dipole,^{81–83} we do not consider this aspect in the present study. Finally, the first term on the left-hand side of eq 4 is the generalized Hessian; for the Dirac–Coulomb Hamiltonian, it is defined by⁶³

$$\begin{aligned} A_{ai,bj} &= (\varepsilon_a - \varepsilon_i)\delta_{ab}\delta_{ij} + K_{\mu\nu,\lambda\tau}C_{\mu a}^*C_{\nu i}C_{\lambda j}^*C_{\tau b} \\ B_{ai,bj} &= K_{\mu\nu,\lambda\tau}C_{\mu a}^*C_{\nu i}C_{\lambda b}^*C_{\tau j} \end{aligned} \quad (5)$$

where ε_i and ε_a are the energies of occupied and virtual reference MOs, respectively, δ_{pq} is the Kronecker delta function ($\delta_{pq} = 1$ if $p = q$ and 0 otherwise), and

$$K_{\mu\nu,\lambda\tau}(\xi) = [\Omega_{\mu\nu}|\Omega_{\lambda\tau}] - \xi[\Omega_{\mu\tau}|\Omega_{\lambda\nu}] + K^{\text{xc}}(\Omega_{\mu\nu}, \Omega_{\lambda\tau}, \xi) \quad (6)$$

is the coupling matrix, with ξ denoting the admixture of HFX. In the expression for the coupling matrix, $[\mathbf{\Omega}|\mathbf{\Omega}]$ refers to the four-center electron repulsion integrals (ERIs) defined over quaternion overlap distribution functions $\Omega_{\mu\nu} = \Omega_{\mu\nu}(\mathbf{r}) \equiv \mathbf{X}_\mu^\dagger(\mathbf{r})\mathbf{X}_\nu(\mathbf{r})$ in terms of which one can design an efficient algorithm for the evaluation of relativistic ERIs facilitating quaternion algebra and restricted kinetic balance (RKB) conditions⁸⁴ for quaternion basis functions $\mathbf{X}(\mathbf{r})$.⁸⁵ The xc kernel (K^{xc}) in eq 6 is defined in our closed-shell DR-TDDFT implementation in a noncollinear fashion as described in ref 63. In addition, the adiabatic approximation⁸⁶ of TDDFT is assumed, resulting in a frequency-independent xc kernel. For more details of the relativistic 4c methodology including quaternion RKB basis, integral evaluation, and noncollinear xc potential and kernel as employed in the RESPECT program, we refer to ref 85.

The DR-TDDFT equation (eq 4) is solved using an iterative subspace algorithm that represents the response vectors in the form of the linear combination of trial vectors, since the size of the matrix on the left-hand side of the equation prohibits its direct inversion or the use of elimination techniques for realistic molecular systems. The iterative subspace solver adapted for relativistic 4c-DR-TDDFT requires a proper parametrization of the response equation based on hermiticity and time-reversal symmetry.^{63,87} Moreover, a suitable noncollinear kernel and careful control of the numerical precision of the algebraic operations are required to achieve stable convergence.⁶³ As indicated by eq 2, the frequency dependence of the spectral function enters via the response vectors.

Therefore, the DR-TDDFT equation, eq 4, has to be solved for each frequency within the spectral range of interest to obtain the corresponding response vectors. However, instead of solving each equation separately in a sequential manner, the DR-TDDFT solver in RESPECT works in a multifrequency regime that allows several frequencies (tens to hundreds) to be considered simultaneously in a common trial subspace, thus covering a large part of the spectrum in a single run and reducing the computational demands. The details of the solution of the DR-TDDFT equation for closed-shell systems as implemented in RESPECT can be found in ref 63.

An integral part of the DR-TDDFT calculations of X-ray spectra in atom-centered basis sets is an isolation of core-level excitations by means of a REW-like approach. This is due to intruder transitions arising from electronic excitations from valence (or higher-lying inner shells) to high-lying (above-ionization threshold) virtual orbitals, which are nonphysical in calculations employing finite atom-centered basis sets that cannot accurately describe continuum states. When these transitions fall into the spectral range of interest, they appear as artifacts in XAS simulations. While one way of identifying these transitions is to recalculate the spectra in different basis sets, as the spurious nonphysical peaks are much more sensitive to changes in the basis set, it is not considered practical and a molecular orbital-energy-based cutoff for virtual orbitals has been suggested instead.⁷² Moreover, the REW approach has been applied in nonrelativistic RT-TDDFT⁴³ where the same problem with spurious peaks appears. In the present DR-TDDFT work, we also employ a technique first introduced in the context of RT-TDDFT.¹⁸ It is based on changing the values of some elements of the electric dipole moment operator \mathbf{P} (on the right-hand side of eq 4). Namely, only those elements of the electric dipole moment operator $P_{\tilde{a}i}$ that correspond to the targeted core occupied orbitals \tilde{i} and sufficiently many virtual orbitals \tilde{a} to cover the desired spectral range are kept at their original value while the rest of the elements of \mathbf{P} are set to zero. Mathematically, the DR-TDDFT equation, eq 4, represents a large system of linear equations, and this prescription sets the right-hand side of some of these equations to zero while keeping these equations in the system and not removing them. The damped response equation is thus solved in its full dimensions, which preserves orbital relaxation effects. An interpretation of this procedure is that the nonphysical transitions in the spectral range of interest were artificially made dipole forbidden.

3. COMPUTATIONAL DETAILS

For the purpose of a benchmark and calibration study, a set of closed-shell heavy-metal compounds with available high-quality experimental data were selected. These involve 3d, 4d, 5d, and 5f elements with various electronic configurations of the central atom, namely, VOCl_3 , CrO_2Cl_2 , MoS_4^{2-} , WCl_6 , PdCl_6^{2-} , ReO_4^- , and $\text{UO}_2(\text{NO}_3)_2$. In addition, XAS spectra of larger systems, namely, $[\text{RuCl}_2(\text{DMSO})_2(\text{Im})_2]$ and $[\text{WCl}_4(\text{PMePh}_2)_2]$, with DMSO, Im, and Ph standing for dimethyl sulfoxide, imidazole, and phenyl, respectively, were calculated to assess the optimized computational protocol.

All molecular geometries were optimized using a protocol designed for transition metal complexes:^{88,89} PBE0 functional^{90–93} and def2-TZVPP basis sets⁹⁴ for all atoms (def-TZVP in the case of the uranium complex) with the corresponding effective core potentials (ECPs)⁹⁵ replacing 28 core electrons in 4d and 60 electrons in 5d and 5f elements using the TURBOMOLE quantum-chemical program.⁹⁶

All X-ray spectra were calculated using a damped response library⁶³ of the Relativistic Spectroscopy DFT program RESPECT⁸⁵ and uncontracted all-electron GTO basis sets. For the basis set calibration, we selected the uncontracted Dyall's VXZ ($X = \text{D}, \text{T}$)^{97–101} basis set for metals and the uncontracted Dunning's cc-pVXZ ($X = \text{D}, \text{T}$) and aug-cc-pVXZ ($X = \text{D}, \text{T}$)^{102–104} basis sets for light elements. For the calibration of exchange–correlation (xc) functionals, we tested the pure generalized gradient approximation (PBE^{90,91,93}), global hybrids (PBE0,^{90–93} B3LYP^{93,105–108}), global hybrids (B3LYP-XHF, PBE0-XHF) with variable exact-exchange admixture X (ranging from 0% to 60%), and range-separated hybrid (CAM-B3LYP^{95,105–109}) xc functionals. The numerical integration of the noncollinear exchange–correlation potential and kernel was done with an adaptive molecular grid of medium size (program default).

In all 4c calculations, atomic nuclei of finite size were approximated by a Gaussian charge distribution model.¹¹⁰ Moreover, the four-center two-electron repulsion integrals were treated within an atom-pair approximation where all integrals over the atom-centered small-component basis functions X^S were discarded unless the bra and ket basis pairs shared the same origin, i.e., $[\text{X}_A^S \text{X}_B^S | \text{X}_C^S \text{X}_D^S]_{\delta_{AB} \delta_{CD}}$. Excitations to virtual negative-energy states were neglected in the damped response calculations at the 4c relativistic level of theory (no-virtual-pair approximation). A validity test of this approximation is available in Section S1.1.6.

The damped linear response calculations covered the spectral regions with a resolution of 0.1 eV. When plotting the calculated spectra, smoothing by means of B-spline interpolation was used. All linear response calculations employed the multifrequency solver with 50 to 100 frequencies treated simultaneously. The damping/broadening parameter γ used in the damped response calculations was set to 0.15 eV when calibrating and when aiming for high-resolution spectra, while values taken from reference works were used to obtain wider peaks to facilitate the comparison with experimental line shapes, specifically (in eV): 0.5 for VOCl_3 and CrO_2Cl_2 , 2.0 for ReO_4^- , 0.4 and 1.6 for $\text{UO}_2(\text{NO}_3)_2$, and 3.0 for WCl_6 and $[\text{WCl}_4(\text{PMePh}_2)_2]$. For all calculations, the elements of the perturbation operator corresponding to the target occupied (p orbitals for L-edges, d orbitals for M-edges) and all virtual orbitals were preserved, while the remaining elements were discarded (zeroed out). Exceptions were PdCl_6^{2-} and $\text{UO}_2(\text{NO}_3)_2$ where only a subset of the core p and d orbitals was maintained as discussed in detail in Section S1.1.4.

4. RESULTS AND DISCUSSION

4.1. Calibration. In this section, we first investigate the role of the molecular geometry, basis set, and exchange–correlation functional for 4c relativistic DR-TDDFT calculations of XAS spectra. On the basis of this calibration study, we determine a computational protocol that is subsequently validated on larger molecular systems and used to resolve broad signals in their experimental XAS spectra, thus providing their ligand field theory-based interpretation.

4.1.1. Role of Geometry Optimization. We first briefly assess whether to use optimized or experimental geometries. MoS_4^{2-} has one of the largest differences between the X-ray structure and the geometry optimized at the PBE0/TZVPP level of theory of the whole test set and was therefore selected for comparing calculated XAS spectra at these two geometries. Whereas the experimental X-ray structure has C_{3v} symmetry with Mo–S bonds of 2.193 and 2.172 Å as a result of crystal packing, the PBE0/TZVPP geometry was optimized in vacuo and has T_d symmetry with all Mo–S bond lengths being 2.193 Å. The $M_{4,5}$ - and $L_{2,3}$ -edge spectra were calculated using the PBE0 functional and the uncontracted Dyall's VDZ basis set for Mo and the uncontracted Dunning's aug-cc-pVDZ basis for sulfur. The differences between the X-ray and optimized structure in the L- and M-edge spectra were negligible with no

Table 1. XAS Main Lines (in eV) from 4c-DR-TDDFT (PBE0) Calculations Using Different Basis Sets^a

		VDZ/VDZ	VDZ/aVDZ	VTZ/VTZ	VTZ/aVTZ
VOCl ₃	L ₃	507.5	507.4	507.5	507.4
	L ₂	514.2	514.2	514.2	514.3
CrO ₂ Cl ₂	L ₃	571.4	571.4	571.5	571.6
	L ₂	579.5	579.5	579.5	579.5
MoS ₄ ²⁻	L ₃	2489.4	2489.3	2489.3	2489.3
	L ₂	2595.9	2595.9	2596.0	2595.9
	M ₅	225.5	225.4	225.4	225.4
	M ₄	228.8	228.7	228.7	228.7
PdCl ₆ ²⁻	L ₃	3138.2	3138.2	3138.2	3138.2
	L ₂	3297.4	3297.4	3297.6	3297.6
WCl ₆	L ₃	10139.9	10139.9	10139.8	10139.8
	L ₂	11492.7	11492.7	11492.7	11492.7
ReO ₄ ⁻	L ₃	10472.0	10472.0	10472.0	10472.0
	L ₂	11912.0	11911.9	11912.0	11912.0
UO ₂ (NO ₃) ₂	M ₅	3515.3	3515.3	3515.3	3515.3
	M ₄	3693.2	3693.2	3693.2	3693.2

^aBasis set notation is defined in Section 4.1.2.

significant differences in positions and intensities of the main absorption bands. Some minor peaks of low-intensity in the M-edge spectra were shifted by ~ 0.1 eV, which is at the limits of the numerical accuracy of our calculations (figures with the calculated XAS spectra are available in Section S1.1.1). Since the calculated XAS spectra show only a minor dependence on the choice of geometry, including differences in symmetry, PBE0/TZVPP-optimized geometries were used in all subsequent calculations.

4.1.2. Role of Basis Set. The effect of the basis set on XAS spectra was investigated by comparing calculations performed with different uncontracted Dyll's VXZ (X = D, T) basis sets for the central heavy-metal atoms and with different uncontracted Dunning's cc-pVXZ and aug-cc-pVXZ (X = D, T) basis sets for the ligand atoms. The following basis combinations were selected: VDZ/VDZ, VDZ/aVDZ, VTZ/VTZ, and VTZ/aVTZ, where the first basis refers to the central heavy atom and the second, to the remaining light elements, while the acronym "a" stands for basis set augmentation.

The results for the main absorption bands are collected in Table 1, and the selected spectra (VOCl₃, MoS₄²⁻, WCl₆) are shown in Figures 1–3. These results show that neither

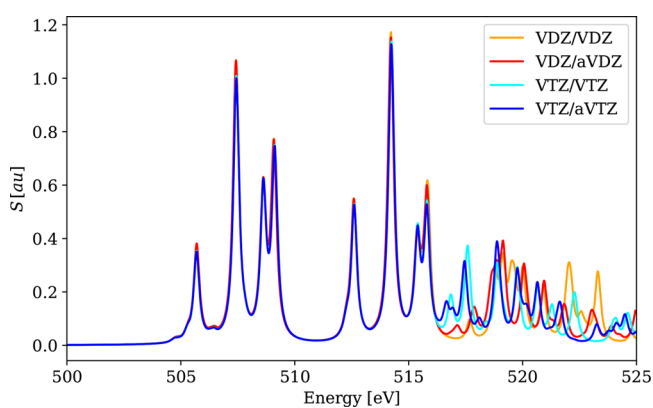


Figure 1. Calculated 4c-DR-TDDFT (PBE0) XAS spectra near vanadium L_{2,3}-edges and oxygen K-edges of VOCl₃ using different basis sets. Basis set notation is defined in Section 4.1.2.

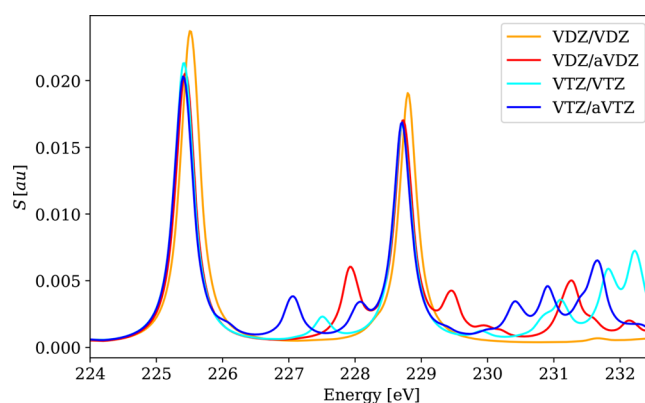


Figure 2. Calculated 4c-DR-TDDFT (PBE0) XAS spectra near molybdenum M_{4,5}-edges of MoS₄²⁻ using different basis sets. Basis set notation is defined in Section 4.1.2.

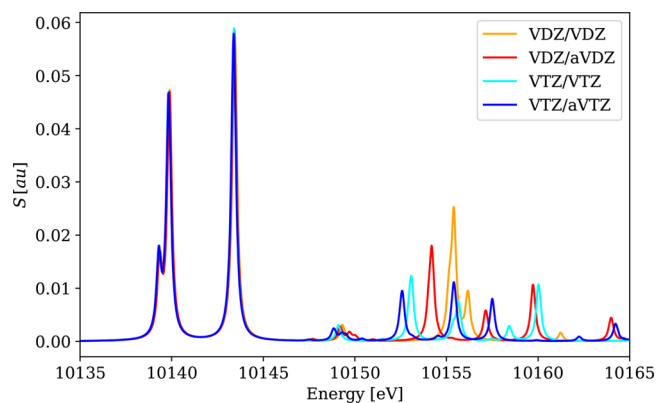


Figure 3. Calculated 4c-DR-TDDFT (PBE0) XAS spectra near the tungsten L₃-edge of WCl₆ using different basis sets. Basis set notation is defined in Section 4.1.2.

increasing the basis set size from VDZ to VTZ nor augmentation has any significant (>0.1 eV) effect on the positions of the main absorption peaks. However, the number of minor low-intensity signals increases with the size of the basis set, and notable differences are also observed in high-frequency parts of the plotted spectra. However, in some cases,

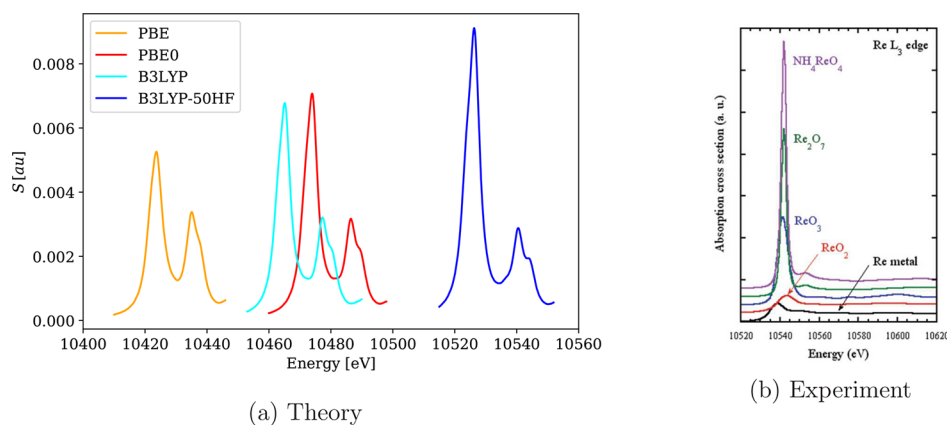


Figure 4. Calculated 4c-DR-TDDFT (VDZ/aVDZ, $\gamma = 2.0$) XAS spectra near the rhenium L_3 -edge of ReO_4^- using different xc functionals and their comparison with experimental results.¹¹¹ (a) Theory and (b) experiment (reprinted from ref 111 with permission from APS).

Table 2. XAS Main Lines (in eV) from 4c-DR-TDDFT (VDZ/aVDZ) Calculations Using Different xc Functionals As Well As Differences between L_2 - and L_3 -Edges (M_4 - and M_5 -Edges) Corresponding to SO Splitting and Their Comparison with Existing Experimental Results

		exp. ^a	PBE	PBE0		B3LYP		CAM-B3LYP
				25HF	40HF	20HF	50HF	
VOCl_3	L_3	516.9	499.2	507.5	512.1	506.0	515.6	506.0
	L_2	523.8	505.9	514.2	518.9	512.8	522.5	512.8
	L_2-L_3	6.9	6.7	6.7	6.9	6.8	6.9	6.8
CrO_2Cl_2	L_3	579.9	562.2	571.4	576.6	569.8	580.4	569.8
	L_2	588.5	570.8	579.5	584.8	577.9	588.7	577.9
	L_2-L_3	8.6	8.6	8.1	8.2	8.1	8.3	8.1
MoS_4^{2-}	L_3	2521.7	2466.9	2489.3	2502.9	2485.4	2513.2	2485.1
	L_2	2626.0 ^b	2572.6	2595.9	2609.6	2591.9	2619.9	2591.6
	L_2-L_3	104.3	105.7	106.6	106.7	106.5	106.7	106.5
	M_5	228.7	220.1	225.4	228.9	224.3	231.2	224.7
	M_4	231.7	223.4	228.7	232.2	227.6	234.5	228.0
PdCl_6^{2-}	M_4-M_5	3.0	3.3	3.3	3.0	3.3	3.3	3.3
	L_3	3177.8	3112.5	3138.2	3155.0	3133.8	3164.8	3133.3
	L_2	3334.7	3271.6	3297.4	3312.7	3293.0	3324.4	3292.5
WCl_6	L_2-L_3	156.9	159.1	159.2	157.7	159.2	159.6	159.2
	L_3	10212.2	10090.8	10139.8	10168.6	10130.7	10191.0	10130.0
	L_2	11547.0	11442.8	11492.8	11522.4	11483.6	11548.9	11483.0
ReO_4^-	L_2-L_3	1334.8	1352.0	1353.0	1353.8	1352.8	1354.1	1353.0
	L_3	10542.0	10422.0	10472.0	10504.0	10463.0	10524.0	10462.0
	L_2	–	11861.3	11911.9	11942.1	11903.2	11965.3	11902.0
$\text{UO}_2(\text{NO}_3)_2$	L_2-L_3	–	1439.3	1439.9	1438.1	1431.2	1441.3	1441.0
	M_5	–	3490.1	3515.3	3530.2	3510.6	3540.6	3509.9
	M_4	3727.0	3667.8	3693.2	3708.2	3688.5	3718.7	3687.8
	M_4-M_5	–	177.7	177.9	178.0	177.9	178.1	177.9

^aExperimental references: VOCl_3 , ref 61; CrO_2Cl_2 , ref 61; MoS_4^{2-} , ref 120; PdCl_6^{2-} , ref 112; WCl_6 , ref 121; ReO_4^- , ref 111; $\text{UO}_2(\text{NO}_3)_2$, ref 122.

^bValue taken from Figure 3 in ref 120, rather than Table 1 *ibid.* due to a misprint.

such as the W L_3 -edge in WCl_6 (Figure 3), these minor peaks lie above the ionization limit and are therefore *not* part of the NEXAFS spectral region. It is therefore advisable to analyze the spectral regions above the ionization limits with caution, in particular in cases when calculations were performed with conventional atom-centered basis sets. Nevertheless, the NEXAFS region of WCl_6 can be considered as being equally well described in all tested basis sets. The VDZ/aVDZ combination was therefore selected for further calculations because (i) VDZ-based calculations reproduce the main absorption line(s) of the VTZ ones well, but with significant computational savings, (ii) the use of the aVDZ basis for light

atoms provides somewhat better agreement with the reference VTZ-based calculations; see for instance, the comparison of the results for different basis sets in the $M_{4,5}$ absorption edges of MoS_4^{2-} in Figure 2.

4.1.3. Role of xc Functional Type. Using the VDZ/aVDZ basis set, we calculated the XAS spectra of the test systems using the PBE, PBE0, B3LYP, B3LYP-50HF, and CAM-B3LYP xc functionals. Unlike for the basis sets, the choice of xc functional significantly affects the position of the absorption edges, as illustrated for the rhenium L_3 absorption edge of ReO_4^- in Figure 4. The positions of absorption line maxima observed for the tested functionals are reported in Table 2. We

see that the calculated results in general underestimate the excitation energies, where PBE provides the worst estimate of the spectral line positions. Significant improvements are achieved by hybrid functionals with the best estimate being given by B3LYP-50HF. Moreover, the range-separated CAM-B3LYP functional leads to almost identical findings as its global hybrid counterpart B3LYP.

Because the choice of xc functional affects the positions of absorption lines, it is of interest to investigate whether the spin-orbit (SO) splitting of core p and d orbitals, represented by the relative positions of L_2 vs L_3 and M_4 vs M_5 absorption edges, changes with xc functional as well. The calculated SO splittings are reported in Table 2. These results show that the experimental SO splittings are in general well reproduced and all xc functionals perform equally well. These results suggest that the correct description of the SO splitting can be ascribed to the relativistic 4c nature of the Hamiltonian used, whereas incorrect absolute positions of absorption edges are likely due to a self-interaction error, a shortcoming of the GGA and hybrid functionals with smaller amounts of HFX.

The choice of xc functional also affects the overall shape of the spectra, as shown in Figures 4, 5, and 6. In particular, the

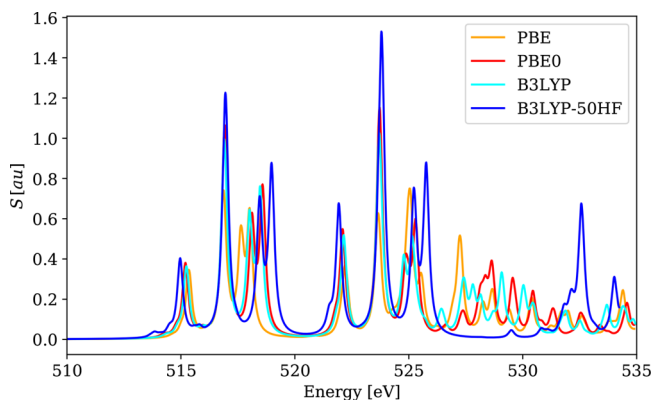
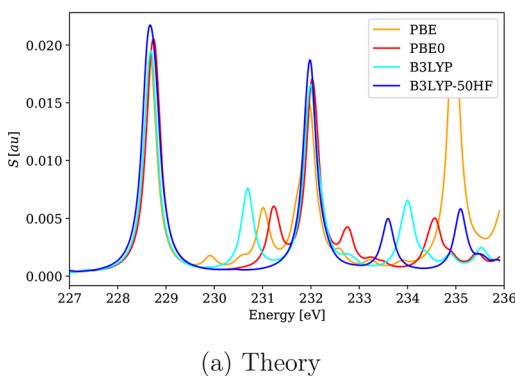
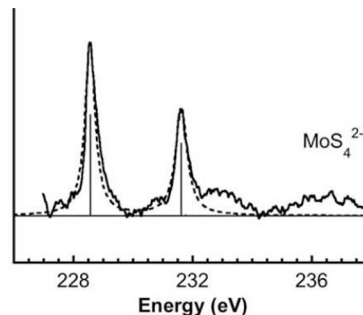


Figure 5. Calculated 4c-DR-TDDFT (VDZ/aVDZ) XAS spectra near vanadium $L_{2,3}$ -edges and oxygen K-edges of VOCl_3 using different xc functionals. To ease comparison, the spectra were shifted so that the L_3 -line maxima are centered on the experimental value.

PBE functional reproduces both energies (see Table 2) and intensities of pre-edge signals poorly with respect to experimental spectra, in addition to overestimating the



(a) Theory



(b) Experiment

Figure 6. Calculated 4c-DR-TDDFT (VDZ/aVDZ) XAS spectra near molybdenum $M_{4,5}$ -edges of MoS_4^{2-} using different xc functionals and their comparison with experimental results.¹²⁰ To ease comparison, the spectra were shifted so that the M_5 -line maxima are centered on the experimental value. (a) Theory and (b) experiment (reprinted from ref 120 with permission from Elsevier).

intensities of the peaks above the edge. This seems to be the case for all GGA functionals; see for instance, the BLYP spectra in Figure S2. Moreover, the range-separated hybrid CAM-B3LYP functional provides spectra similar to global hybrids with smaller admixtures of HFX (B3LYP, PBE0), as shown in Figures S3–S5. The only exception is the $M_{4,5}$ spectrum of MoS_4^{2-} , where the low-frequency minor peaks are not present in the CAM-B3LYP spectrum, thus mirroring the B3LYP-50HF spectrum.

Overall, the functional with the highest amount of HFX (B3LYP-50HF) was found to reproduce experimental spectra the best not only in terms of the lowest absolute energy shift but also in terms of relative signal intensities and positions of minor signals. The correct reproduction L_3/L_2 intensity ratio was investigated for the PdCl_6^{2-} complex, where the value observed in the experiment¹¹² is close to the theoretical predicted ratio of 2:1.⁷ Figure 7 shows the main peaks near

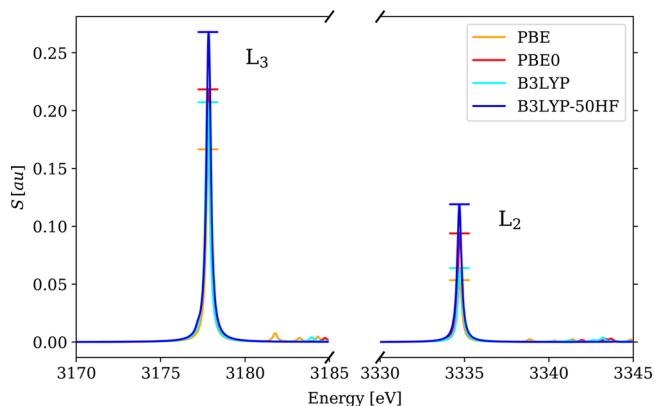


Figure 7. Calculated 4c-DR-TDDFT (VDZ/aVDZ) XAS spectra near palladium $L_{2,3}$ -edges of PdCl_6^{2-} using different xc functionals. To ease comparison, the spectra were shifted so that the maxima of the main lines are centered on the experimental values. The markers denote the intensities of the main lines.

palladium L_3 and L_2 absorption edges in PdCl_6^{2-} . The expected intensity ratio of $L_3/L_2 = 2:1$ is correctly reproduced only by B3LYP-50HF, while other functionals yield ratios of 3:1 or even 4:1. Note, however, that branching ratios often differ from expected statistical ratios for a number of reasons.^{113,114} Similarly, the rhenium L_3 absorption edge in ReO_4^- (Figure 4) has a significantly more intense main line

than the only secondary peak for B3LYP-50HF, thus resulting in spectra more consistent with the experiment. Furthermore, spectra calculated with B3LYP-50HF also agree better with the experiments in the fine structure of the spectra; see for example, XAS near the molybdenum $M_{4,5}$ -edges of MoS_4^{2-} in Figure 6, where spectra calculated with other functionals contain minor signals absent in the experimental data. This agrees with earlier observations of the good performance of B3LYP-50HF for core excitations⁷⁰ and led us to perform an additional investigation of the role of HFX in xc functionals.

There exists a good physical ground for the observed trend, which is related to theoretical conditions imposed on xc functionals for several limiting cases. Of relevance for core-level spectroscopies is the high-density limit,^{115,116} which relates to the homogeneous coordinate scaling of the xc functional in the limit of an infinitely large density. In this limit, the exchange energy scales linearly, whereas the correlation energy is known to scale to a finite constant.¹¹⁷ Thus, the correlation energy becomes negligible in the high-density limit compared to the exchange energy. In fact, in regions dominated by exchange, that is, where the correlation contribution is considerably smaller than the exchange contribution, the cancellation of self-interaction error (SIE) predominates over the consideration of the nondynamical correlation. Therefore, global hybrid functionals meant to improve the description of core excitations require an alteration in their parametrization, in particular, regarding the amount of admixed exact exchange. Hence, the scaling of HFX can be viewed as correcting for SIE, albeit not entirely satisfying the high-density limit.¹¹⁸ A further step to improve this description requires the development and implementation of more sophisticated local hybrid functionals^{118,119} or orbital-specific hybrid functionals such as CVR-B3LYP^{74,75} that, in principle, can satisfy the limiting case. However, the implementation and validation of these specific functionals are beyond the scope of the present work.

4.1.4. Role of the Amount of HF Exchange. In order to determine the dependence of the XAS spectra on the amount of HFX and to see whether there is an optimal value that best reproduces experimental main lines, we investigated the series of functionals derived from PBE0 and denoted here as PBE0-XHF where $X = 0, 25,$ and 40 . This series was selected due to its good and reliable performance in calculations of the properties of transition metal systems, requiring typically more HFX than the standard PBE0 parametrization.^{88,89,123} We also explored the effect of different amounts of HFX in the CAM-B3LYP functional, going from 65% to 100%. However, this modified range-separated functional gave results almost identical with the original CAM-B3LYP functional and was therefore not pursued any further; see Figures S3–S5. The final results are summarized in Table 2, and the dependence of the relative shift, defined as $(E_{\text{Theory}} - E_{\text{Exp}})/E_{\text{Exp}}$, on the amount of HFX is plotted in Figure 8. The figure also includes B3LYP with its standard parametrization of 20% HFX as well as B3LYP-50HF and shows that the relative shift depends linearly on the percentage of HFX, regardless of the type of functional used. Therefore, the most important parameter determining the relative shift remains the amount of HFX, not the type of functional. On the basis of this finding, we determined an optimal amount of HFX (rounded to tens) that best reproduces the experimentally observed position of the main absorption edges. The results obtained with these

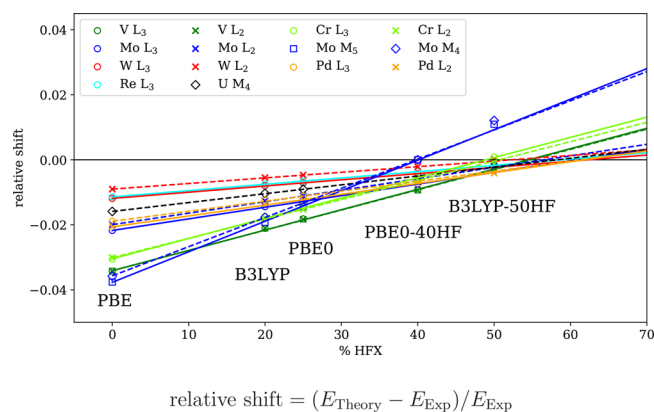


Figure 8. Relative shifts of spectral lines as functions of the percentage of HFX in a functional. For each molecule, a linear fit describes this dependence well and is used to estimate an optimal amount of HFX.

optimal values of HFX together with the errors with respect to the experiments are collected in Table 3.

The optimal amount of HFX is partially dependent on the frequency (energy) of the absorption in question. For

Table 3. XAS Main Lines (in eV) As Well As Differences between $L_{2,3}$ - and $M_{4,5}$ -Edges Corresponding to SO Splitting, As Obtained from Experiments and 4c-DR-TDDFT (VDZ/aVDZ) Calculations Using the PBE0-XHF Functional, where X Is the Determined Optimal Admixture of HFX

		exp. ^a	PBE0-XHF		
			X	energy	error
VOCl ₃	L ₃	516.9	50	515.2	-1.7
	L ₂	523.8	50	522.0	-1.8
	L ₂ -L ₃	6.9		6.8	-0.1
CrO ₂ Cl ₂	L ₃	579.9	50	580.0	0.1
	L ₂	588.5	50	588.2	-0.3
	L ₂ -L ₃	8.6		8.2	-0.4
MoS ₄ ²⁻	L ₃	2521.7	60	2523.1	1.4
	L ₂	2626.0 ^b	60	2627.6	1.6
	L ₂ -L ₃	104.3		104.5	0.2
	M ₅	228.7	40	228.9	0.2
	M ₄	231.7	40	232.2	0.5
PdCl ₆ ²⁻	M ₄ -M ₅	3.0		3.3	0.3
	L ₃	3177.8	60	3173.4	-4.4
WCl ₆	L ₂	3334.7	60	3332.9	-1.8
	L ₂ -L ₃	156.9		159.5	2.6
	L ₃	10212.2	60	10207.3	-4.9
ReO ₄ ⁻	L ₂	11547.0	60	11561.7	14.7
	L ₂ -L ₃	1334.8		1354.4	19.6
	L ₃	10542.0	60	10541.0	-1.0
UO ₂ (NO ₃) ₂	L ₂	-	60 ^c	11982.1	-
	L ₂ -L ₃	-		1441.1	-
	M ₅	-	60 ^c	3549.9	-
PdCl ₆ ²⁻	M ₄	3727.0	60	3728.0	1.0
	M ₄ -M ₅	-		178.1	-

^aExperimental references: VOCl₃, ref 61; CrO₂Cl₂, ref 61; MoS₄²⁻, ref 120; PdCl₆²⁻, ref 112; WCl₆, ref 121; ReO₄⁻, ref 111; UO₂(NO₃)₂, ref 122. ^bValue taken from Figure 3 in ref 120, rather than Table 1 *ibid.* due to a misprint. ^cSince an experimental reference was not available, we selected 60% HFX as the most likely optimal value on the basis of other spectra in the calibration.

absorption edges above 1000 eV, which include the heavy-element L_2 - and L_3 -edges and the uranium M_4 -edge, the optimal amount of HFX turned out to be 60%. In the case of WCl_6 , the optimal amount was 60% for the L_3 -edge and 50% for the L_2 -edge due to a slightly larger error in the SO splitting and the missing Gaunt term, which was compensated in the fitting procedure by different amounts of HFX. Therefore, we adopt a single value of 60% for the amount of HFX as this provides the best agreement with the experiment across the board, although in some cases, the separation of signals within one spectral range increases with the amount of HFX. While the absolute errors in the W L_2 -edge of WCl_6 as well as the $L_2 - L_3$ difference with 60% HFX are larger than in all other systems, the relative error remains below 0.2% for absorption line energies and below 2% for the SO splitting, which is a very good result in the context of DFT calculations. This amount of HFX admixture is therefore used in the remaining calculations of heavy-element XAS spectra above 1000 eV.

Whereas 60% of HFX seems to be quite robust for high-energy spectra, caution should be taken for spectral ranges below 1000 eV, where the optimal amount varies from 50% for V $L_{2,3}$ -edges in $VOCl_3$ and CrO_2Cl to 40% for Mo $M_{4,5}$ -edges in MoS_4^{2-} . The optimal amount of HFX seems to scale with energy as indicated by 40% needed for ~ 200 eV edges and 50% for 500–550 eV edges, suggesting that a simple, e.g., linear, prescription for lower X-ray energies exists, but its exact determination requires further studies. By using a fully relativistic theory and a single optimal amount of HFX for selected energy ranges, we avoid the need for empirical shifts of each spectrum to match the corresponding experimental reference. Such a simple computational prescription offers a very satisfactory agreement between calculated and experimental results. This is demonstrated in Figure 9, and similarly, no shifts are applied to calculated spectra presented onward when comparing them to the experiments.

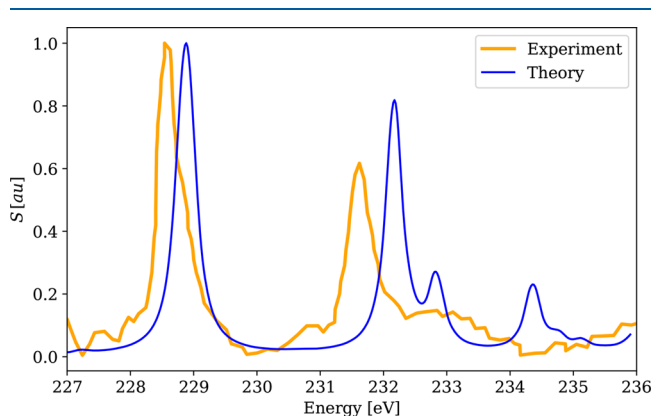


Figure 9. Calculated 4c-DR-TDDFT (PBE0-40HF, VDZ/aVDZ) XAS spectrum near molybdenum $M_{4,5}$ -edges of MoS_4^{2-} and its comparison with the experimental results.¹²⁰ The spectra were normalized by setting the maximum to unity. No shift on the energy axis was applied.

4.1.5. Role of DR-TDDFT Damping Parameter. One of the characteristic features of DR-TDDFT is its ability to directly calculate the spectral function for the frequencies of interest without the need to determine the excitation energies–eigenvalues of the Casida equation and their corresponding eigenvectors. The line shape of the spectrum is governed by the damping parameter γ in eq 4 that corresponds to the half

width at half-maximum of a Lorentzian peak and models the finite lifetimes of the excited states. Since DR-TDDFT does not provide a means for determining this parameter, a single user-defined damping parameter is used in practice, thus assuming the same lifetime for all excited states that relax back to the electronic ground state. The use of values from available experimental compendia of core-hole lifetimes thus offers a simple way of reproducing experimental lineshapes. Moreover, a decrease in the damping parameter serves as a theoretical tool to obtain narrow peaks with better resolution and thus eases the interpretation of the experimental spectra. An example is the determination of crystal field splitting where the calculation can complement the determination based on second derivatives of experimental spectra. Examples of spectra calculated with different values of γ are shown for $VOCl_3$ and CrO_2Cl_2 in Figure 10 and for $UO_2(NO_3)_2$ in Figure 11. These spectra were calculated using the optimal HFX admixture determined in the previous section, i.e., 50% for $VOCl_3$ and CrO_2Cl_2 and 60% for $UO_2(NO_3)_2$. Since the damping parameter affects the peak magnitudes, spectra calculated with different values of the damping parameter were normalized by setting their maximum to unity to ease their side-by-side comparison. Reference experimental spectra are well reproduced by the calculations, particularly in terms of absorption energies and overall lineshapes. The comparison of calculated $VOCl_3$ and CrO_2Cl_2 spectra with the experiment in Figure 10 also demonstrates that different damping parameters may be applied for the L_2 - and L_3 -edges to achieve even better agreement. Particularly, in heavier complexes, individual edges are calculated separately due to the large spin–orbit splitting, which eases the application of different damping parameters compared to cases when these edges overlap.

4.2. Application to Larger Systems. All-electron relativistic 4c DFT calculations of XAS spectra have in the past been limited to small molecules due to their computational cost. However, recent theoretical advances implemented in RESPECT⁸⁵ or more specifically in its DR-TDDFT module⁶³ have made it possible to tackle XAS of larger and chemically relevant systems. As examples, we employed the calibrated computational protocol (PBE0-60HF, VDZ/aVDZ) and investigated: (a) a ruthenium anticancer prodrug $[RuCl_2(DMSO)_2(Im)_2]$ (Figure 12a) related to chemotherapeutics NAMI-A and KP1019¹²⁴ that consists of 41 atoms and 4652 4c basis spinors; (b) a tungsten complex $[WCl_4(PMePh_2)_2]$ (Figure 12b) used to study the influence of the W oxidation state on XAS spectra¹²¹ that consists of 59 atoms and 7212 4c basis spinors.

4.2.1. $[RuCl_2(DMSO)_2(Im)_2]$. An interesting feature of the XAS spectrum of $[RuCl_2(DMSO)_2(Im)_2]$ is the proximity of the Ru L_3 -edge and the Cl K-edge (Figure 13), which offers a great opportunity to address XAS signals for p- and d-type elements in a single run. The calculated position of the Cl K-edge is 2812.5 eV while that of the Ru L_3 -edge is 2836.4 eV, and they differ from the experiment by -9.8 eV (0.35%) for the Cl K-edge and by -4.7 eV (0.17%) for the Ru L_3 -edge, respectively. In other words, both Cl and Ru XAS transition energies are underestimated, although the difference is rather small considering the total energy of the transitions. A less satisfactory result is obtained when comparing the separation between these edges; the values are 23.9 eV (calculation) vs 18.8 eV (experiment). The energy of the Cl transition is underestimated more than the L_3 -edge of Ru, which is the reason for the increased separation between the edges in

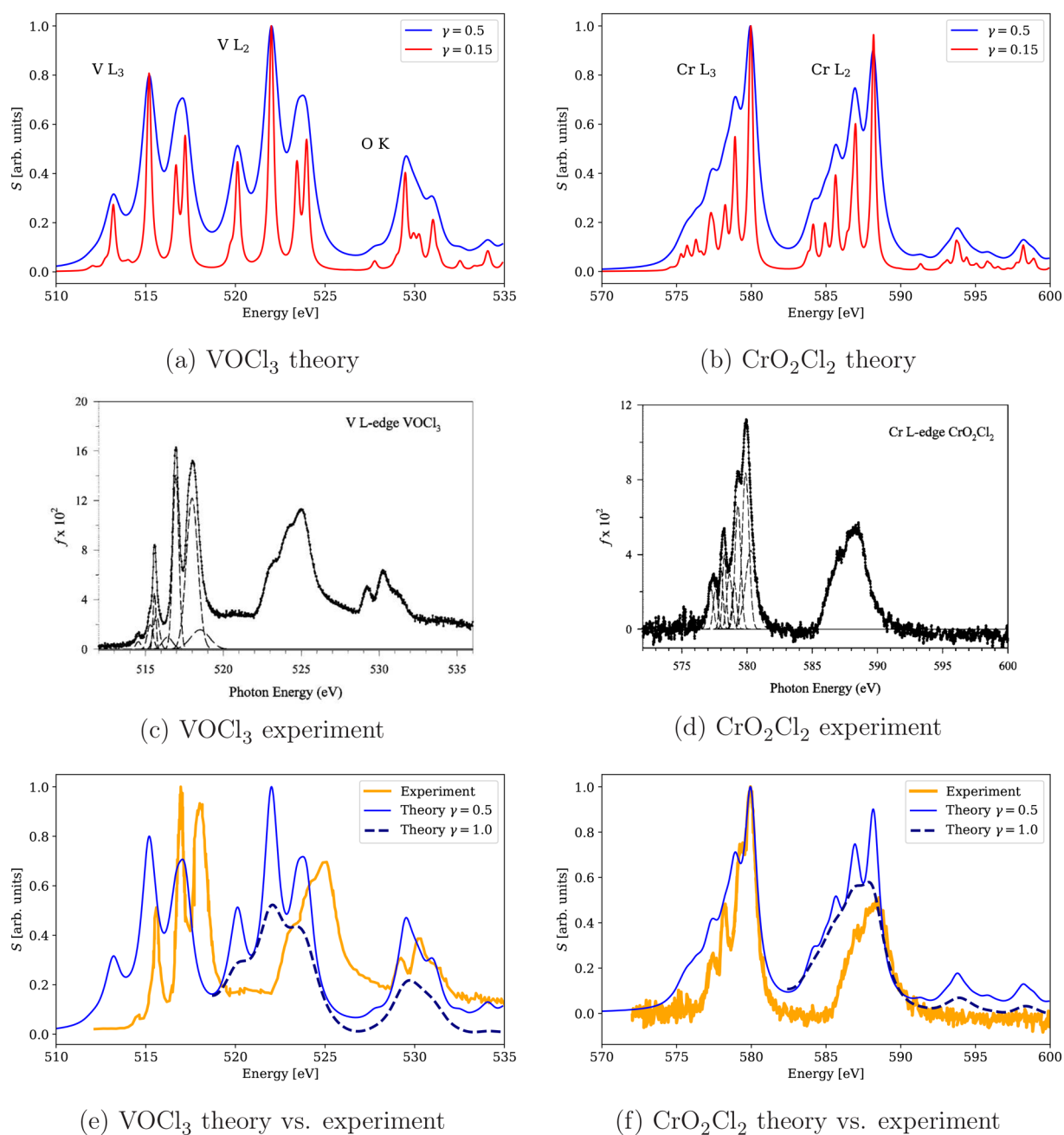


Figure 10. Calculated 4c-DR-TDDFT (PBE0-S0HF, VDZ/aVDZ) XAS spectra near vanadium and chromium $L_{2,3}$ -edges and oxygen K-edge of VOCl_3 and CrO_2Cl_2 using different damping parameters and their comparison with the experimental results.⁶¹ The spectra were normalized by setting the maximum to unity with the exception of $\gamma = 1.0$ spectra in (e) and (f), which were normalized to preserve the intensity ratio of the maxima for $\gamma = 1.0$ and $\gamma = 0.5$ as well as shifted on the vertical axis to connect with $\gamma = 0.5$ spectra. (a) VOCl_3 theory, (b) CrO_2Cl_2 theory, (c) VOCl_3 experiment, (d) CrO_2Cl_2 experiment, (e) VOCl_3 theory vs experiment, and (f) CrO_2Cl_2 theory vs experiment, (c, d) Reprinted from ref 61. Copyright 2009 American Chemical Society.

comparison with the experiment. This could be due to K-edges at this energy range requiring a different amount of HFX than the Ru L_3 -edge. However, a detailed investigation of this is beyond the scope of this paper.

A very broad peak located between both edges and attributed to transitions from the $1s_{1/2}$ orbital of Cl to upper-lying virtual orbitals was found closer to the Cl edge in the experiment. While this spectral feature was predicted correctly by calculations with the calibrated computational protocol (PBE0-60HF, VDZ/aVDZ), results obtained with a smaller VDZ/aVDZ basis assign its position closer to the Ru L_3 -

edge, as seen in Figure 13. At the same time, both basis sets perform equally well for the main XAS edges (their energies and intensities are essentially the same). While the application of the VDZ/aVDZ basis was motivated by its relatively good performance for smaller test systems and by an attempt to explore a computationally less expensive scheme for larger systems; this example shows that the basis set augmentation for light elements is mandatory, regardless of the size and complexity of the investigated molecules.

4.2.2. $[\text{WCl}_4(\text{PMePh}_2)_2]$. The second complex studied, $[\text{WCl}_4(\text{PMePh}_2)_2]$, was originally investigated experimentally

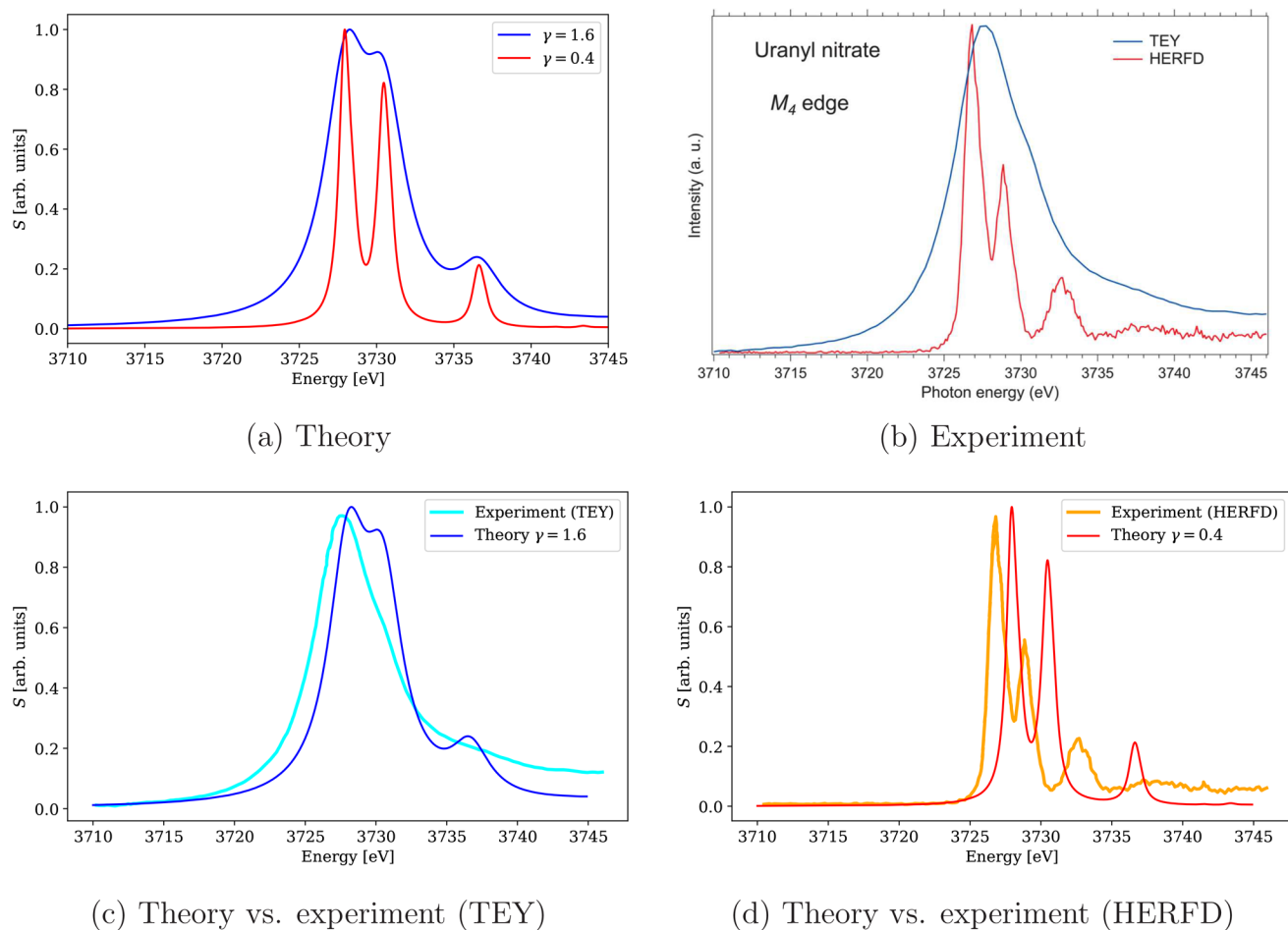


Figure 11. Calculated 4c-DR-TDDFT (PBE0-60HF, VDZ/aVDZ) XAS spectra near the uranium M_4 -edge of $UO_2(NO_3)_2$ using different damping parameters and their comparison with the experimental results.¹²² The spectra were normalized by setting the maximum to unity. (a) Theory and (b) experiment (reprinted from ref 122, copyright 2016 American Chemical Society). (c) Theory vs experiment (TEY); (d) theory vs experiment (HERFD).

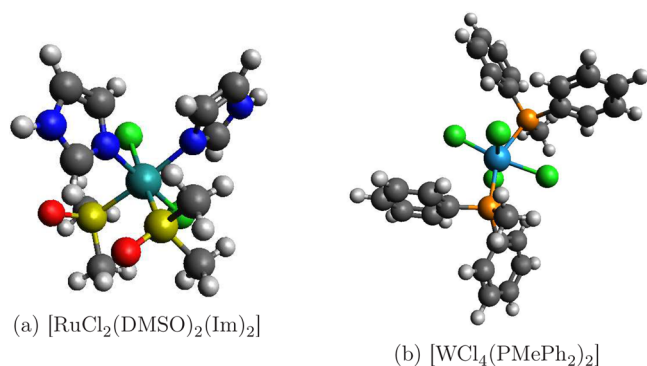


Figure 12. Structures of the larger metal complexes: (a) $[RuCl_2(DMSO)_2(Im)_2]$; (b) $[WCl_4(PMePh_2)_2]$.

by Jayarathne et al.¹²¹ in a study of L_1 -, L_2 -, and L_3 -edge spectra of tungsten complexes with different oxidation numbers. Inspired by this work, we have calculated the L_2 - and L_3 -edge spectra of the closed-shell $[W^{IV}Cl_4(PMePh_2)_2]$ complex and compared them with the $W^{VI}Cl_6$ complex from the test set. Figure 14 shows L_2 - and L_3 -edge spectra of WCl_6 and $[WCl_4(PMePh_2)_2]$ calculated with two different damping parameters and the experimental spectra of various tungsten species from ref 121. All calculated spectra are normalized such

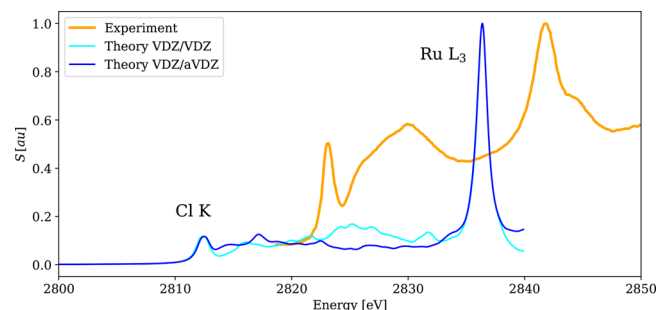


Figure 13. Calculated 4c-DR-TDDFT (PBE0-60HF, $\gamma = 0.5$) XAS spectra near chlorine K-edges and ruthenium L_3 -edges of $[RuCl_2(DMSO)_2(Im)_2]$ and their comparison with existing experimental results.¹²⁴

that the most intense peak has unit intensity. A larger damping factor ($\gamma = 3.0$) was employed for better resemblance with the experiment; see the black and green lines in Figure 14c for the experimental spectra of WCl_6 (line f) and $[WCl_4(PMePh_2)_2]$ (line d), respectively. On the other hand, spectra calculated using a smaller damping parameter ($\gamma = 0.15$) shown by dashed lines were used to identify individual transitions, which comprise the white lines. As both compounds have roughly an octahedral ligand sphere, these narrow peaks correspond to the

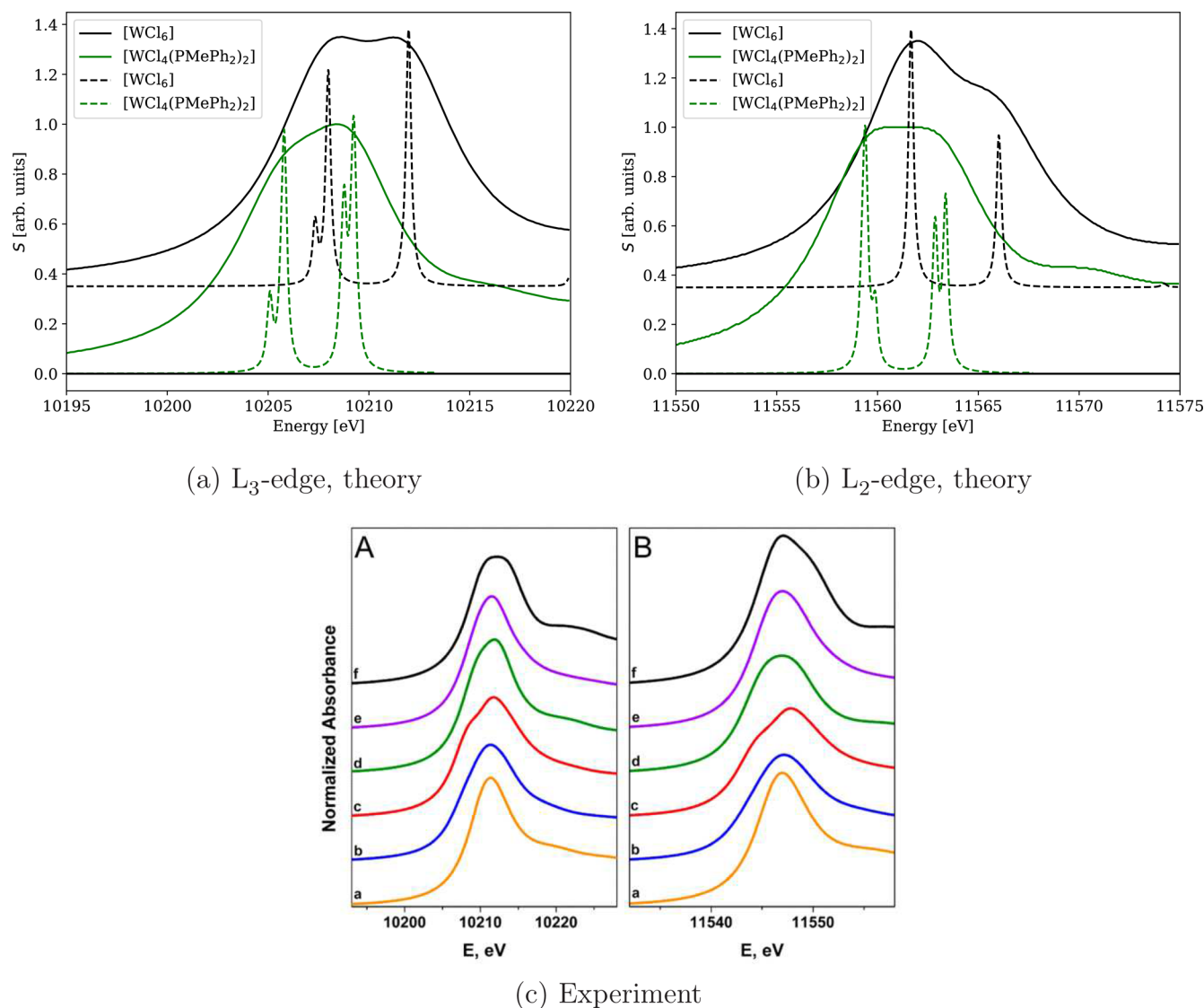


Figure 14. Calculated 4c-DR-TDDFT (PBE0-60HF, VDZ/aVDZ) XAS spectra of WCl_6 and $[WCl_4(PMePh_2)_2]$ near the tungsten L_3 -edge (a) and L_2 -edge (b) with two different damping parameters, $\gamma = 3.0$ (solid line) and $\gamma = 0.15$ (dashed line). The compounds correspond to lines f and d in the experimental spectra¹²¹ (c) (panel A L_3 -edge, panel B L_2 -edge) and are color coded the same way: (a) L_3 -edge, theory, (b) L_2 -edge, theory, and (c) experiment (reprinted from ref 121, copyright 2014 American Chemical Society).

transitions from the tungsten 2p shell into its unoccupied d orbital sets. In (nonrelativistic) point-group notation, these orbitals are labeled t_{1u} for occupied and t_{2g} and e_g for unoccupied states. In the relativistic case, the correct language for symmetries is provided by double point groups.¹²⁵ Here, the core $p_{1/2}$ and $p_{3/2}$ orbitals belong to representations $E_{1/2,u}$ and $F_{3/2,w}$ respectively. Due to their atomic nature, this is true for both WCl_6 and $[WCl_4(PMePh_2)_2]$. The unoccupied orbitals in WCl_6 belong to $F_{3/2,g}$ (a combination of t_{2g} and e_g) and $E_{5/2,g}$ (t_{2g}) representations; see Figure 15. On the other hand, in $[WCl_4(PMePh_2)_2]$, the octahedral symmetry is broken, which leads to further splitting of $F_{3/2,g}$ while no transitions are symmetry forbidden. In the L_2 -edge spectra of octahedral WCl_6 (Figure 14b), only two signals at 11561.7 eV ($E_{1/2,u} \rightarrow F_{3/2,g}$) and 11566.0 eV ($E_{1/2,u} \rightarrow F'_{3/2,g}$) are present. This is due to the fact that only transitions $E_{1/2,u} \rightarrow F_{3/2,g}$ are allowed while the transition $E_{1/2,u} \rightarrow E_{5/2,g}$ is forbidden. This is also reflected in the absence of the forbidden transition in the MO analysis (see Figures S11 and S12). The intensity ratio of

the observed transitions is 3.26:2 (t_{2g}/e_g), which is close to the ideal 3:2 ratio, but due to the forbidden transition, this does not reflect the number of vacant orbitals. The calculated energy difference of these signals, corresponding to ligand field splitting (LFS), is 4.3 eV, which is higher than the experimental value of 3.4 eV. The larger computed splitting may be due to the increased HFX in the functional (60%), as the LFS calculated using the standard PBE0 functional is 3.6 eV, i.e., much closer to the experimental value. Further investigations are needed to determine whether these observed changes in LFS with different amounts of exact exchange are also manifested in other, similar complexes.

In the L_2 -edge spectrum of WCl_6 , the splitting into two levels corresponds to the expectations from nonrelativistic considerations. However, this is due to the forbidden transition. On the other hand, in the L_3 -edge spectrum, the transition $F_{3/2,u} \rightarrow E_{5/2,g}$ is allowed. Thus, we see an additional peak in the spectrum resulting from the spin-orbit splitting of the t_{2g} level. Note, however, that the t_{2g} is mixed also in $F'_{3/2,g}$.

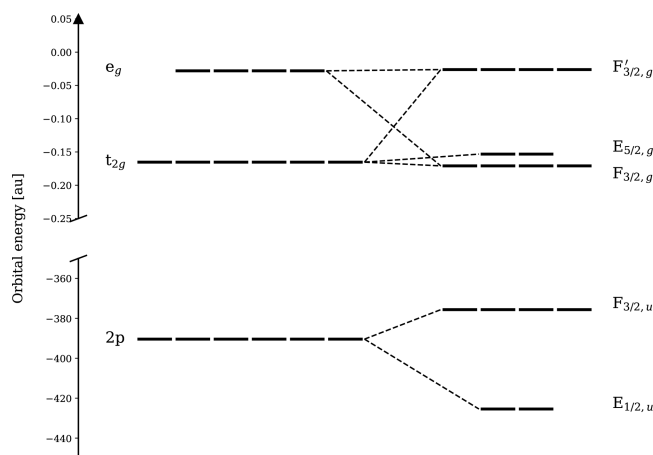


Figure 15. Schematic MO diagram of WCl_6 showing the assignment of its core and valence spin-orbitals to double point group irreducible representations. The orbital energies without SO coupling were obtained using the scalar-relativistic Douglas–Kroll–Hess Hamiltonian of the second-order. The contributions of the atomic 5d orbitals to the molecular orbitals show the combined effect of the SO interaction and the octahedral ligand field: $F_{3/2,g} = d_{3/2,\pm 3/2}, d_{3/2,\pm 1/2}$, $E_{5/2,g} = (1/6)^{1/2} d_{5/2,5/2} - (5/6)^{1/2} d_{5/2,-3/2}, (1/6)^{1/2} d_{5/2,-5/2} - (5/6)^{1/2} d_{5/2,3/2}$, $F_{3/2,g} = (5/6)^{1/2} d_{5/2,5/2} + (1/6)^{1/2} d_{5/2,-3/2}, (5/6)^{1/2} d_{5/2,-5/2} + (1/6)^{1/2} d_{5/2,3/2}, d_{5/2,\pm 1/2}$.

The presence of two different sets of ligands in $[\text{WCl}_4(\text{PMePh}_2)_2]$ breaks the octahedral symmetry and lifts the degeneracy of the $F_{3/2,g}$ and $F'_{3/2,g}$ levels. This is manifested as an ~ 0.5 eV splitting of narrow signals in both the L_2 - and L_3 -edge spectra. Instead of the original three levels $F_{3/2,g}$, $E_{5/2,g}$, and $F'_{3/2,g}$ in WCl_6 , five levels (each doubly degenerate) appear now with the lowest being fully occupied due to the lower oxidation number of W in $[\text{WCl}_4(\text{PMePh}_2)_2]$. Therefore, in both L_2 - and L_3 -edge spectra, we observe four signals in place of the two and three of WCl_6 .

Let us now compare the spectra of both compounds with respect to the differences in the tungsten oxidation state. According to Jayarathne et al.,¹²¹ the change of the tungsten oxidation state from IV to VI is accompanied by (a) a shift of both L_2 and L_3 white lines toward higher energies; (b) an increase of the absolute intensity of white lines; (c) different peak shapes attributed to the increase of the intensity of transitions into the t_{2g} state compared to the e_g state due to the increased number of vacancies in the t_{2g} orbitals. All these effects are also seen in the calculated spectra: (a) the $\text{W}^{\text{VI}}\text{Cl}_6$ white line peaks are shifted toward higher energies with respect to the $[\text{W}^{\text{IV}}\text{Cl}_4(\text{PMePh}_2)_2]$ complex (Figure 14); (b) their absolute intensities are higher (about 1.5-times for L_2 and 1.1-times for L_3 , not shown in the figure due to normalization); (c) the shapes of the calculated peaks are in excellent agreement with the experimentally obtained ones; see Figure 14. However, the interpretation of the observed line shapes in the framework of double group theory, i.e., with the inclusion of relativistic effects, is more involved. The change in overall shape of the broad peaks (full lines in Figure 14) with a change in oxidation state in both L_3 - and L_2 -edges is attributed to the relative increase of the intensity of the lower-energy transitions compared to the higher-energy ones (revealed by the dashed lines in Figure 14). Within an absorption edge, the transitions at higher energy are from core orbitals to four $F'_{3/2,g}$ spinors in $\text{W}^{\text{VI}}\text{Cl}_6$ (see Figure 15) and their four broken symmetry counterparts in $[\text{W}^{\text{IV}}\text{Cl}_4(\text{PMePh}_2)_2]$. The transitions at lower

energy are from core orbitals to four $F_{3/2,g}$ and two $E_{5/2,g}$ spinors in $\text{W}^{\text{VI}}\text{Cl}_6$ but only to four spinors in $[\text{W}^{\text{IV}}\text{Cl}_4(\text{PMePh}_2)_2]$ due to the lowest two spinors being occupied. In the L_3 -edge spectra (Figure 14b), the shift of broad peak intensity maxima toward lower energies from $[\text{W}^{\text{IV}}\text{Cl}_4(\text{PMePh}_2)_2]$ to $\text{W}^{\text{VI}}\text{Cl}_6$ can thus be attributed to the increased number of vacancies. However, this argument is problematic in the L_2 -edge spectra (Figure 14b) due to the forbidden transition of $E_{1/2,u} \rightarrow E_{5/2,g}$. However, its broken symmetry-allowed counterpart transition in $[\text{W}^{\text{IV}}\text{Cl}_4(\text{PMePh}_2)_2]$ is of comparatively low intensity and appears only as a minor shoulder of the main peak in the dashed-line spectrum. Thus, in the L_2 -edge spectra (Figure 14b), the $\text{W}^{\text{VI}}\text{Cl}_6$ signal has maximum intensity around the position of the $F_{3/2,g}$ transition, whereas the $[\text{W}^{\text{IV}}\text{Cl}_4(\text{PMePh}_2)_2]$ signal features a broad plateau on the top. To summarize, the presented four-component scheme could be used not only to calculate spectra of even relatively large and chemically relevant systems but also to facilitate an in-depth analysis of individual signals in the framework of double point groups to explain the observed spectral shapes.

5. CONCLUSIONS

In this work, we applied our recently developed four-component (4c) relativistic linear damped response time-dependent density functional theory (DR-TDDFT) based on the Dirac–Coulomb Hamiltonian including scalar and SO relativistic effects variationally to calculate the XAS spectra of transition metal and actinide compounds. We performed a calibration to determine the best computational protocol in terms of molecular geometry, basis set, exchange–correlation (xc) functional, and other computational parameters to reproduce experimental spectra of systems with different central atoms, ligands, and oxidation states. The differences between spectra calculated at a computationally optimized geometry and at an experimental geometry were found to be negligible, supporting the use of the optimized geometries in all calculations. While the main absorption lines were already described well using a comparatively small basis set of VDZ quality, a reliable description of the secondary peaks required basis sets of at least augmented VDZ (aVDZ) quality for the light elements.

Hybrid functionals were found to perform better than pure functionals. Range-separated functionals provided no further improvement. The variational inclusion of relativity at the 4c-level of theory allowed the effects of both scalar and spin–orbit relativistic effects on the position and shape of the X-ray spectra to be treated. The SO splittings were reproduced well for all systems. By adjusting the amount of Hartree–Fock exchange (HFX) in the hybrid xc functionals, we found that the shift in absorption energies compared to the experiment depends linearly on the amount of HFX. This linear dependence allowed us to determine an optimal amount of HFX that minimizes the energy shift from the experiment. For most of the absorption bands above 1000 eV, the optimal value was close to 60%, which we propose as a rule of thumb for calculating XAS spectra using relativistic TDDFT. Such a setup yields relative errors below 0.2% and below 2% for line energies and SO splittings, respectively. However, at lower energies, the optimal amount varied from 55% to 40% and caution is advised in these cases. While the increase of the HFX amount has been suggested by previous studies, the

present work is the first one performed at the 4c relativistic level of theory and focused on L- and M-edges.

Finally, using the optimized methodology, we calculated XAS spectra of larger systems of chemical interest. For $[\text{RuCl}_2(\text{DMSO})_2(\text{Im})_2]$, we have reproduced the spectra in a region where Ru L₃-edge and Cl K-edge overlap. Furthermore, for L_{2,3}-edge spectra of $[\text{WCl}_4(\text{PMePh}_2)_2]$, we resolved broad experimental peaks into well-separated lines and thus provided a ligand field theory-based interpretation and explained the differences in the spectra of this W^{IV} system and the W^{VI} molecule WCl₆.

Our results demonstrate the necessity of using multi-component relativistic methodologies to calculate XAS spectra near metal L- and M-edges dominated by SO coupling. DR-TDDFT allows for the direct calculation of XAS spectra in the frequency domain for a user-defined spectral range. Non-physical peaks resulting from valence to continuum excitations can be removed in DR-TDDFT by selecting an MO window for which the elements of the perturbation operator remain untouched while the elements outside the window are set to zero. Standard hybrid functionals with scaled HFX and relatively small basis sets of VDZ or aVDZ quality are sufficient to reproduce experimental spectra, making such relativistic calculations feasible even for systems with 50–100 atoms. These results show how the accuracy of DFT-based calculations of XAS spectra can be advanced such that the calculated spectra fall into the same range as experimental ones without the need for large shifts that were required before.

■ ASSOCIATED CONTENT

SI Supporting Information

The Supporting Information is available free of charge at <https://pubs.acs.org/doi/10.1021/acs.inorgchem.1c02412>.

Further calculated spectra, discussion of MO window for the perturbation operator, and molecular geometries (PDF)

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Notes

The authors declare no competing financial interest.

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